Imaging at the molecular level: Measuring molecular motion and interactions

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Imaging at the molecular level: Measuring molecular motion and interactions

- <u>Brief intro to theory of molecular motion</u>
- Fluorescence techniques for measuring molecular motion
- Single particle tracking (SPT)
- Fluorescence Recovery after Photobleaching (FRAP)
- Fluorescence Correlation Spectroscopy (FCS)
- Fluorescence techniques for measuring molecular interactions
- Förster Resonance Energy Transfer (FRET)
- Fluorescence Cross-Correlation Spectroscopy (FCCS)

Many biological samples are dynamic at a wide range of time-scales

Example 1: Cell cycle; 3D re-construction of HeLa cells expressing H2B-GFP imaged on Spinning-disc Confocal at 6 Z-stacks/h



Example 2: Cell cycle; U2OS cells expressing PCNA-Chromobody-RFP imaged on Widefield/TIRF microscope at 24 z-planes/h





Example 3: Mitosis; HeLa cells expressing LifeAct-RFP imaged in TIRF microscope at 24 z-planes/h



Examples 4: Molecular motion of phospholipid analogue (KK114-PE) in substrate supported bilayer (SLB) imaged in TIRF mode at 65 Hz



- ... but time-lapse imaging alone does not reveal <u>quantitative</u> information about movements of cell organelles, proteins, lipids, or DNA
- In particular, time lapse imaging is not sufficient to differentiate between different modes of motion or transient binding of a molecule i.e.
 - 1. Random (Brownian) diffusion
 - 2. Directed active (motor driven) transport
 - 3. Reversible binding and moving by 1, 2, or combination thereof
 - 4. ...

Imaging at the molecular level: Measuring molecular motion and interactions

· Brief intro to theory of molecular motion

Brief intro to theory of molecular motion

ON THE MOVEMENT OF SMALL PARTICLES SUSPENDED IN A STATIONARY LIQUID DEMANDED BY THE MOLECULAR-KINETIC THEORY OF HEAT

N this paper it will be shown that according to the molecular-kinetic theory of heat, bodies of microscopically-visible size suspended in a liquid will perform movements of such magnitude that they can be easily observed in a microscope, on account of the molecular motions of heat. It is possible that the movements to be discussed here are identical with the so-called "Brownian molecular motion"; however, the information available to me regarding the latter is so lacking in precision, that I can form no judgment in the matter (1).

Mean Squared Displacement:

Stokes-Einstein Relation: (3D diffusion in solution)

(Free (Brownian) diffusion in 1D) $\langle (x(t) - x_0)^2 \rangle = \int x^2 N[0, 2Dt] dx = 2Dt$

$$D_{S} = \frac{k_{B}T}{6\pi \,\mu_{S} \,R_{H}}$$

$$D_M = \frac{k_B T}{4\pi \,\mu_M \,h} \ln[\frac{\mu_M \,h}{\mu_S \,R_H} - \gamma]$$

Einstein, A. (1905). Uber die von der molekularkinetischen Theorie der Wärme geforderte Bewegung von in ruhenden Flüssigkeiten suspendierten Teilchen. Annalen der Physik, 17, 549-560.

Einstein, A. (1956). *Investigations on the theory of the Brownian movement* (A. D. Cowper, Trans.). New York, NY: Dover Publications.

Saffman, P. G., & Delbruck, M. (1975). Brownian motion in biological membranes. Proc Natl Acad Sci USA, 72(8), 3111-3113.

Diffusion in membranes and solution



Saffman-Delbruck:

$$D_M = \frac{k_B T}{4\pi \mu_M h} \ln[\frac{\mu_M h}{\mu_S R_H} - \gamma]$$

$$\mu_S = 1.002 \text{ cP}$$

T = 293 K $\mu_M / \mu_S = 100 \text{ (solid line)}$ $\mu_M / \mu_S = 80 \text{ (short dashed line)}$ $\mu_M / \mu_S = 60 \text{ (long dashed line)}.$

Stokes-Einstein:

$$D_{S} = \frac{k_{B}T}{6\pi \,\mu_{S} \,R_{H}}$$

μ_s = 1.002 cP *T* = 293 K. Fluorescence techniques for measuring molecular motion

- 1) Single particle tracking (SPT)
- 2) Fluorescence Recovery after Photobleaching (FRAP)
- 3) Fluorescence Correlation Spectroscopy (FCS)

