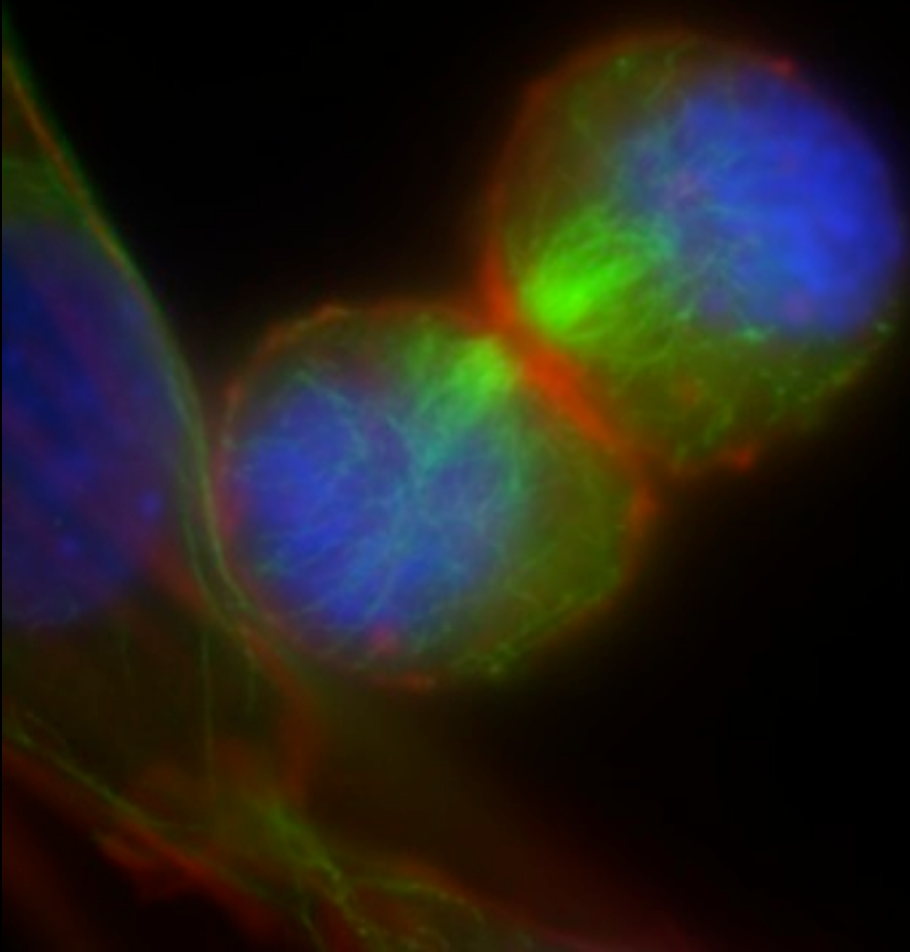


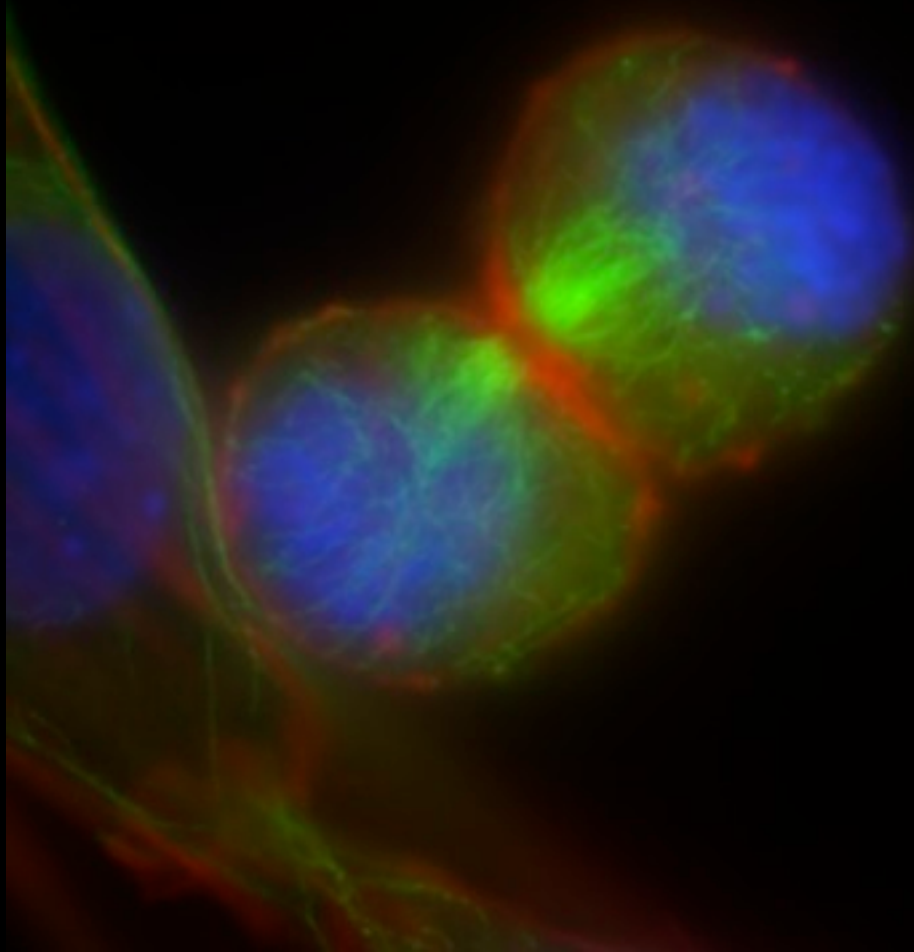
Lecture 13: Super-resolution microscopy



lothar.schermelleh@bioch.ox.ac.uk

Typical widefield image...

Lecture 13: Super-resolution microscopy

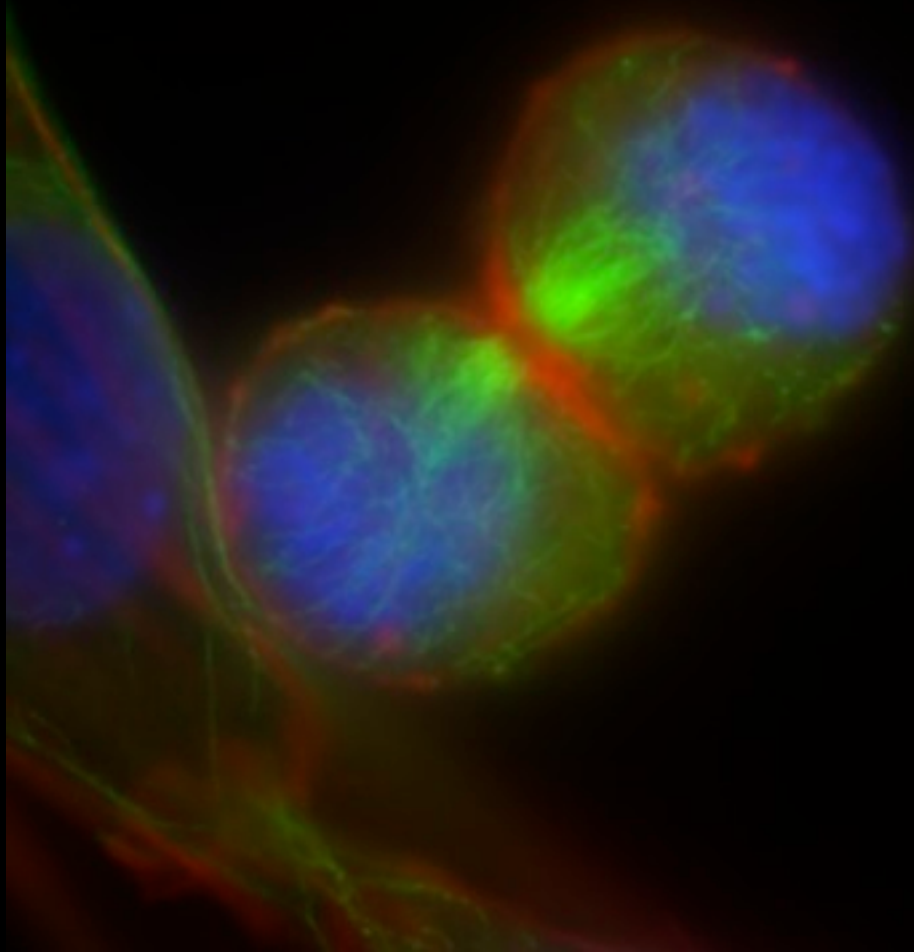


Optical resolution is
diffraction limited!

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Typical widefield image...

Lecture 13: Super-resolution microscopy



Optical resolution is
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Magnification alone does
not give more details!

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Lecture 13: Super-resolution microscopy

Optical resolution is
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Typical widefield image...

... a little reminder:

“What determines the resolution of an optical microscope ?”



