

Plan

Basics

Images as Arrays

Numeric types

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ImageJ

Segmentation

Logical images

Threshold

Logical operations

Object properties

Morphology

Image  
alignment

Filters

Explained

Convolution

Fancier filters

Summary

# Microscope Image Analysis

David Miguel Susano Pinto

Micron Advanced Microscopy Course, 2019

# Microscope Image Analysis in 3 parts

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### Summary

- ① What is in a microscope image
  - What is in a image?
  - Image display
  - Image acquisition
- ② Careful with your data
  - File formats
  - OMERO
  - Figure preparation
- ③ Images as N dimensional numeric arrays
  - N dimensional images
  - Spatial filters
  - Morphology
  - Connected components
  - Tools

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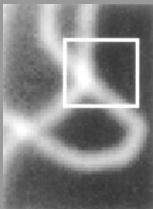
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63	84	119	<b>172</b>	<b>219</b>	<b>225</b>	182	135	79	51	36	24	23	19	15	-1	14	14	8	0	-4	7	18
78	84	104	<b>170</b>	<b>223</b>	<b>224</b>	196	118	84	49	36	28	16	11	25	4	15	13	8	-4	9	11	7
61	80	115	<b>153</b>	<b>209</b>	<b>204</b>	170	113	73	46	41	29	9	17	11	11	0	12	-2	2	2	3	23
72	98	121	<b>160</b>	<b>190</b>	<b>207</b>	178	116	68	50	29	22	17	19	7	27	15	9	-3	-4	14	5	8
64	90	132	<b>167</b>	<b>210</b>	<b>214</b>	180	115	71	37	36	31	13	15	9	8	15	6	0	5	-14	4	12
75	93	124	<b>169</b>	<b>216</b>	<b>229</b>	196	107	71	56	19	18	22	24	7	5	15	11	8	-1	12	6	7
97	87	128	<b>193</b>	<b>210</b>	<b>225</b>	193	111	85	47	27	27	21	12	5	2	-1	4	1	-3	7	2	-10
103	108	134	<b>180</b>	<b>201</b>	<b>233</b>	185	115	55	38	26	25	15	20	18	6	2	2	1	4	-3	-13	0
142	132	161	<b>216</b>	<b>238</b>	<b>223</b>	160	90	59	45	17	10	9	13	10	11	4	-9	5	2	7	0	5
172	162	175	<b>231</b>	<b>239</b>	<b>238</b>	155	88	48	28	24	17	15	13	0	14	0	11	-3	4	9	0	-10
226	219	230	<b>260</b>	<b>265</b>	<b>236</b>	161	92	43	31	31	11	5	11	7	13	19	9	18	-11	-9	-2	8
<b>234</b>	<b>247</b>	<b>256</b>	<b>302</b>	<b>311</b>	<b>253</b>	174	97	48	27	12	15	7	7	0	16	8	5	3	-4	0	-6	4
<b>260</b>	<b>263</b>	<b>297</b>	<b>346</b>	<b>349</b>	<b>303</b>	196	126	65	27	30	24	3	6	7	1	12	3	9	0	-2	-13	2
<b>244</b>	<b>293</b>	<b>340</b>	<b>388</b>	<b>399</b>	<b>321</b>	223	130	74	29	24	30	17	4	3	11	0	8	7	-3	-2	-2	-2
<b>209</b>	<b>273</b>	<b>359</b>	<b>423</b>	<b>436</b>	<b>365</b>	264	141	80	57	32	45	13	3	18	8	-7	0	-6	4	-1	-2	-3
176	253	<b>342</b>	<b>430</b>	<b>443</b>	<b>394</b>	291	161	86	59	37	23	18	5	0	7	8	11	1	-3	13	-5	-2
152	218	311	<b>425</b>	<b>470</b>	<b>420</b>	326	208	111	66	52	29	28	9	4	7	8	4	-7	11	-18	-13	-2
129	199	<b>294</b>	<b>413</b>	<b>469</b>	<b>441</b>	<b>384</b>	<b>257</b>	148	111	69	34	20	20	6	3	15	4	-2	-6	-3	-10	9
140	<b>206</b>	<b>294</b>	<b>385</b>	<b>439</b>	<b>442</b>	<b>365</b>	<b>310</b>	<b>223</b>	157	114	76	45	28	9	21	5	15	-4	-13	0	-5	-1
173	<b>233</b>	<b>309</b>	<b>354</b>	392	375	333	<b>303</b>	<b>261</b>	<b>214</b>	135	92	51	47	18	12	13	12	20	-9	4	1	15
<b>221</b>	<b>278</b>	<b>300</b>	<b>321</b>	306	293	286	279	<b>250</b>	<b>231</b>	<b>184</b>	<b>142</b>	108	67	41	18	13	5	8	-8	0	7	5
<b>267</b>	<b>302</b>	291	244	228	211	201	215	241	<b>227</b>	<b>205</b>	<b>184</b>	<b>136</b>	110	68	51	26	11	8	3	0	8	-3
<b>284</b>	<b>279</b>	257	202	133	129	137	151	183	213	<b>209</b>	<b>188</b>	<b>187</b>	<b>155</b>	109	69	49	26	25	8	8	18	-4
275	248	191	143	95	85	87	98	122	166	184	<b>192</b>	<b>206</b>	<b>194</b>	<b>176</b>	<b>135</b>	98	50	44	19	21	0	1