1) Single particle tracking (SPT)

anti-CD73 Fab'-biotin + sAv-605 Qdot



189 Hz (5.3 ms integration) with 160X magnification and Andor EMCCD

Playback 100 Hz, 2000 frames Scale bar = 1µm

Single Particle Tracking

• Time lapse imaging of spatially resolved single particles, molecules, or subcellular structures

• Technique results in time trajectories of sub-pixel positions of single objects

- Such trajectories contain information about:
 - diffusion coefficients
 - velocities
 - step sizes
 - spatial and temporal confinement

• Dynamics are analyzed with respect to that predicted by Brownian (random) motion in a 2 D (or 3D) fluid

• For 2D, the mean square displacement (MSD) is

 $\left\langle \left(r(t) - r_0 \right)^2 \right\rangle = 4Dt$

where D is the diffusion coefficient



Brownian motion $\langle r^2 \rangle = 4Dt$ Anomalous diffusion $\langle r^2 \rangle = 4Dt^{\alpha}$ $\alpha < 1$ Diffusion with flow $\langle r^2 \rangle = 4Dt + (Vt)^2$ Confined diffusion $\langle r^2 \rangle \approx \langle r_c^2 \rangle [1 - A_1 \exp(-4A_2Dt / \langle r_c^2 \rangle)]$

Saxton and Jacobson (1997) Annu. Rev. Biophys. Biomol. Struct. 26: 373-99

Data Analysis

• Obtain sub-pixel resolution by curve fitting to determine centroids of single molecules

•Approximate Airy pattern with a 2D spatial Gaussian and fit each image

$$\boldsymbol{A} + \frac{\boldsymbol{B}}{2\pi \boldsymbol{w}^2} \boldsymbol{E} \boldsymbol{x} \boldsymbol{p} [-\frac{1}{2\pi \boldsymbol{w}^2} ((\boldsymbol{x} - \boldsymbol{x}_{\boldsymbol{o}})^2 + (\boldsymbol{y} - \boldsymbol{y}_{\boldsymbol{o}})^2)]$$

where w = width of the PSF of the microscope (~220 nm)





Mode of Motion & Diffusion Coefficient



Probe Considerationsfor SPT

- Very bright and stable
- Small
- Monovalent (i.e. one probe per molecule of interest)
- Low non-specific binding

	Gold particles	Cy3	Quantum dots
Means of detection	Scattering	Fluorescence	Fluorescence
Size (diameter)	40 nm	~1-2 nm	~10-20 nm
Advantages	Photostable	Small Monovalent	Photobleaching resistant
Disadvantages	Immobilization Large Multivalent	Photobleaching (~5 s)	Non-specific binding Blinking

Examples 4: Molecular motion of phospholipid analogue (KK114-PE) in substrate supported bilayer (SLB) imaged in TIRF mode at 65 Hz



Cell Focal Adhesions in Widefield and TIR Fluorescence



http://www.microscopyu.com/articles/fluorescence/tirf/tirfintro.html





2) Fluorescence Recovery after Photobleaching (FRAP)

 Select photobleaching of region of interest (ROI) with very high laser intensity
Monitor the progress of fluorescence recovery in the bleached area with high temporal resolution

- Changes in intensity in the bleached region represent the sum of all movements of fluorescent molecules, whether passive (e.g., diffusion) or active (e.g., transport).
- The half-recovery time is a measure of the average speed of protein movement.



Bleached spot size ~ 1 μm

(www.zeiss.com)



http://www.embl-heidelberg.de/eamnet/frap/html/how_frap_works.html

Can also do FRAP with most confocal microscopes



In this geometry, D is typically calculated numerically by comparing fluorescence recovery curves with simulated curves
(See i.e. http://www.embl.de/eamnet/html/frap_analysis.html)



Dynamics of putative raft-associated proteins at the cell surface

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The Journal of Cell Biology, Volume 165, Number 5, June 7, 2004 735-746



Large-scale lateral diffusion measurements by confocal microscopy. (A) Selected images from a confocal FRAP experiment at 37 °C of GFP-KRas expressed in COS-7 cells. Bleach box, 4 μ m wide. Bar, 10 μ m. (B) Kinetics of recovery for 1.4- (circles) versus 4- μ m-wide (squares) bleach box. Calculated D and t1/2 values are indicated. Data shown are for GFP-KRas expressed in COS-7 cells at 37 °C. (C) Kinetics of recovery for YFP-GT46 (triangles), YFP-GL-GPI (squares), and GFP-KRas (circles) in COS-7 cells at 37 °C using a 4- μ m-wide bleach box. Each curve shows the mean ± SD from seven to nine cells from a single experiment. The calculated Ds were as follows: GFP-KRas, 1.01 ± 0.11 μ m2/s; YFP-GL-GPI, 0.47 ± 0.07 μ m2/s; YFP-GT46, 0.23 ± 0.02 μ m2/s.