63x/1.25



100x/1.25



63x/1.4

„... what objective would you take...“

... a little reminder:

“What determines the resolution of an optical microscope ?”



63x/1.25

€ 5.557,56



100x/1.25

€ 693,68



63x/1.4

€ 6.370,72

„... what objective would you take...“

„... a bit more difficult...?“



25x/1.05



40x/1.0



40x/1.1

„... what objective would you take...“

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40x/1.1

What's the difference in brightness ?

„... what objective would you take...?“

„... a bit more difficult...?“



25x/1.05

€ 15.000,00



40x/1.0

€ 3.786



40x/1.1

€ 11.110,48

What's the difference in brightness ?

„... what objective would you take...“

Numerical aperture determines ...

Brightness	$B = NA^4 / Mag^2$	(epifluorescence)
Lateral Resolution	$d_{x,y} = 0.61 \lambda / NA$	(200-300 nm)
Axial Resolution	$d_z = 2 \lambda / NA^2$	(500-700 nm)

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Only applies under optimal conditions! BUT ...

spherical aberrations
chromatic aberrations
straylight
out-of-focus blur
noise
sample

...

Effective resolution is worse!
(max. 250 nm lateral and $\leq 1 \mu\text{m}$ axial)

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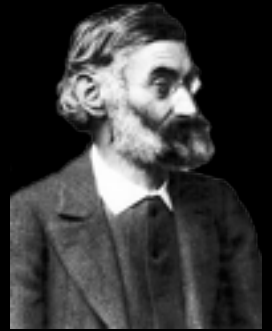
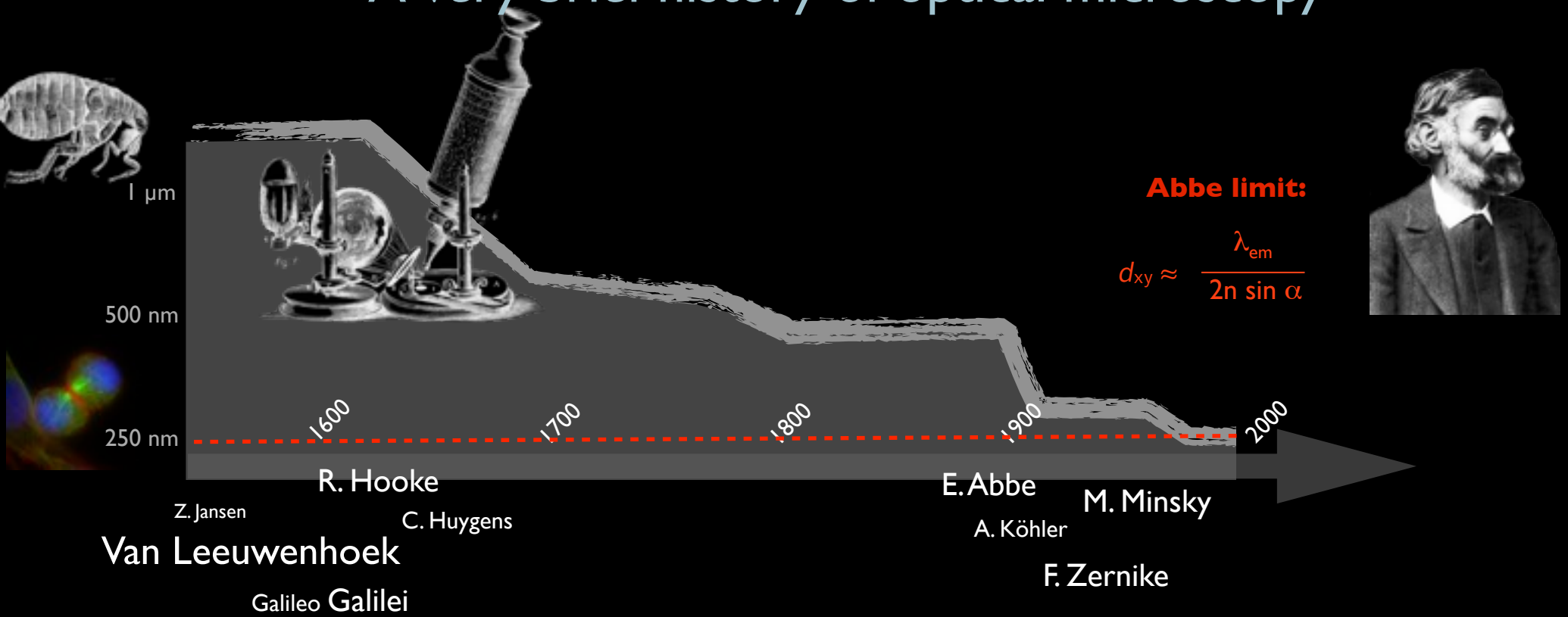
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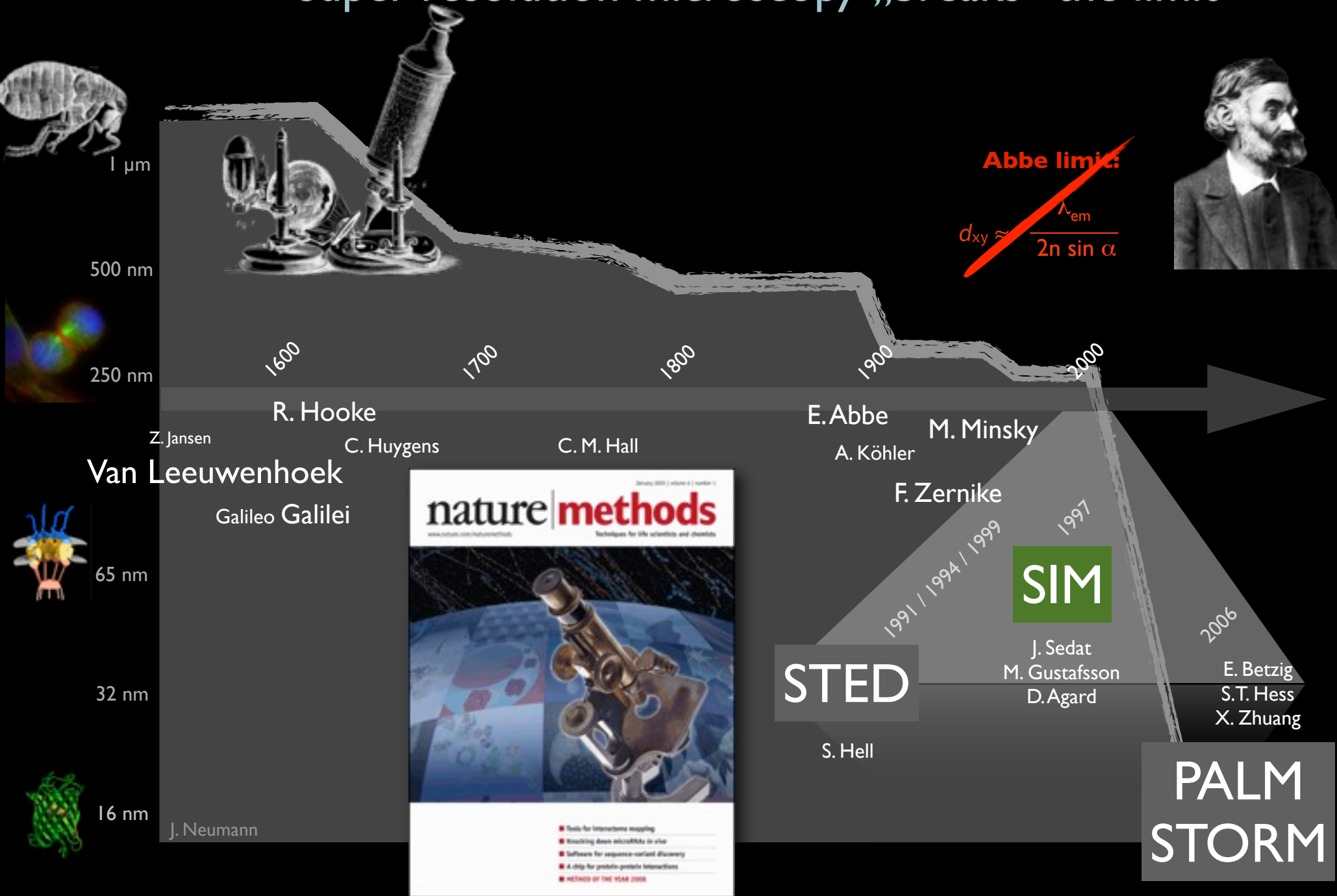
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...improved to some extent by Confocal LSM or Deconvolution