# Images as Signals

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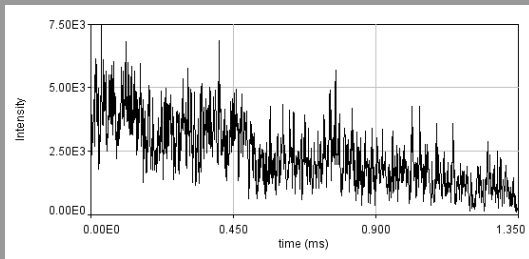
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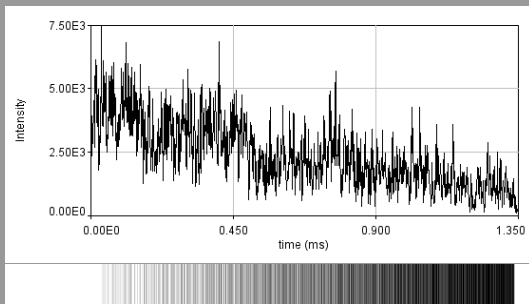
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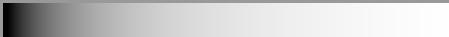
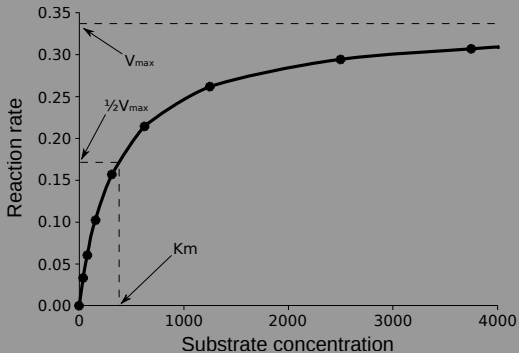
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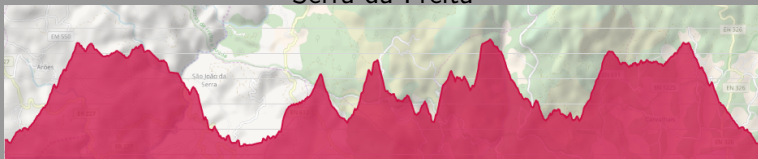
Explained

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## Serra da Freita



# Images as Signals

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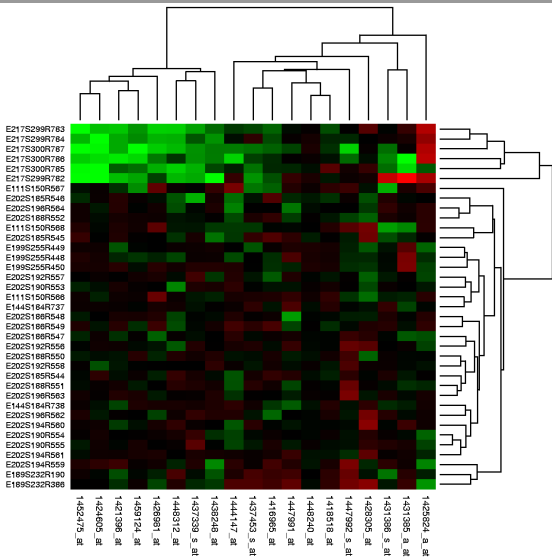
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### Image alignment

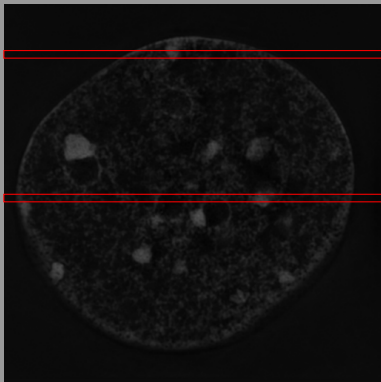
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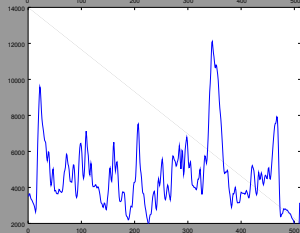
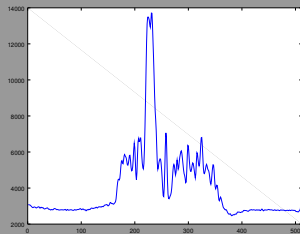
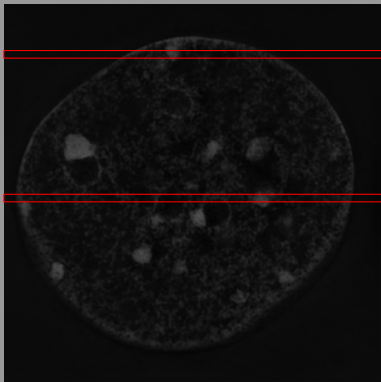
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# Images as Surfaces

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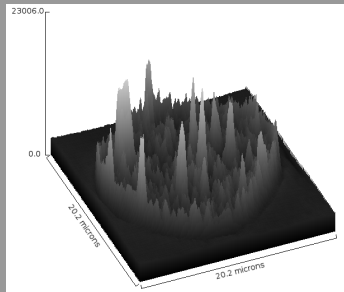
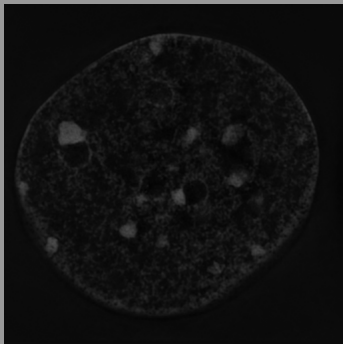
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# Images as ND Arrays

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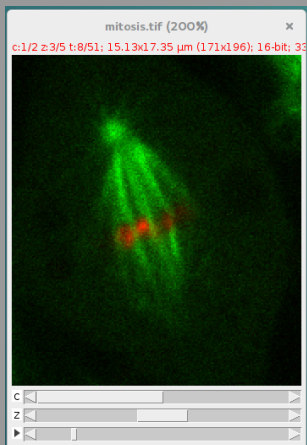
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- x and y
- time
- z (volume)
- wavelength
- phase
- stage angle

Think "data", not "picture"



# Localisation Microscopy

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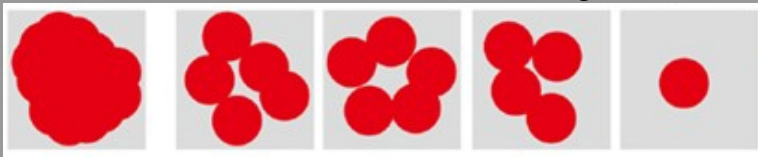
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## Diffraction limited fluorescence images