J. Ellenberg, E. D. Siggia, J. E. Moreira, C. L. Smith, J. F. Presley, H. J. Worman, and J. Lippincott-Schwartz (1997) Nuclear Membrane Dynamics and Reassembly in Living Cells: Targeting of an Inner Nuclear Membrane Protein in Interphase and Mitosis. J. Cell Biol. 138: 1193-1206





Distribution and mobilities of LBR-GFP in interphase and mitotic membranes. (A) Confocal section close to the lower cell surface showing steady-state expression of LBR-GFP in an interphase cell. (*Inset*) Boxed region at higher magnification showing LBR- GFP distribution within the ER network. (*B*) Qualitative FRAP experiments in ER and NE membranes in interphase cells expressing LBR-GFP. (*Left*) Photobleach recovery in ER membranes. (*Right*) Photobleach recovery in NE membranes. Note the complete recovery of fluorescence in the ER and the lack of recovery in the NE. (*C*) Thin confocal section through the mitotic apparatus showing the steady-state expression pattern of LBR-GFP in metaphase cells. (*Insets*) Boxed regions at higher magnification showing the tubular membrane network within which LBR-GFP redistributed. Note its resemblance to the interphase ER shown in *A*. (*D*) Qualitative FRAP experiments in mitotic membranes of cells expressing LBR-GFP. (*Left*) Photobleach recovery in telophase membranes. (*Right*) Photobleach recovery in telophase membranes. DNA damage; U2OS cells expressing PCNA-GFP or wtSNM1A-GFP imaged on Confocal microscope at 240 z-planes/h



Characterization of role of *SNM1A*, a 5'–3' exonuclease, in DNA damage response (Lonnie Swift, Ghadir Almuhaini, Christoffer Lagerholm, Peter McHugh)

3) FCS – Fluorescence Correlation Spectroscopy

- FCS is used to get time-resolved information about an ensemble with single molecule sensitivity in a small confocal volume
- Widely used technique to obtain quantitative information such as
 - diffusion coefficients
 - hydrodynamic radii
 - average concentrations
 - kinetic chemical reaction rates
 - singlet-triplet dynamics



 $D=rac{k_BT}{6\pi\,\eta\,r}~~$ Diffusion in solution (3D) – Stokes-Einstein relation

FCS – Autocorrelation of Fluorescence Fluctuations



What causes fluctuations in intensity? a) Poison noise, b) diffusion of molecules



Bursts of photons are seen as single fluorophores diffuse in and out of the laser beam

FCS – Autocorrelation of Fluorescence Fluctuations



Fluorescence Correlation Spectroscopy

Wrapping it up: How many



1. Concentration dynamic range: pM - µM

Fluorescence Correlation Spectroscopy

Wrapping it up: How many, how fast



Fluorescence Correlation Spectroscopy

Wrapping it up: How many, how fast, what mechanism



3. TYPE OF MOVEMENT



- 1. Concentration dynamic range: $pM \mu M$
- 2. Time scale range: µs s
- 3. Type of dynamics: rafts, flow, free, ...

Example: Translational diffusion of lipids in plasma membrane of live cells



Summary - Fluorescence techniques for measuring molecular motion

• All methods are dependent on the availability of theoretical models such that experimental data is compared to theoretical models by curve fitting

• SPT can yield information about "heterogeneties" of single molecule behavior that is not apparent in ensemble average techniques and at a spatial resolution of ~ tens of nanometers

...but only for single molecules that are separated by a distance greater than r_{Airy}

• FRAP, FLIP, FLAP, FCS, and RICS are ensemble average techniques that are often easy to implement on a standard confocal microscope

• FCS is best choice for very fast dynamics including 3D diffusion in solution of small molecules

•Techniques can also be used to investigate binding constants and equilibria (with suitable models)

Fluorescence techniques for measuring molecular interactions

- 1) Förster Resonance Energy Transfer (FRET)
- · 2) Fluorescence Cross-Correlation Spectroscopy (FCCS)

Why can't we image molecular interactions directly?