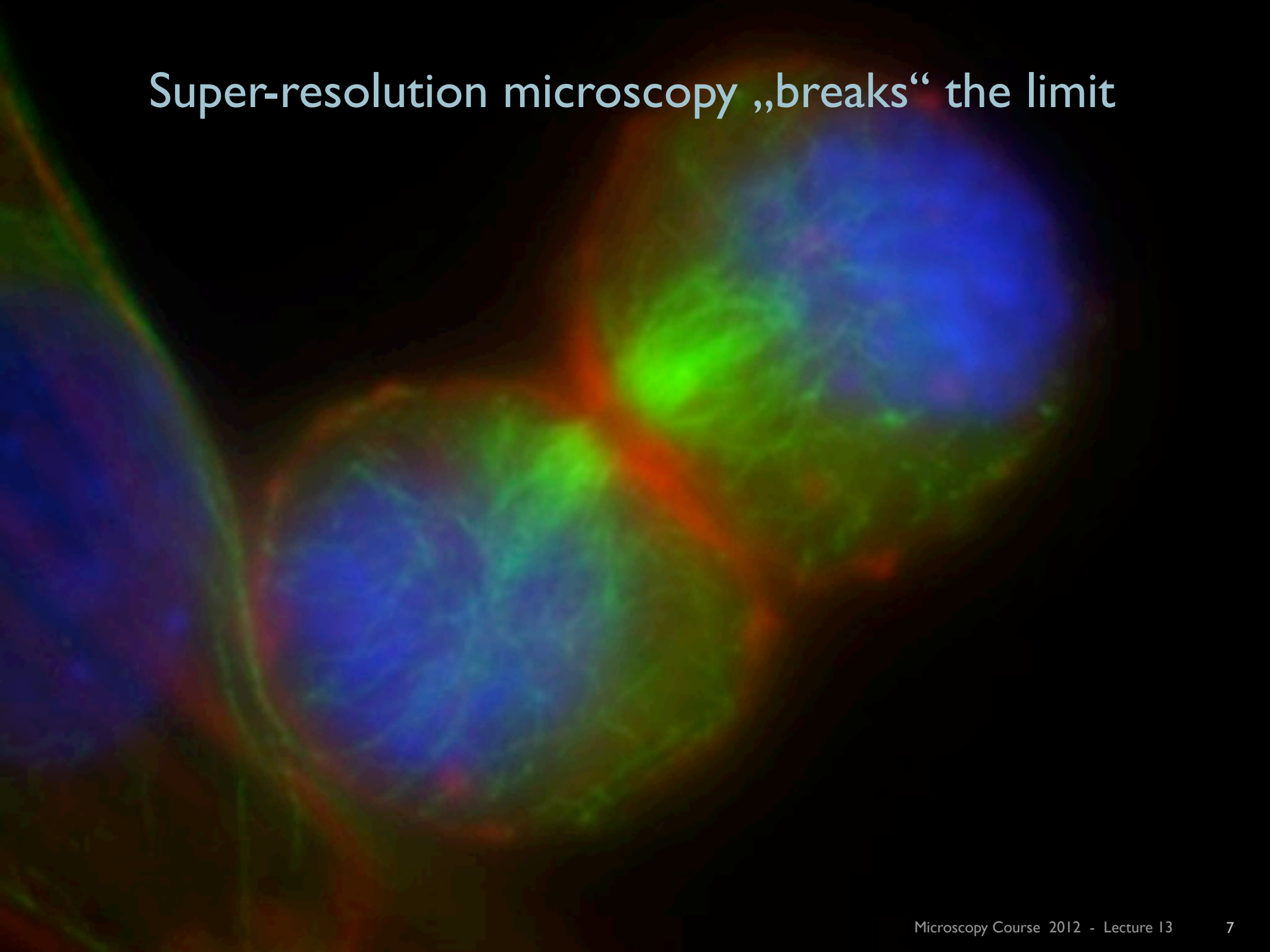
A very brief history of optical microscopy



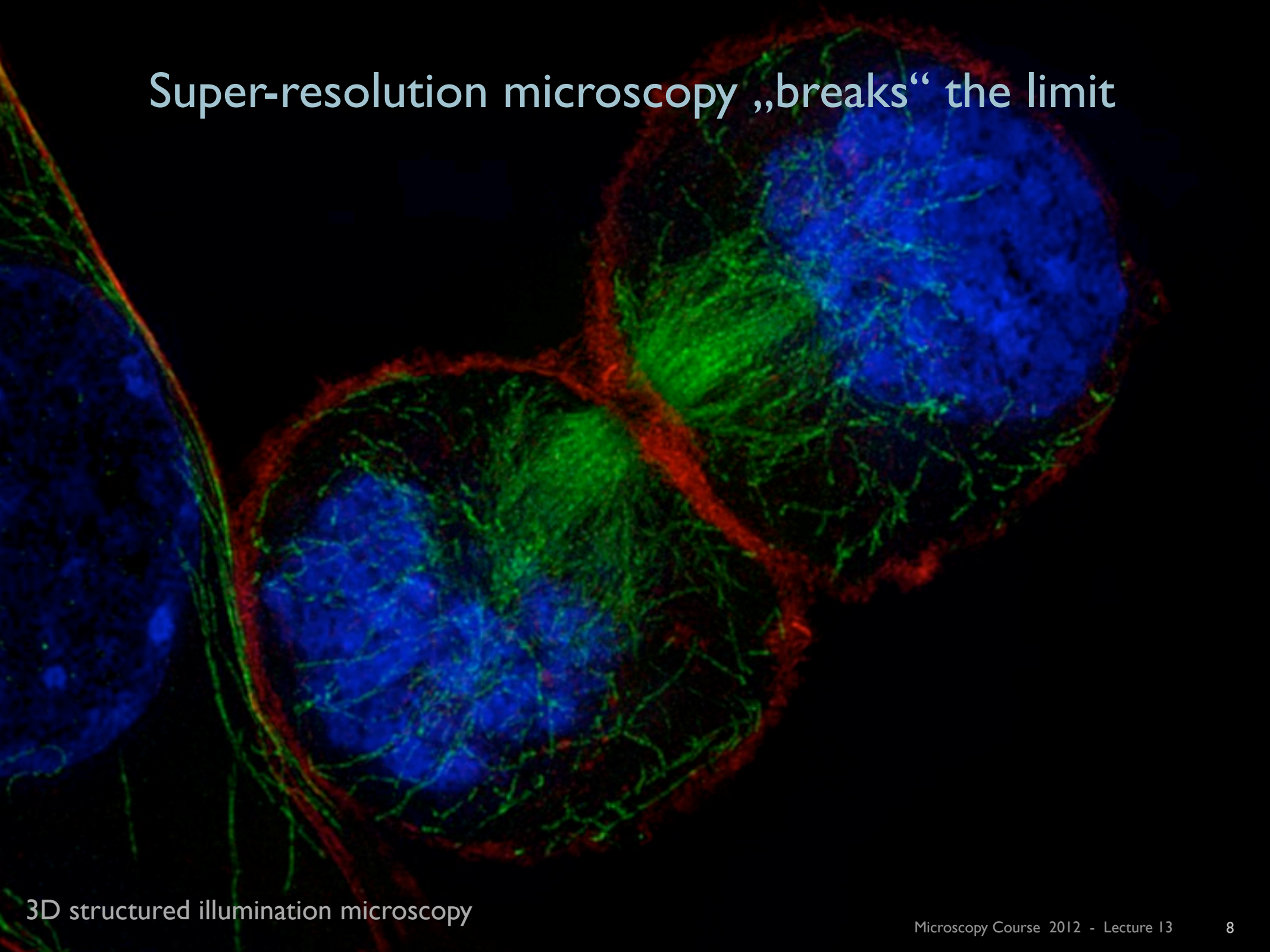
Super-resolution microscopy „breaks“ the limit



Super-resolution microscopy „breaks“ the limit



Super-resolution microscopy „breaks“ the limit



Super-resolution microscopy „breaks“ the limit

General overview of SR methods
(4Pi, STED, SIM, Pointilism)

Super-resolution microscopy „breaks“ the limit

General overview of SR methods
(4Pi, STED, SIM, Pointilism)

How Structured Illumination
improves not only resolution ...
& how it is realized in
OMX