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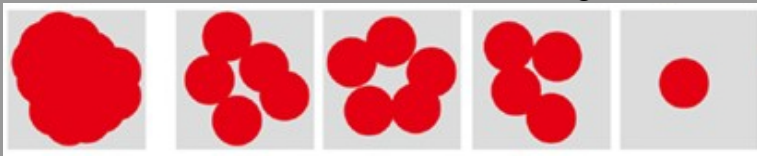
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## Diffraction limited fluorescence images



## Localised fluorophores



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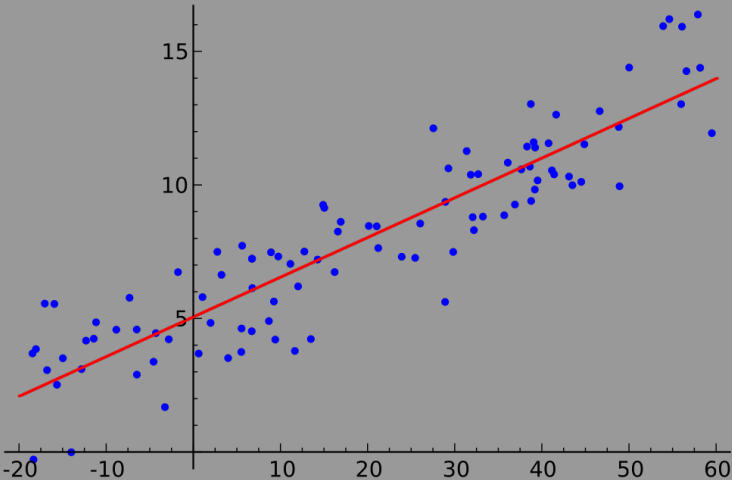
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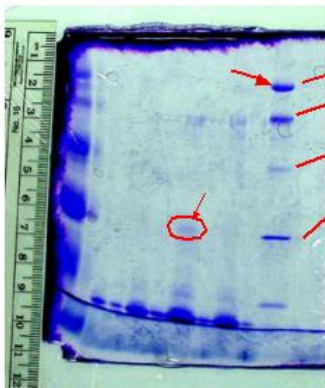
Filters

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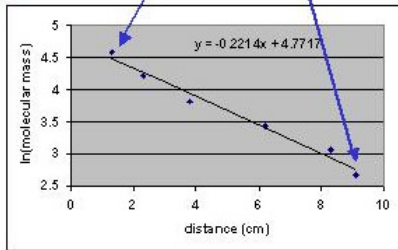
Convolution

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Summary



molec. mass	distance	ln(mass)
97.4	1.3	4.57883
68	2.3	4.21951
45	3.8	3.80666
31	6.2	3.43399
21.5	8.3	3.06805
14.3	9.1	2.66026



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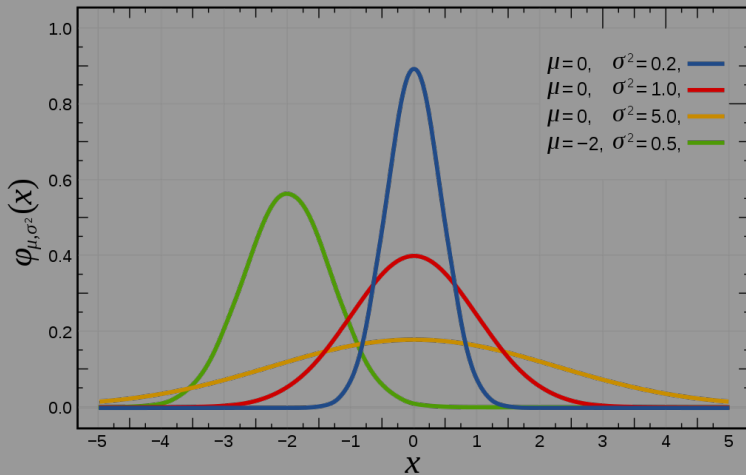
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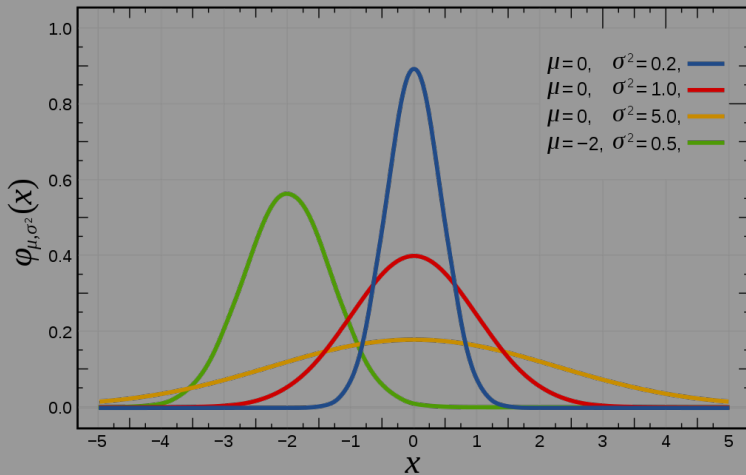
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Check line profile of a bead.

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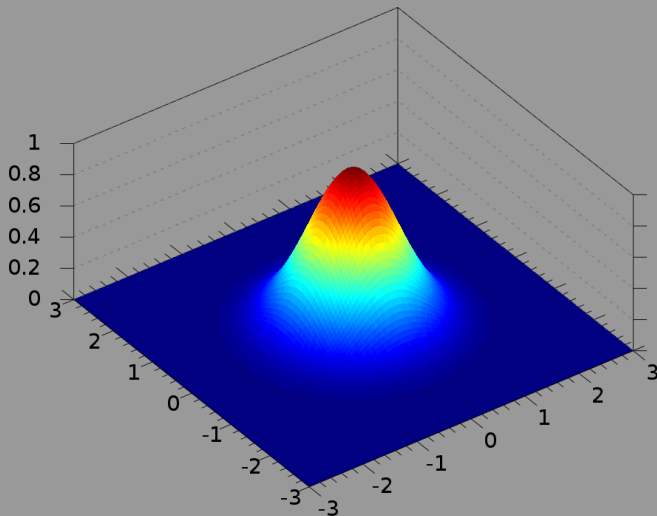
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# Localisation imaging

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Table of coordinates.