Microscope Resolution

• The diffraction of light causing the Airy disk is also the limiting factor of the resolution of a microscope

•The resolution of a microscope is defined as the minimum distance two objects have to be separated by to be resolved as two separate objects



Airy patterns of two point sources

• For 100X magnification, 1.4 NA oil immersion objective and illumination with green light (500 nm = $0.5 \ \mu m$)

Resolution =
$$\frac{(0.61) (0.5 \,\mu\text{m})}{1.4} \approx 220 \,\text{nm}$$

1) FRET – Förster Resonance Energy Transfer

- energy is transferred non-radiatively (via long-range dipole-dipole coupling)
- relies on the close physical interaction of the two fluorophores (0.5 – 10nm)
- used to determine molecular interactions beyond the resolution limits



- distance between two molecules
- spectral overlap
- the quantum yield of the donor
- the relative orientation of the transition dipoles







NatProt, 8, 265-281, 2013

FRET Pairs

Donor	Acceptor	Donor Excitation λ _{max} (nm)	Acceptor Emission λ _{max} (nm)	Donor QY (–)	Acceptor ε (M ⁻¹ cm ⁻¹)	Förster Distance (nm)	Cý5 Fluorescein FITC	Cy5.5 Tetramethylrhodamine TRITC	649 487 ¹ 494	694 574 572	> 0.28 0.93 ² 0.92	250,000 ~ 87,000 100.000	>8.0 4.9–5.5 5.4
Fluoreso	ent protein FRET pairs						Phycoerythrin	APC ³	(546), 565	660	0.98	700.000	4.0-11.0
BFP	DsRFP	380	586	0.18	72,500	3.1–3.3	Europium	APC	340	660		700,000	9.0
EBFP2	mEGFP	383	507	0.56	57,500	4.8	Tryptophan	Dansyl	280	525	0.01-0.354	4050	2.1
CFP	GFP	433	509	0.40	21,000	4.7-4.9	Dansyl	FITC	335	519	< 0.035 ⁵	77,000	3.3-4.1
CFP	YFP	433	526	0.40	77,000	~ 5.0	Dansyl	Octadecylrhodamine	335	625	< 0.035	106,000	4.3
Cerulean	YFP	440	526	0.62	77,000	-	Europium	Cy5	340	670		250,000	7.0
ECFP	EYFP	440	527	0.40	83,400	4.9	Atto 488	Atto 647N	501	670	0.8	150,000	5.1
Cerulean	Venus	440	528	0.62	92,200	5.4	Atto 488	Atto 590	501	621	0.8	120,000	6.0
MiCy	mKO	472	559	0.90	51,600	5.3	Atto 550	Atto 647N	554	670	0.8	150,000	6.5
GFP	YFP	475	526	0.77	77,000	5.5-5.7	Atto 550	Atto 655	554	684	0.8	125,000	6.4
GFP	mRFP	475	579	0.77	50,000	~ 4.7	Atto 590	Atto 655	594	684	0.8	125,000	7.3
CyPet	YPet	477	530	0.51	104,000	5.1	Alexa 405	Alexa 430	401	541		16,000	
TFP1	mVenus	492	528	0.85	92,200	5.1	Alexa 488	Alexa 514	495	542	0.92	80,000	
EGFP	mCherry	507	510	0.60	72,000	5.1	Alexa 488	Alexa 532	495	554	0.92	81,000	
Venus	mCherry	528	610	0.57	72,000	5.7	Alexa 488	Alexa 546	495	573	0.92	104,000	6.4
Venus	tdTomato	528	581	0.57	138,000	5.9	Alexa 488	Alexa 610	495	628	0.92	138,000	
Venus	mPlum	528	649	0.57	41,000	5.2	Alexa 647	Alexa 680	650	702	0.33	184,000	
Fluoresce	nt protein-dye FRET pairs						Alexa 647	Alexa 700	650	723	0.33	192,000	
EGFP	Alexa Fluor 555	484	568	0.6	155,000	6.3	Alexa 647	Alexa 750	650	780	0.33	240,000	
EGFP	Alexa Fluor 546	484	573	0.6	112,000	5.7	Non-fluoresc	ent acceptor pairs					
EGFP	Alexa Fluor 594	484	618	0.6	92,000	5.3	Rhodamine 6G	Malachite Green	526	NE	0.95	76.000	61
EGFP	Alexa Fluor 568	484	603	0.6	88,000	5.4	innoddininne o'd	(Abs 628 nm)	520	, NI	0.95	70,000	0.1
Dye and dye	-biofluorochrome FRET pairs						Alexa 488	QSY 35 (Abs 475 nm)	495	NF	0.92	23,000	4.4
Cy2	Суз	489	570	> 0.12	150,000	5.0-6.0	Alexa 488	Dabcyl (Abs 453 nm)	495	NF	0.92	32,000	4.9
Cv3	Cv5	550	670	> 0.15	250.000	>5.0	Alexa 647	QSY 21 (Abs 661 nm)	650	NF	0.33	90,000	6.9