Optical super-resolution microscopy methods

Principle	Near-field		Far-field					
	Small aperture scanning (no lens)	Evanescent wave illumination	Wide-field + deconvolution	Confocal laser scanning	Moiré effect with structured illumination	PSF shaping with saturated emission depletion	Photoswitching and localization of single molecules (pointillism)	
Acronym	SNOM/NSOM	TIRFM		CLSM	SIM (HELM, FEM) 3D-SIM	SSIM (SPEM)	STED/CW-STED	PALM/FPALM/STORM/dSTORM/PALMIRA
Illumination-emission dependence	Linear	Linear	Linear	Linear	Linear	Non-linear	Non-linear	Linear
Detector	Scanning PMT/APD	Wide-field CCD/CMOS	Wide-field CCD/CMOS	Scanning PMT/APD	Wide-field CCD/CMOS	Wide-field CCD/CMOS	Scanning PMT/APD	Wide-field CCD/CMOS
XY-resolution	20–120 nm	200–300 nm	180–250 nm	180–250 nm	100–130 nm	50 nm	20–100 nm	20–50 nm
Z-resolution	10 nm (near-field range)	100 nm (near-field range)	500–700 nm	500–700 nm	250–350 nm	N.D.	560 nm [CW-STED] to 700 nm [100 nm with z-phase mask]	100 nm (TIRF) 20–30 nm (3D-STORM, TIRF) 75 nm (BPFPALM, in plane)
Serial z-sectioning	No	No	Yes	Yes	Yes	Yes	Yes	Yes
Z stack range	N.A.	N.A.	100 µm	100 µm	10–20 µm	N.A.	>20 µm	100 nm – few µm (BPFPALM)
Dyes	Any	Any	Any	Any	Most conventional dyes (photostable)	Dyes require special characteristics	Dyes require special characteristics (CW-STED works with many conventional dyes)	Dyes require special characteristics
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Energy load/intensity	Low	Low	Low	Medium	Medium	High	Medium-high	Medium-high
Live-cell imaging	Yes	Yes	Yes	Yes	Restricted (2D-TIRF)	No	Restricted	Restricted
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Dual lens implementation			1stM	4Pi	1stS		4 Pi-STED/iso-STED	#PALM
Z-resolution			70 nm	80 nm	100 nm		20–100 nm	10 nm (depth ~200 nm)

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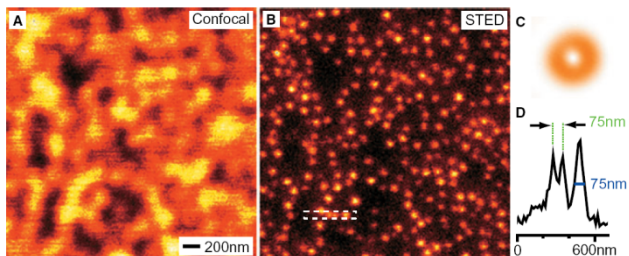
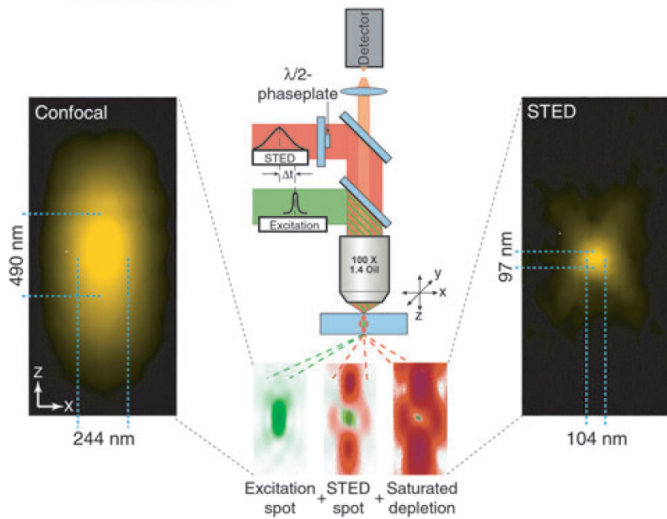
„Gold standard“

Super-resolution light microscopy: Imaging beyond Abbe's diffraction limit

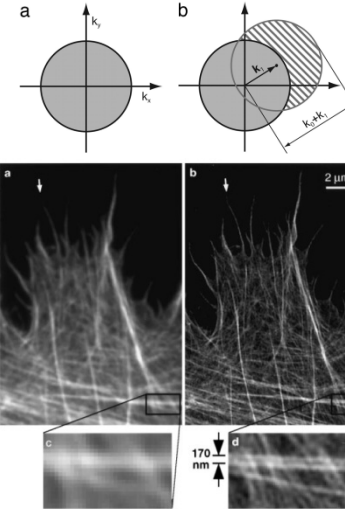
$$\Delta x, \Delta y = \frac{\lambda}{2n \sin \alpha}$$

Stimulated emission depletion (STED)

C STED microscope

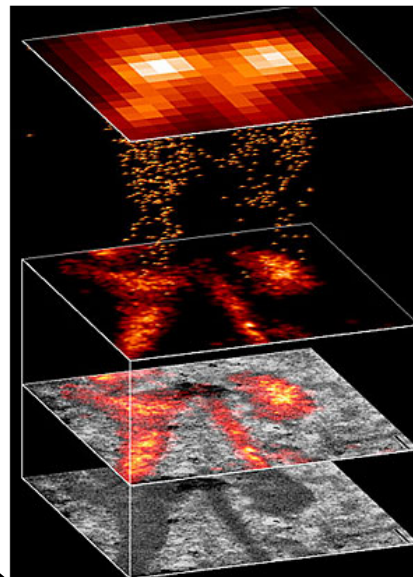


Structured illumination

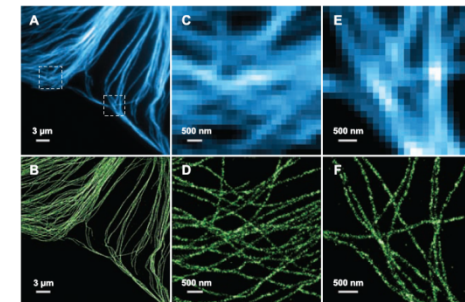
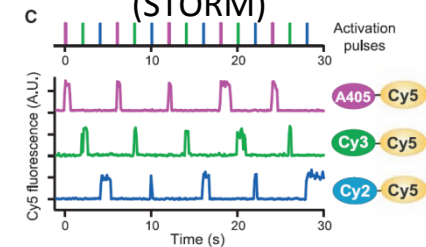


Localization microscopy (Pointilism)

Photoactivation localization microscopy (PALM)



Stochastic optical reconstruction microscopy (STORM)



Milestones in super-resolution microscopy

1873: Resolution limit, E Abbe

⋮

1992: 4Pi Microscopy, SW Hell, E Stelzer

(1994: STED Microscopy, SW Hell)

1995: I5M Microscopy, M Gustaffson, J Sedat

1998: Diffraction grating, R Heintzmann, C Cremer

2000: STED Microscopy, SW Hell

2000: Structured illumination, M Gustaffson

2006: PALM, E. Betzig, H. Hess

2006: FPALM, S. Hess

2006: STORM, X. Zhuang

2008: 3D SIM, M Gustaffson, J Sedat

2008: 3D STORM, X. Zhuang

2008: Biplane FPALM, S Hess, J Bewersdorf

2008: Nature Methods: Method of the year

2009: 21st Nature Milestone for light microscopy

⋮

axial resolution

lateral resolution

3D capability

2003: Leica 4Pi (2P)

2006: Leica TCS STED

2009: DeltaVision OMX 3D-SIM

2009: Zeiss Elyra PALM/SIM

2009: Leica CW STED

2010: Nikon N-SIM/N-STORM

2012: OMX Blaze

4Pi Microscopy



(S. Hell)

- Phase and wave front corrected interferometer to generate counter propagating coherent wavefronts
- Illumination and imaging from both sides,
- Confocal/multiphoton system for image acquisition