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Table of coordinates.  
What is the pixel size?

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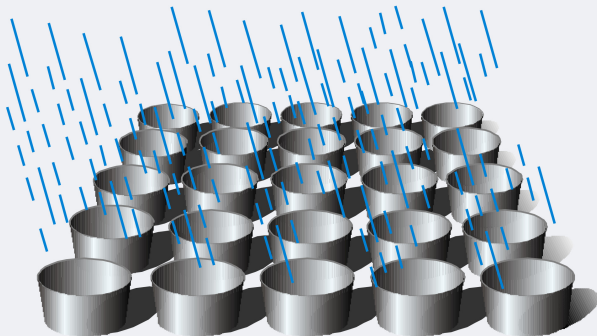
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### Summary



*Array of Discrete Photodetectors*

# Image Reconstruction

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- Localisation Microscopy (STORM/PALM)
- Structured Illumination

Two step process

# Integer types

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Images as Arrays		$2^3$	8
Numeric types		$2^4$	16
Tools		$2^5$	32
ImageJ		$2^6$	64
Segmentation		$2^7$	128
Logical images		$2^8$	256
Threshold		$2^9$	512
Logical operations		$2^{10}$	1024
Object properties		$2^{11}$	2048
Morphology		$2^{12}$	4096
Image alignment		$2^{13}$	8192
Filters		$2^{14}$	16384
Explained		$2^{15}$	32768
Convolution		$2^{16}$	65536
Fancier filters		$2^{17}$	131072
Summary	...		
		$2^{18}$	262144
		$2^{19}$	524288

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**Numeric types**

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	unique values	min	max
$2^1$	2	-1	0
$2^2$	4	-2	1
$2^3$	8	-4	3
...			
$2^8$	256	-128	127
$2^{32}$	4294967296	-2147483648	2147483647

# Floating point

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The diagram illustrates the bit layout of a floating point number. At the top, a horizontal bar represents 32 bits, indexed from 31 on the left to 0 on the right. Bit 31 is the sign bit (S). Bits 30 through 23 form the 8-bit exponent (EXPONENT). Bits 22 through 0 form the 23-bit mantissa (MANTISSA). Below this, a box shows the three sections: S, EXPONENT, and MANTISSA. The text 'Floating Point internals.' is centered above this box. Below the box, the text 'The three sections of a floating Point number.' is centered. At the bottom, the text 'So far, so good. Now, how numbers are interpreted is usually explained with the formula:' is followed by the formula  $(-1)^S * 1.M * 2^{(E-127)}$ .

Floating points — sometimes incorrectly called 32 bit.

# Tools for image analysis

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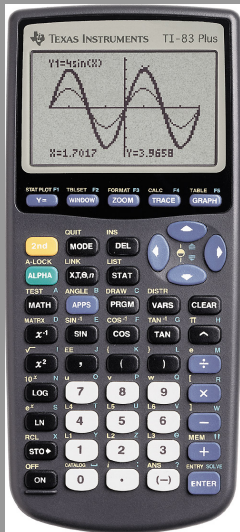
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ImageJ / FIJI



Python with NumPy



Octave



R



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ImageJ / FIJI



Python with NumPy



Octave



R

- CellProfiler
- Icy
- OMERO
- KNIME

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Python with NumPy



Octave



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- CellProfiler
- Icy
- OMERO
- KNIME
- Imaris
- softWoRx
- Velocity
- Matlab
- Metamorph
- Image-Pro Plus
- Huygens
- Mathematica
- ...

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Summary

- *de facto* standard in medical sciences
- libre software (free and open source)
- massive helpfully massive community



ImageJ1



ImageJ2



FIJI

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## Concentration

Protein expression, number of complexes.

## Co-localization

Do two overlap and correlate?

## Dynamics

How fast does it move?

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## Summary

## Concentration

Protein expression, number of complexes.

## Co-localization

Do two overlap and correlate?

## Dynamics

How fast does it move?

All require identifying a region of interest.

# Logical (binary) images

Very useful as masks

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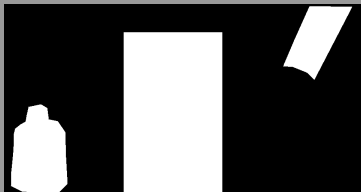
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# Logical (binary) images

Very useful as masks

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#### alignment

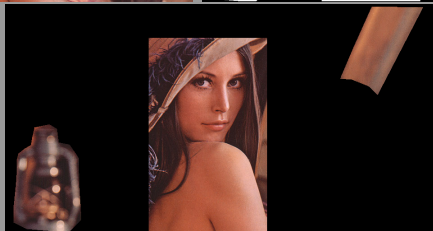
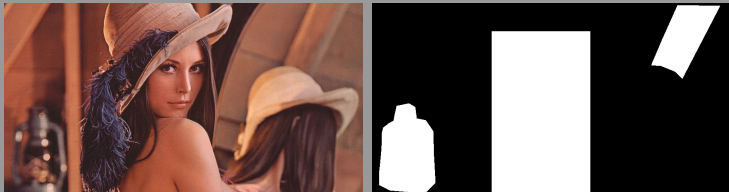
### Filters