FRET – traditionally used as Molecular Ruler



PNAS,102,2754-2759, 2005

Fundamental cellular FRET-Approaches

- FRET-biosensors: fusion proteins or other appropriate pairs linked by a sensory domain
- monitoring of donor/ acceptor channels and detection of changes in the FRET signal as a result of biological activity



A variation of FRET: FRET-FLIM

FLIM – Fluorescence Lifetime Imaging

- ...is an imaging technique for producing an image based on the differences in the exponential decay rate of fluorophores.
- ...is independent of probe concentration
- the lifetime of the fluorophore signal, not the intensity, is used to create the image in FLIM.





FRET-FLIM

- measurement of lifetime dynamics pixelby-pixel
- mapping of spatial distributions to measure biomolecule concentrations, interactions between biomolecules, and conformational changes with a much higher accuracy than conventional FRET methods



FLIM with TCSPC in practice



Figure 1: Measurement of start-stop times in time-resolved fluorescence measurement with TCSPC.



Figure 2: Histogram of start-stop times in time-resolved fluorescence measurement with TCSPC.

FLIM Measurements

- essential components of a FLIM set-up:
 - pulsed laser source
 - detector (APD or PMT)
 - TCSPC unit to measure the time between excitation and fluorescence emission (timedomain FLIM)
- the delay times are sorted into a histogram



2) FCCS – Dual-Colour Extension of FCS

- interaction of two differently labeled molecular species with higher precision than single-color FCS
- high specificity: FCCS curve is only formed if the differently labeled molecules are bound and moving together (co-diffuse).
- From amplitude and decay time: binding constants, mobility of the bound complex, concentrations of all of the species



Toxicity of Choleratoxin unfolds as the active A-units separated from B₅ in Golgi



Summary - Fluorescence techniques for measuring molecular interactions

•FRET is a direct method for measuring molecular interactions beyond the resolution limits (~0.5-10 nm)

•FRET-FLIM is particularly powerful method because it minimizes spectral crosstalk problems and concentration dependent artefacts

•FCCS is extension of FCS that enables the direct measurement of molecular interactions provided that the interacting molecules are mobile

Jablonski-Diagram

- molecules have electronic, vibrational and rotational energy levels
- absorption = electron moves to a higher excited state
- vibrational relaxation (Stokes-Shift), internal conversion, intersystem crossing
- return to the ground state: fluorescence, phosphorescence



3) FLIP – Fluorescence Loss in Photobleaching

- a small region is repeatedly bleached and the loss of fluorescence in another region is measured.
- useful to show connectivity of compartments or for measuring turnover of molecules between different compartments



J. Ellenberg, E. D. Siggia, J. E. Moreira, C. L. Smith, J. F. Presley, H. J. Worman, and J. Lippincott-Schwartz (1997) Nuclear Membrane Dynamics and Reassembly in Living Cells: Targeting of an Inner Nuclear Membrane Protein in Interphase and Mitosis. J. Cell Biol. 138: 1193-1206



Fig. 6. FLIP to probe the continuity of interphase and mitotic membranes containing LBR-GFP. FLIP experiments were performed on interphase membranes (*left*) and metaphase membranes (*right*). Note the complete loss of fluorescence from both interphase ER membranes and mitotic membranes over a similar time course, but not from NE membranes in interphase. ER fluorescence that remained in interphase is from an adjacent cell whose membranes were not connected to those within the photobleached box. Bars, 10 μ m.

4) FLAP – Fluorescence Localization after Photobleaching

- In FLAP a protein is tagged with two fluorescent labels: one is photobleached and the other acts as a reference
- The use of a reference fluorochrome allows the tracking of the distribution of the labelled molecules by simple image differencing (I) and thus enables measurement of fast relocation dynamics.



Dunn, G. A., Dobbie, I. M., Monypenny, J., Holt, M. R., & Zicha, D. (2002). Fluorescence localization after photobleaching (FLAP): a new method for studying protein dynamics in living cells. *J Microsc, 205* (Pt 1), 109-112.