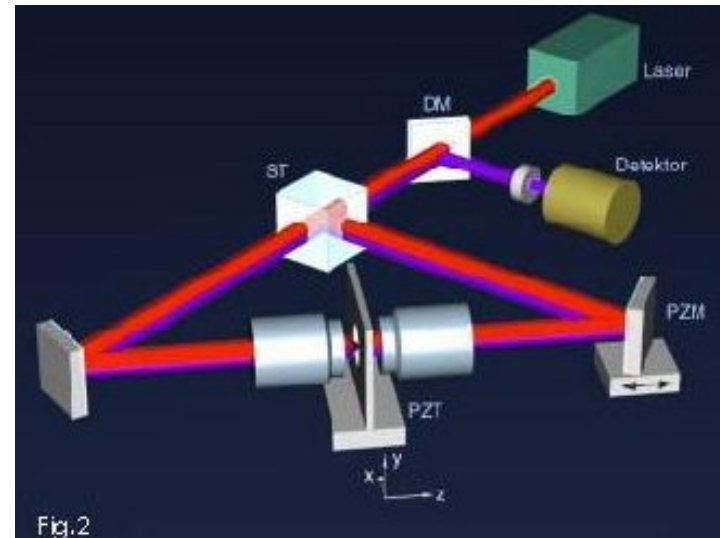


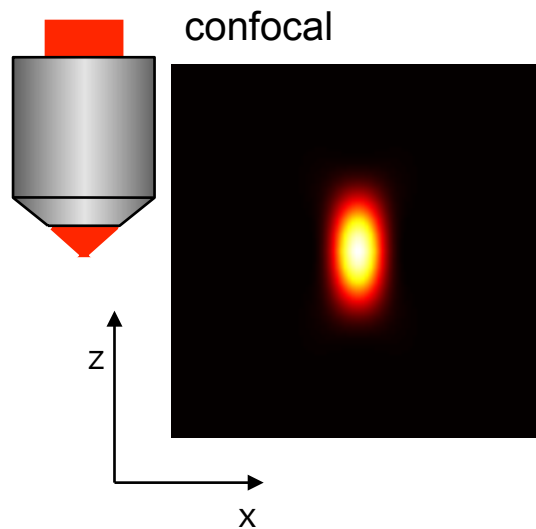
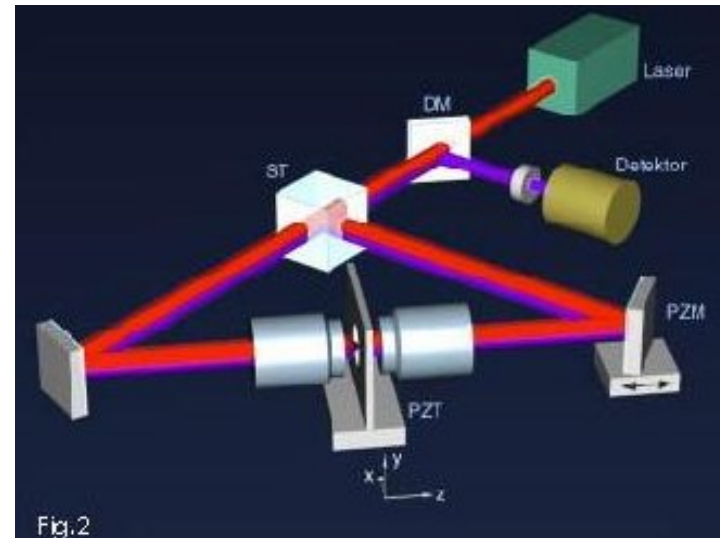
Fig.2

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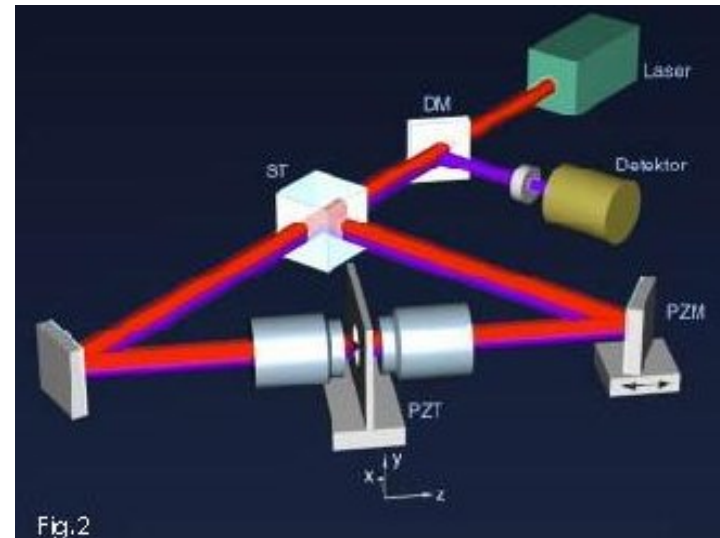
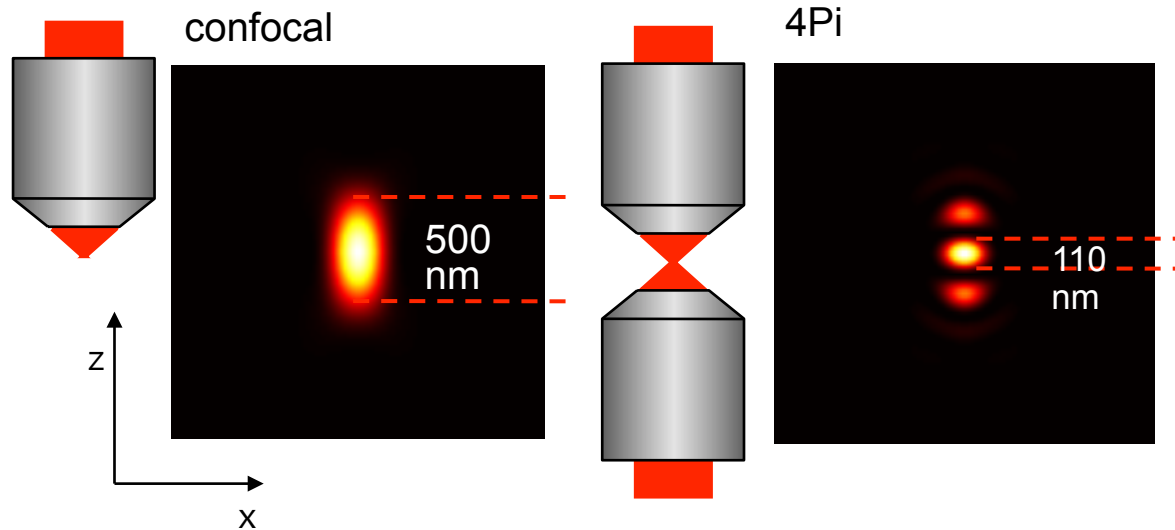


Fig.2



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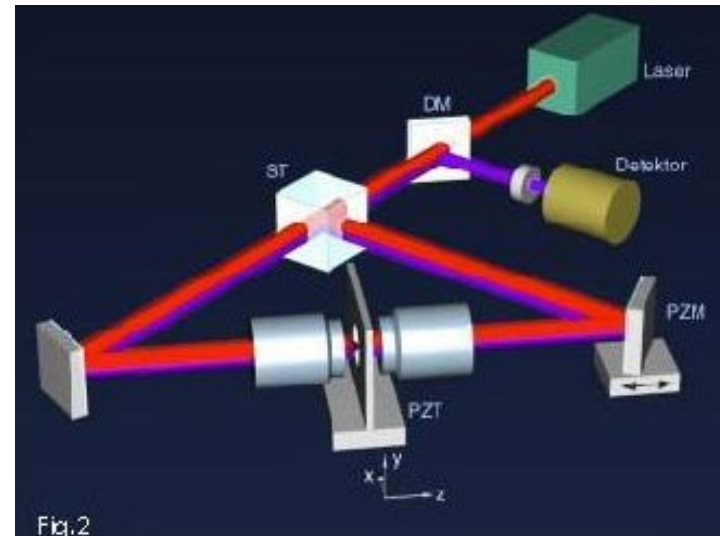
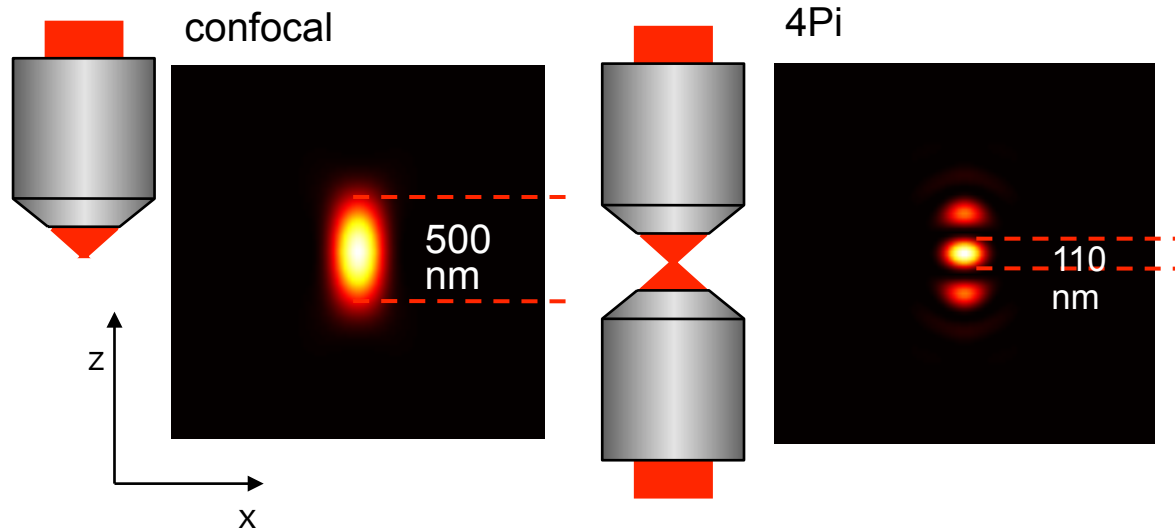