Explained

Convolution

Fancier filters

### Summary



# Manual threshold

## Plan

## Basics

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Numeric types

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## Segmentation

Logical images

**Threshold**

Logical operations

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Morphology

## Image alignment

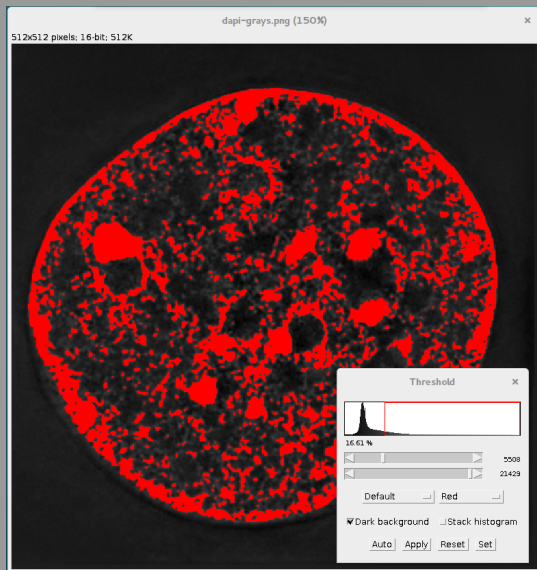
## Filters

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# Automatic threshold

## Triangle algorithm

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Image alignment

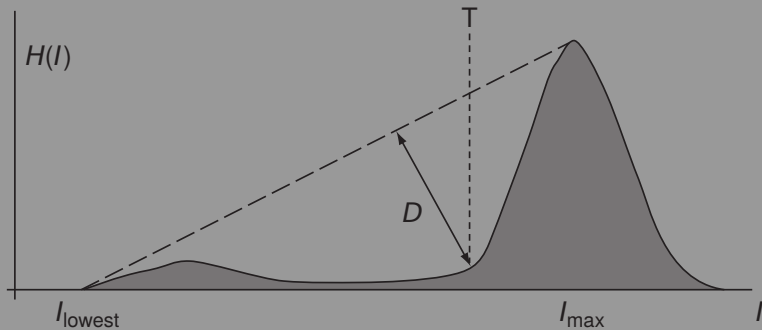
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# Automatic threshold

## Triangle algorithm

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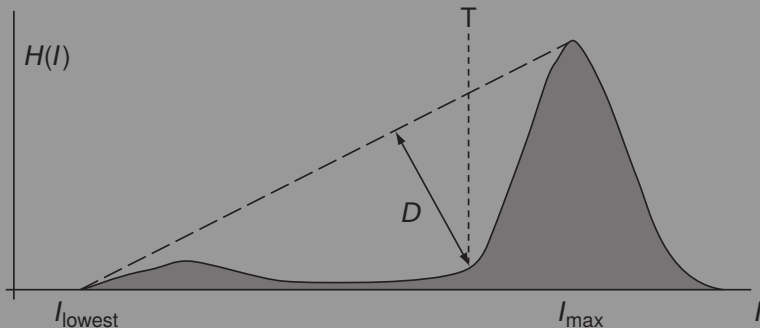
### Filters

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- histogram smoothing (mean filter)

# Automatic threshold

## Otsu's algorithm

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### Image

### alignment

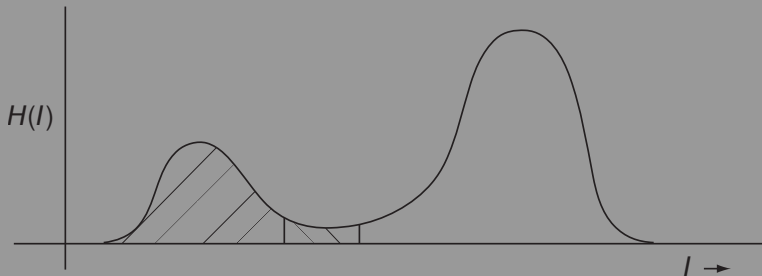
### Filters

Explained

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### Summary



- bimodal histogram
- reduce intra-class variance (spread)

# Logical operations

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## Image

alignment

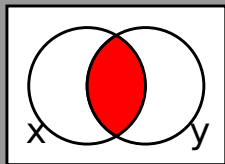
## Filters

Explained

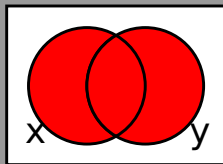
Convolution

Fancier filters

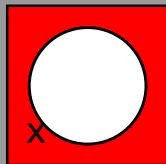
## Summary



x AND y



x OR y



NOT x

# Logical operations

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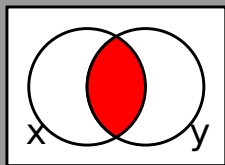
Filters

Explained

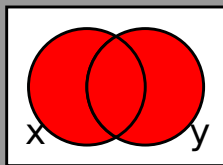
Convolution

Fancier filters

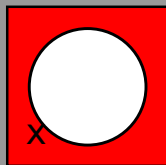
Summary



$x \text{ AND } y$



$x \text{ OR } y$



$\text{NOT } x$

Example: split plant cells with cell membrane.

# colocalisation

Plan

Basics

- Images as Arrays
- Numeric types
- Tools
- ImageJ

Segmentation

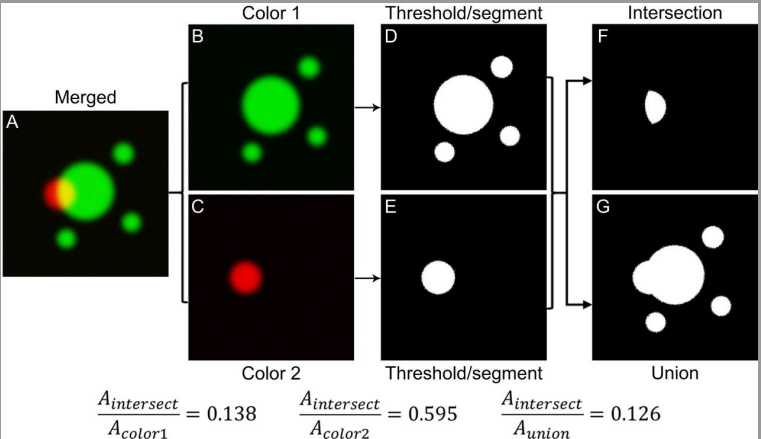
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#### alignment