Fig.2



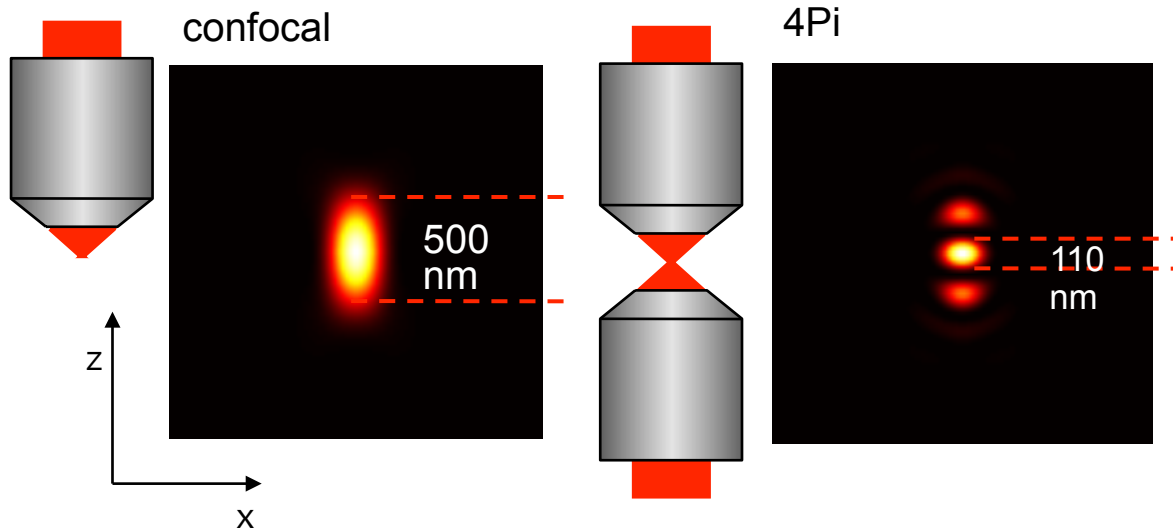
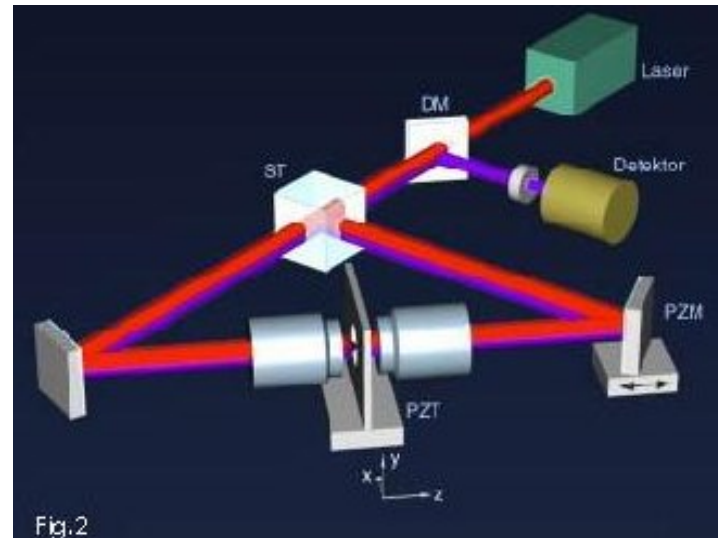
- constructive interference of excitation and emission light
- 5-8 times higher **axial resolution**: 110nm resolution @780 nm
- Side lobes can be eliminated by deconvolution

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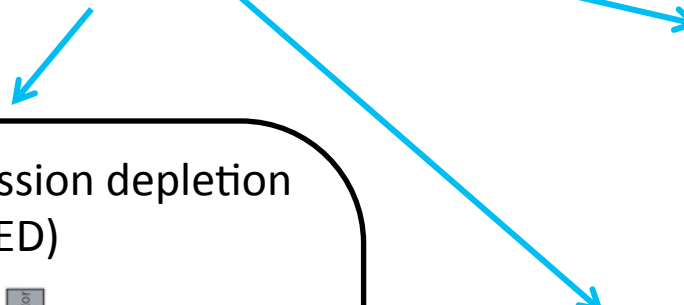
Problem: special sample requirements and need for physicist(s) to operate

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Structured illumination

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C STED microscope

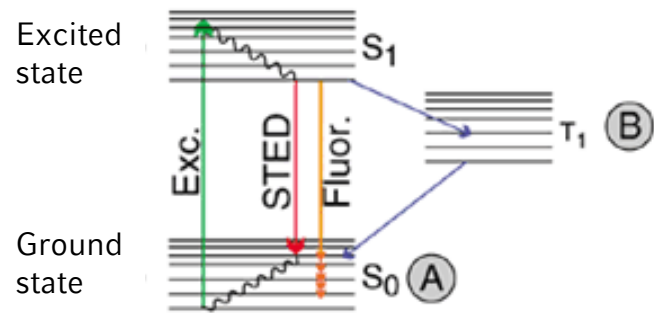
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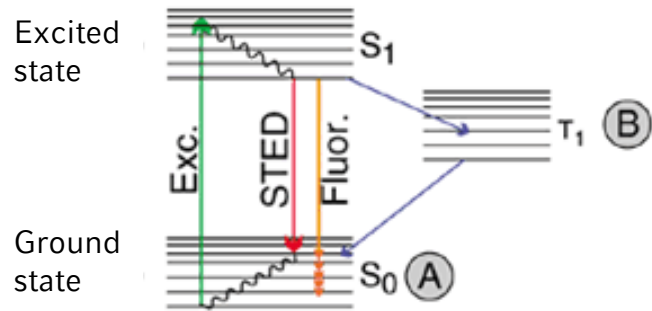
Stochastic optical reconstruction microscopy (STORM)

Cy5 fluorescence (A.U.) vs Time (s)

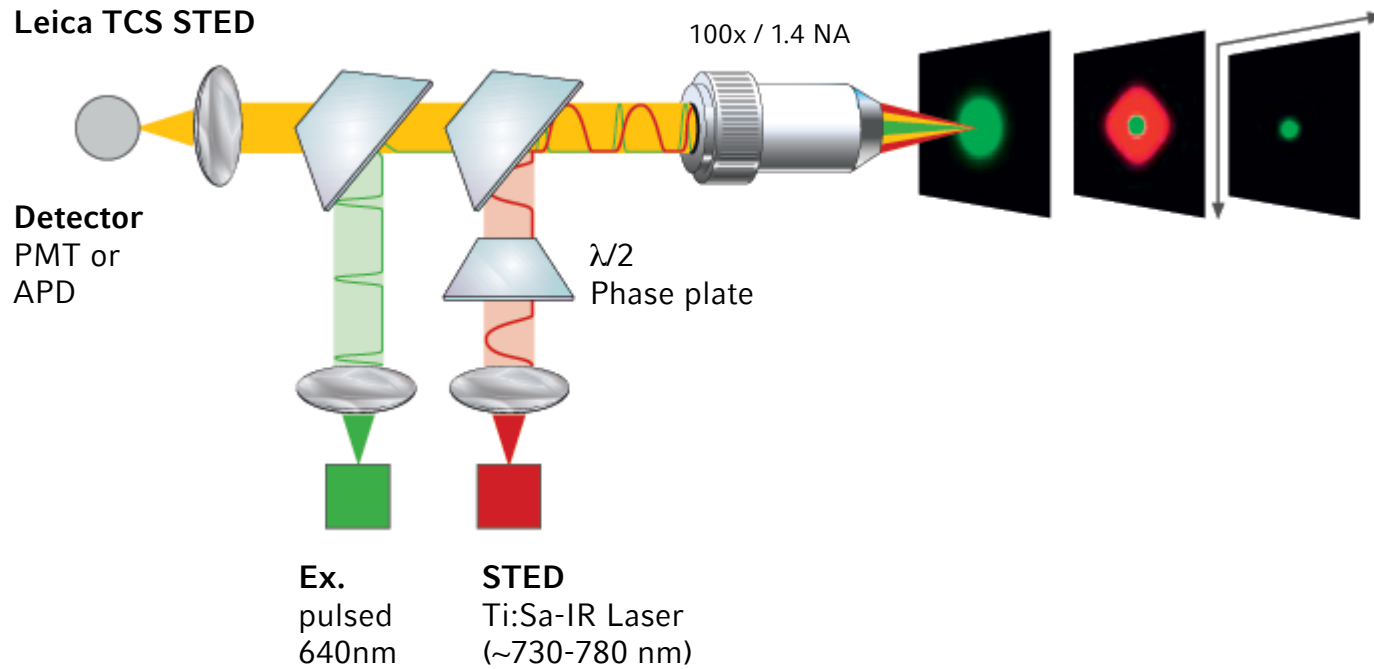
STED microscopy



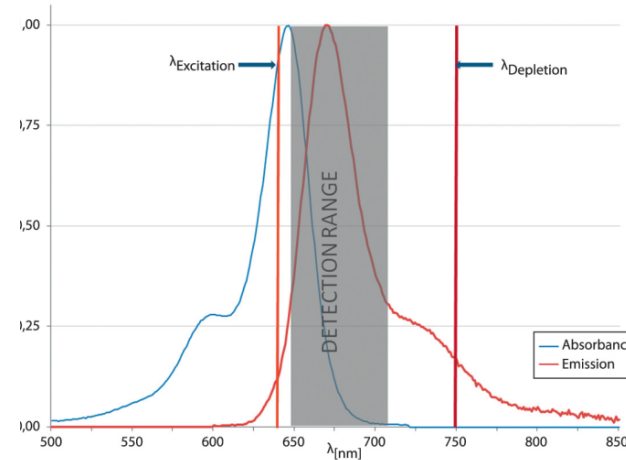
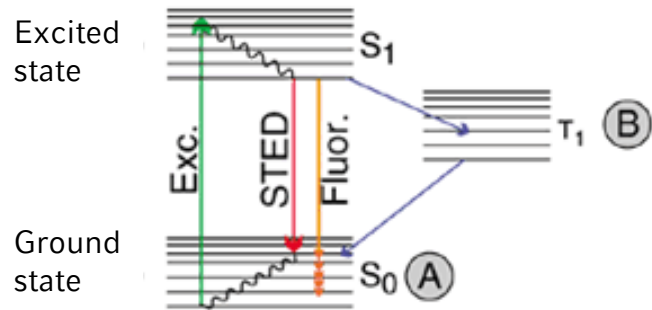
STED microscopy