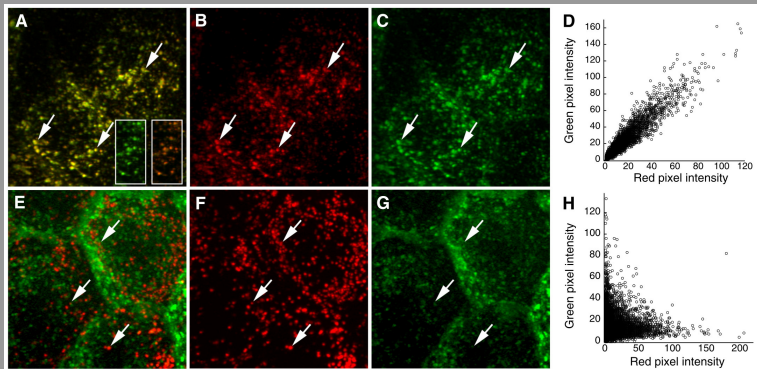
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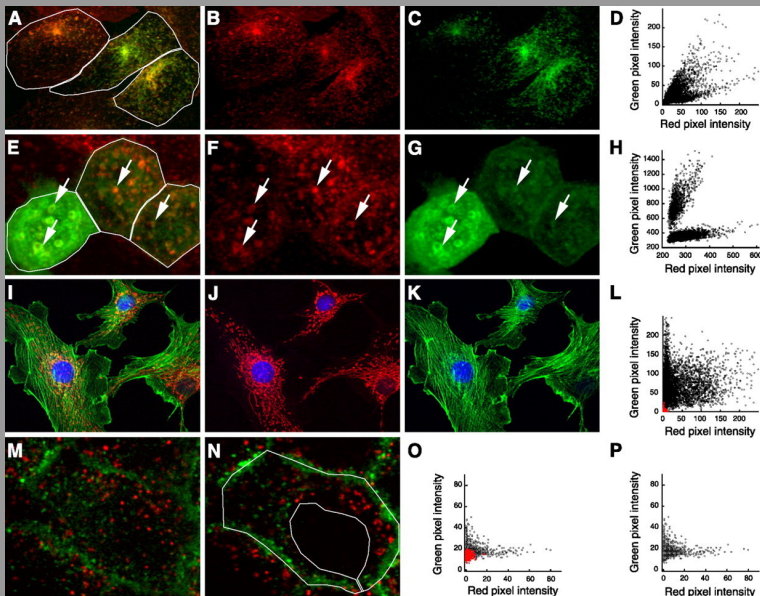
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# Object properties

## Particle/Region/ROI properties/measurements

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#### Summary

These are always one button or one line of code. The only problem is getting to this point.

- area
- eccentricity
- centroid
- center of mass
- integrated density
- min and max
- perimeter

# Erosion and dilation

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### Summary



Dilation



Closing



Erosion



Opening

# Erosion and dilation

## Plan

### Basics

- Images as Arrays
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### Segmentation

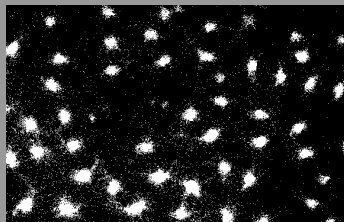
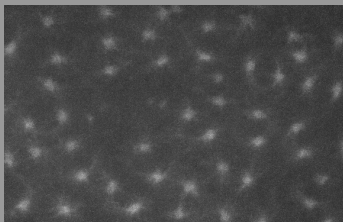
- Logical images
- Threshold
- Logical operations
- Object properties
- Morphology

### Image alignment

### Filters

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### Summary



# Reconstruction from markers

## Plan

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### Image alignment

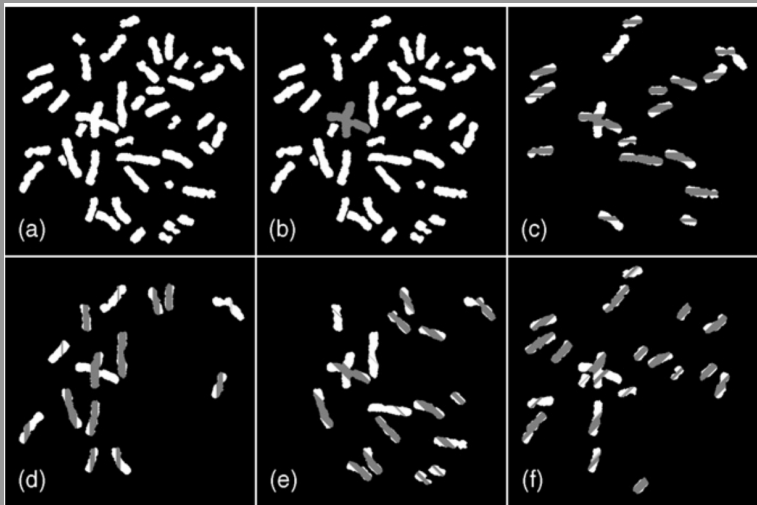
### Filters

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## Plan

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### Image alignment

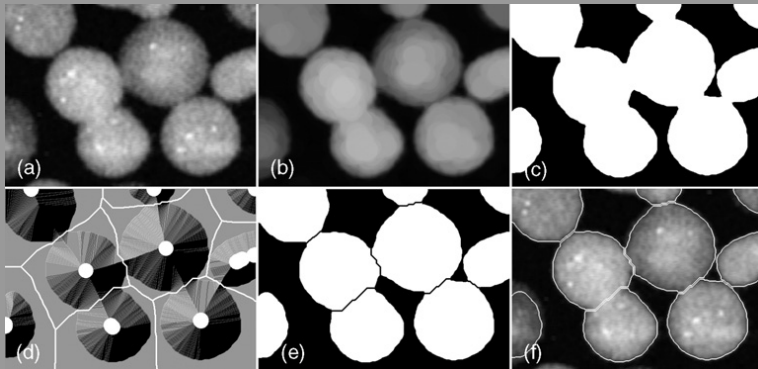
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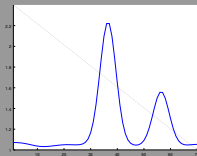
Explained

Convolution

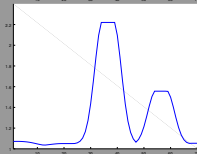
Fancier filters

Summary

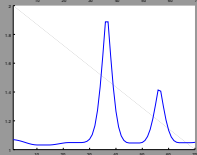
Original



Dilation



Erosion



Gradient  
(dilate - erode)

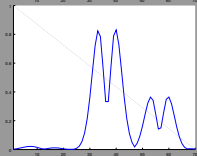
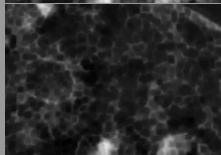
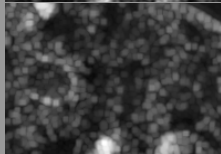
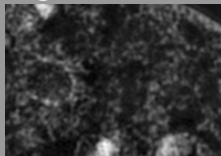


Image gradient



# Moving image

Why doing it?