Leica TCS STED

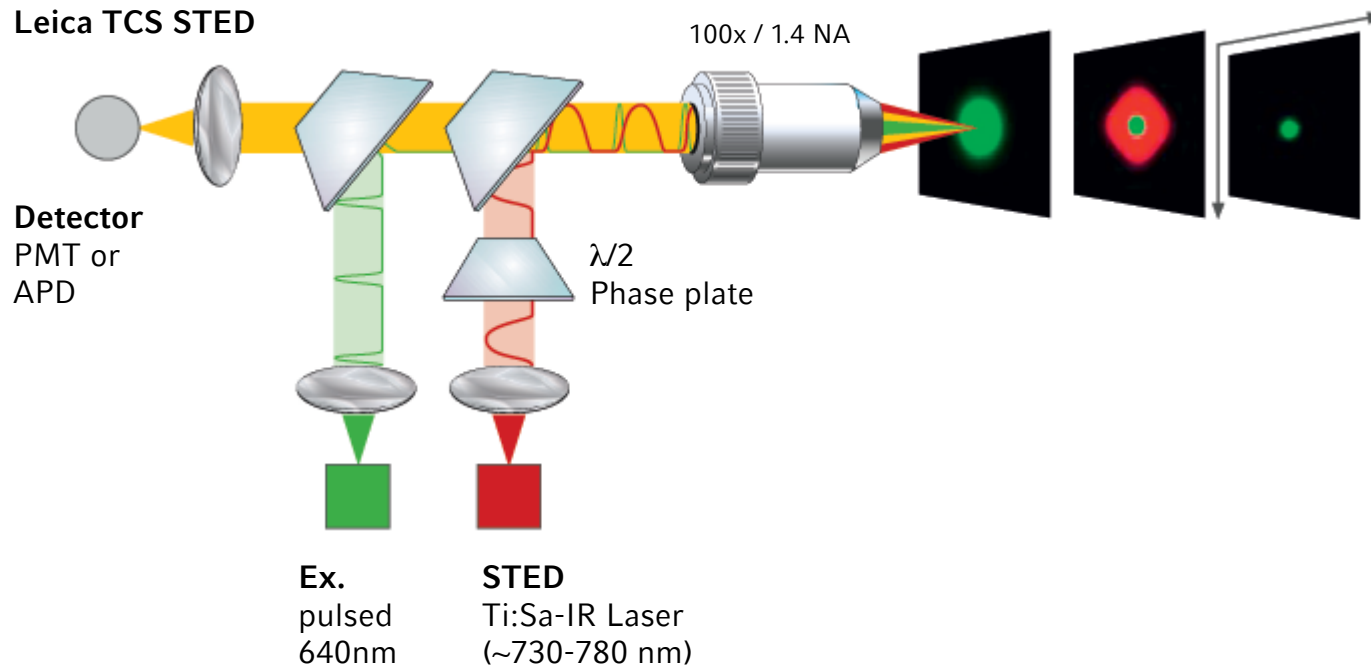


STED microscopy



Best dyes:
ATTO 647N
ATTO 655

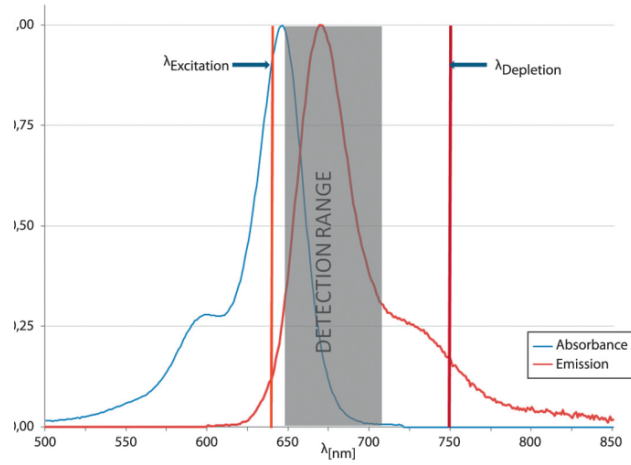
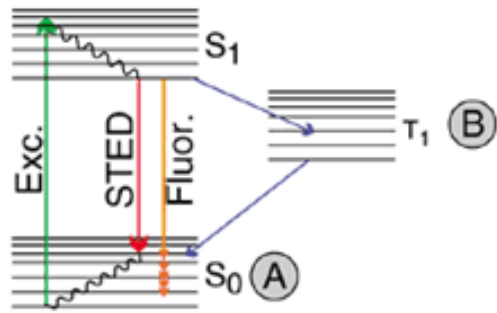
Leica TCS STED



STED microscopy

Excited state

Ground state



Best dyes:
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Leica TCS STED

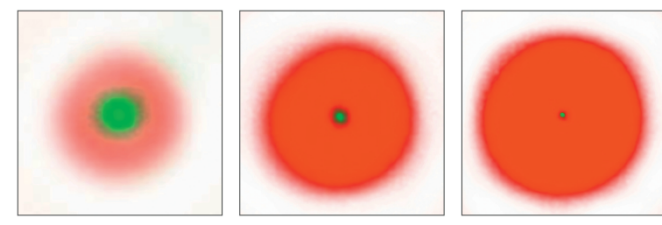
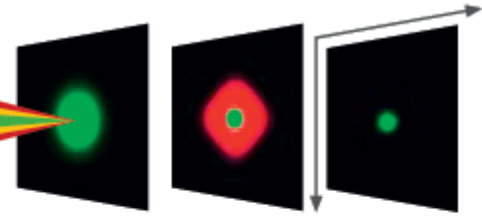
Detector
PMT or
APD

100x / 1.4 NA

$\lambda/2$
Phase plate

Ex.
pulsed
640nm

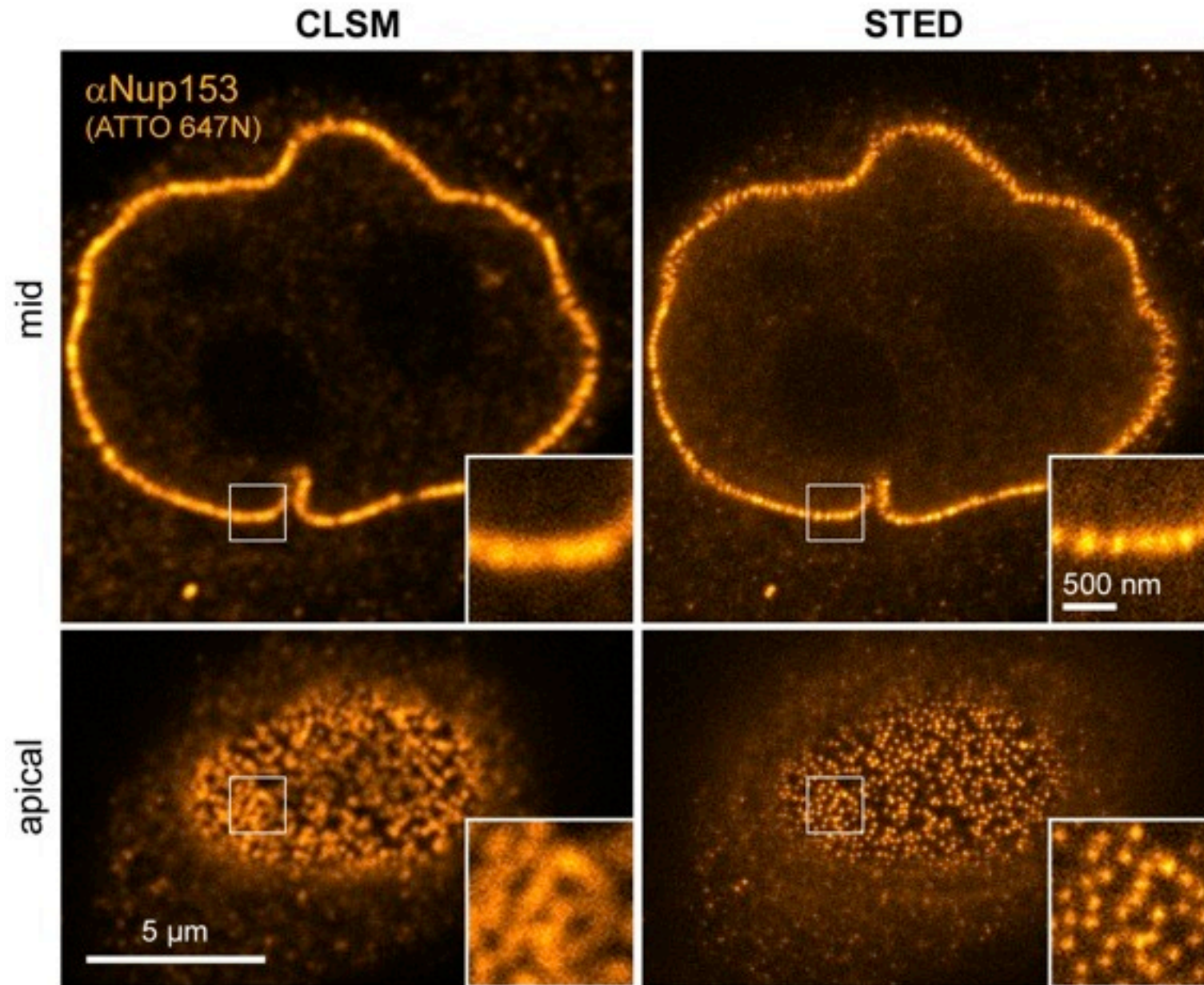
STED
Ti:Sa-IR Laser
(~730-780 nm)