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Image  
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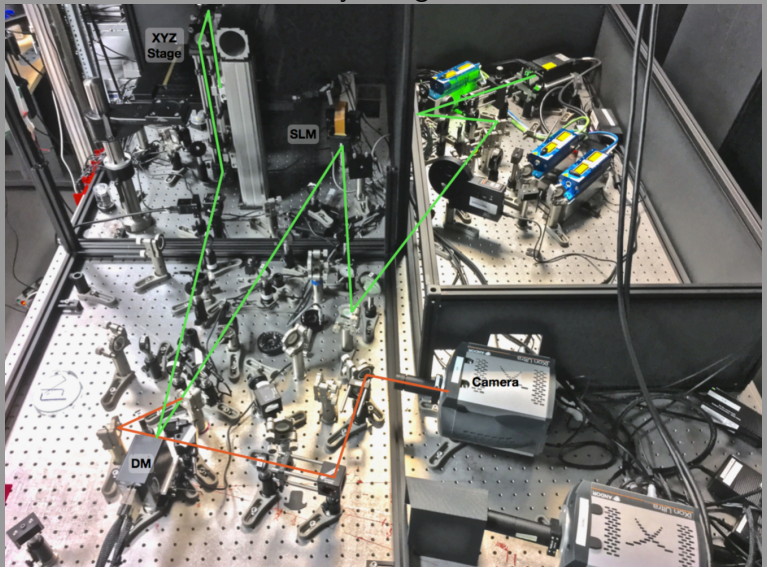
Filters

Explained

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Summary



# geometric transformation

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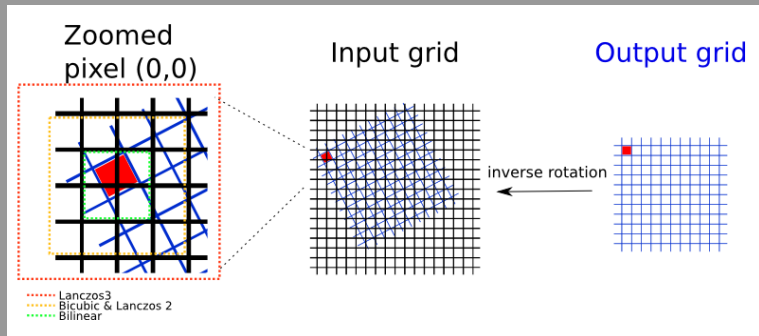
Convolution

Fancier filters

Summary

What happens when you:

- rotate
- align
- translate
- stretch





# Linear interpolation

## Plan

### Basics

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### Segmentation

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### Image alignment

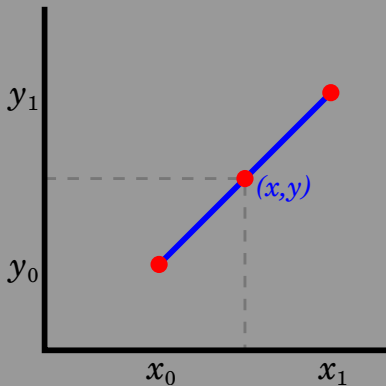
### Filters

Explained

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### Summary



# Bilinear interpolation

## Plan

## Basics

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## Image alignment

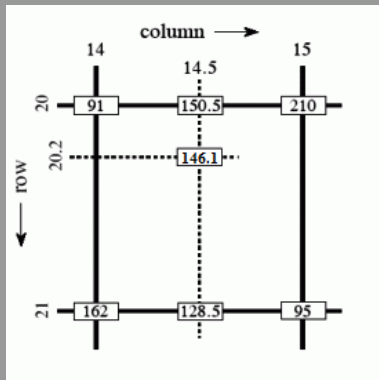
## Filters

Explained

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## Summary



# Background correction

## Plan

### Basics

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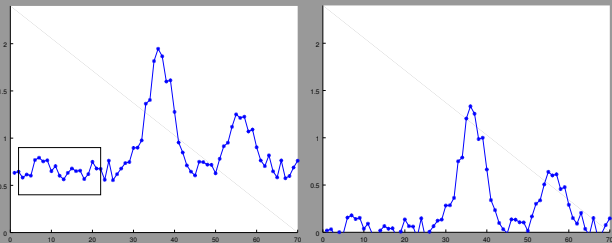
Explained

Convolution

Fancier filters

### Summary

- Subtract mean of a known background region (darks).
- Many cameras (not-microscopes) do this.



# Local means

Plan

Basics

- Images as Arrays
- Numeric types
- Tools
- ImageJ

Segmentation

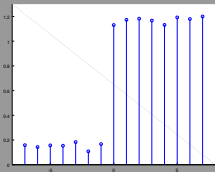
- Logical images
- Threshold
- Logical operations
- Object properties
- Morphology

Image alignment

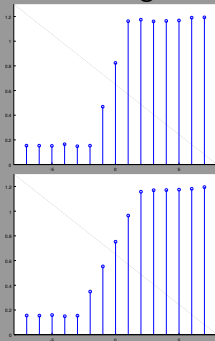
Filters

- Explained
- Convolution
- Fancier filters

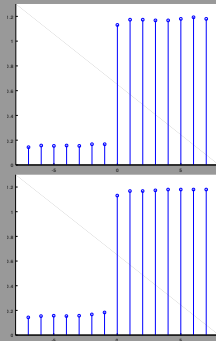
Summary



Average



Median



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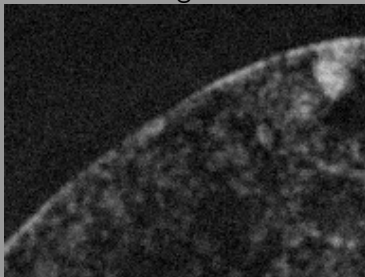
Explained

Convolution

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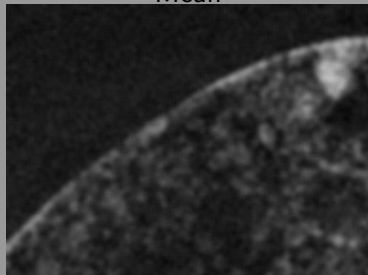
Summary

Original

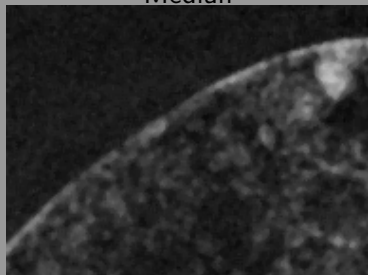


Local means

Mean



Median



# Mean as convolution kernel

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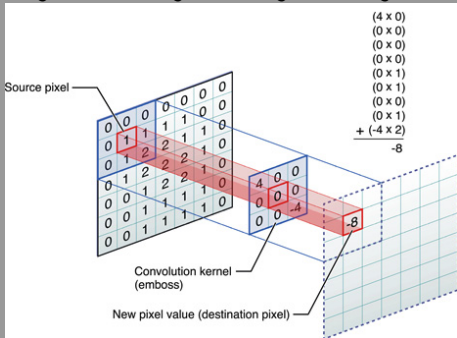
Explained

Convolution

Fancier filters

Summary

$$\frac{4+5+6}{3} = 4 \times \frac{1}{3} + 5 \times \frac{1}{3} + 6 \times \frac{1}{3}$$



$$\begin{bmatrix} 1/9 & 1/9 & 1/9 \\ 1/9 & 1/9 & 1/9 \\ 1/9 & 1/9 & 1/9 \end{bmatrix}$$

3x3 mean kernel

$$\begin{bmatrix} 1/25 & 1/25 & 1/25 & 1/25 & 1/25 \\ 1/25 & 1/25 & 1/25 & 1/25 & 1/25 \\ 1/25 & 1/25 & 1/25 & 1/25 & 1/25 \\ 1/25 & 1/25 & 1/25 & 1/25 & 1/25 \\ 1/25 & 1/25 & 1/25 & 1/25 & 1/25 \end{bmatrix}$$

5x5 mean kernel

# Non-local means patch based denoise

## Plan

## Basics

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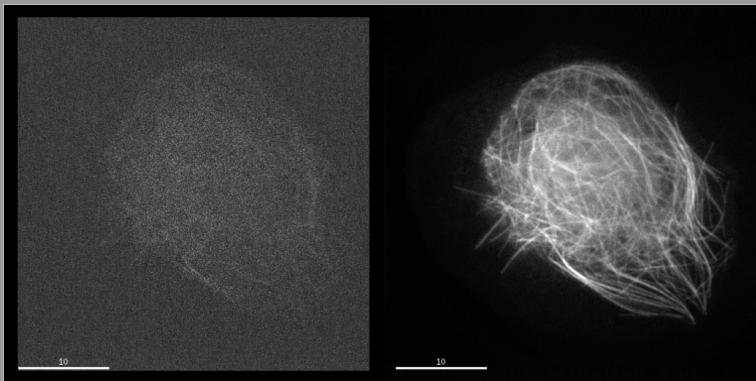
## Filters

Explained

**Convolution**

Fancier filters

## Summary



# Gaussian filter

as weighed mean

## Plan

### Basics

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### Segmentation

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### Summary

$$\begin{bmatrix} 0.011 & 0.014 & 0.017 & 0.018 & 0.017 & 0.014 & 0.011 \\ 0.014 & 0.019 & 0.023 & 0.024 & 0.023 & 0.019 & 0.014 \\ 0.017 & 0.023 & 0.027 & 0.029 & 0.027 & 0.023 & 0.017 \\ 0.018 & 0.024 & 0.029 & 0.030 & 0.029 & 0.024 & 0.018 \\ 0.017 & 0.023 & 0.027 & 0.029 & 0.027 & 0.023 & 0.017 \\ 0.014 & 0.019 & 0.023 & 0.024 & 0.023 & 0.019 & 0.014 \\ 0.011 & 0.014 & 0.017 & 0.018 & 0.017 & 0.014 & 0.011 \end{bmatrix}$$



# Edge detection

## Sobel operator

### Plan

### Basics

- Images as Arrays
- Numeric types
- Tools
- ImageJ

### Segmentation

- Logical images
- Threshold
- Logical operations
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- Morphology

### Image alignment

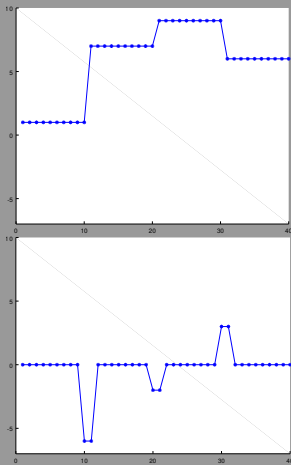
### Filters

- Explained
- Convolution
- Fancier filters

### Summary

1D filter

$$\begin{bmatrix} +1 & 0 & -1 \end{bmatrix}$$



# Edge detection

## Sobel operator

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Convolution

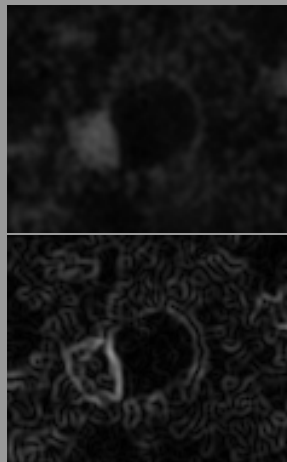
Fancier filters

### Summary

2D filter(s)

$$\begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ -1 & +2 & +1 \end{bmatrix}$$



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Explained

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### Summary

Limitations such as:

- only black and white;
- only 8 bit;
- only 2D images;
- only 3D images;

are limitations of the implementation.

## Plan

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### Summary

- Images are just N dimensional array of numbers
- Mathematical operations can be extended to images
- Thresholding to create masks
- Filters for processing image
- Morphology to identify shapes