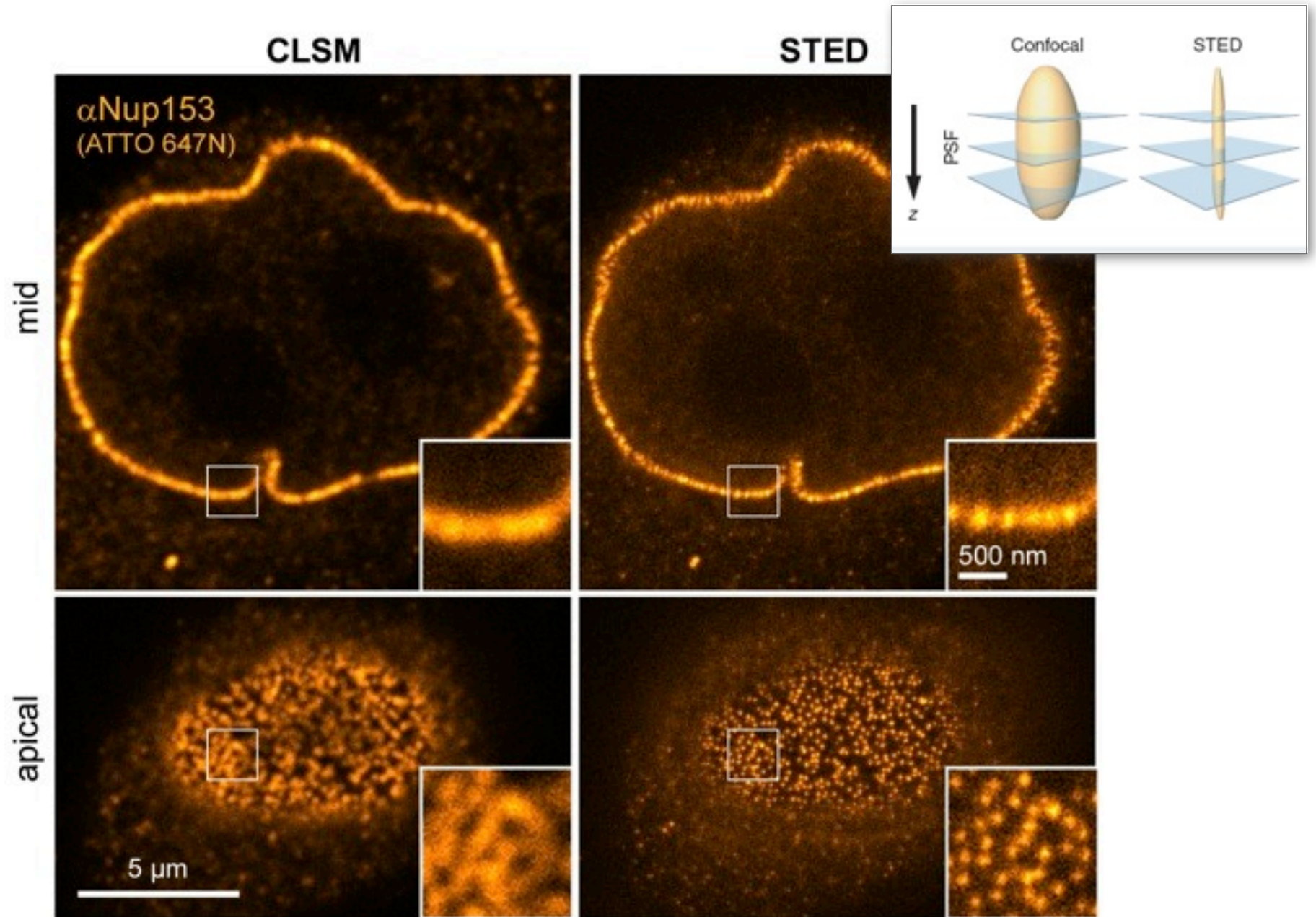
$$\Delta x \approx \frac{\lambda}{2n \sin \alpha \sqrt{1 + I/I_s}}$$

Resolution depends on the ratio of the depletion intensity (I) and the saturation intensity (I_s)

STED microscopy (Leica TCS)



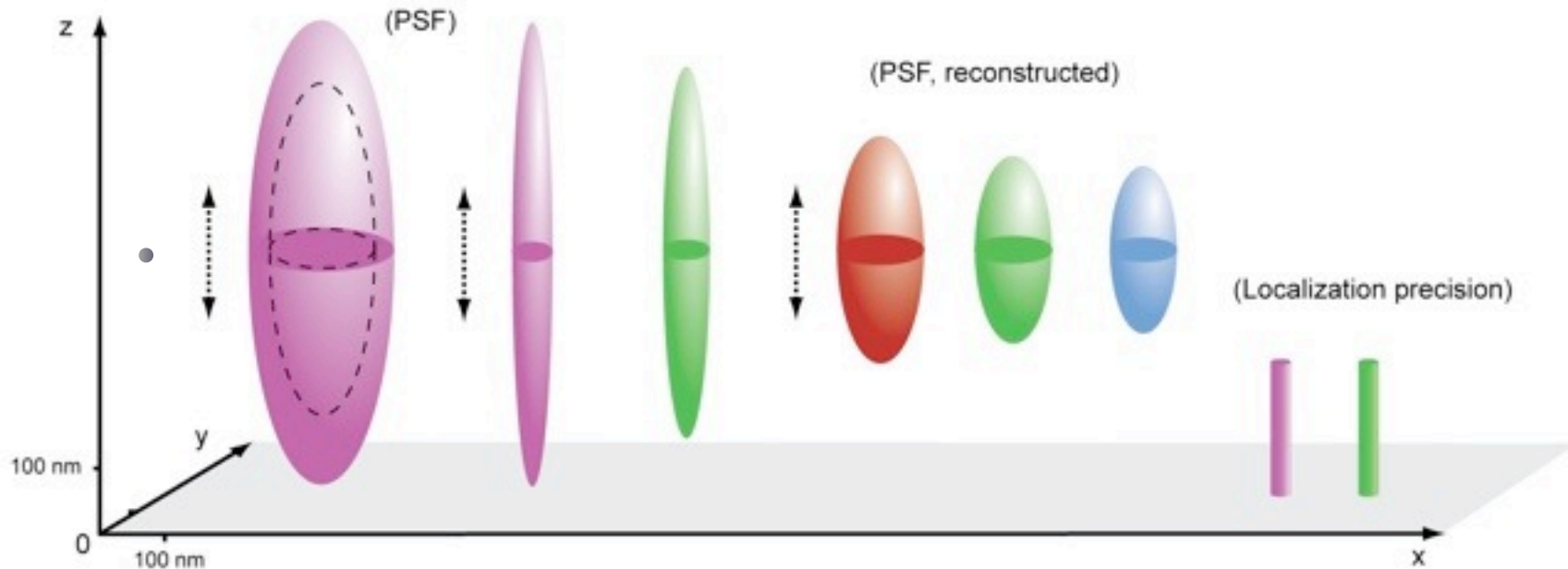
STED microscopy (Leica TCS)



Resolving power of current commercial setups

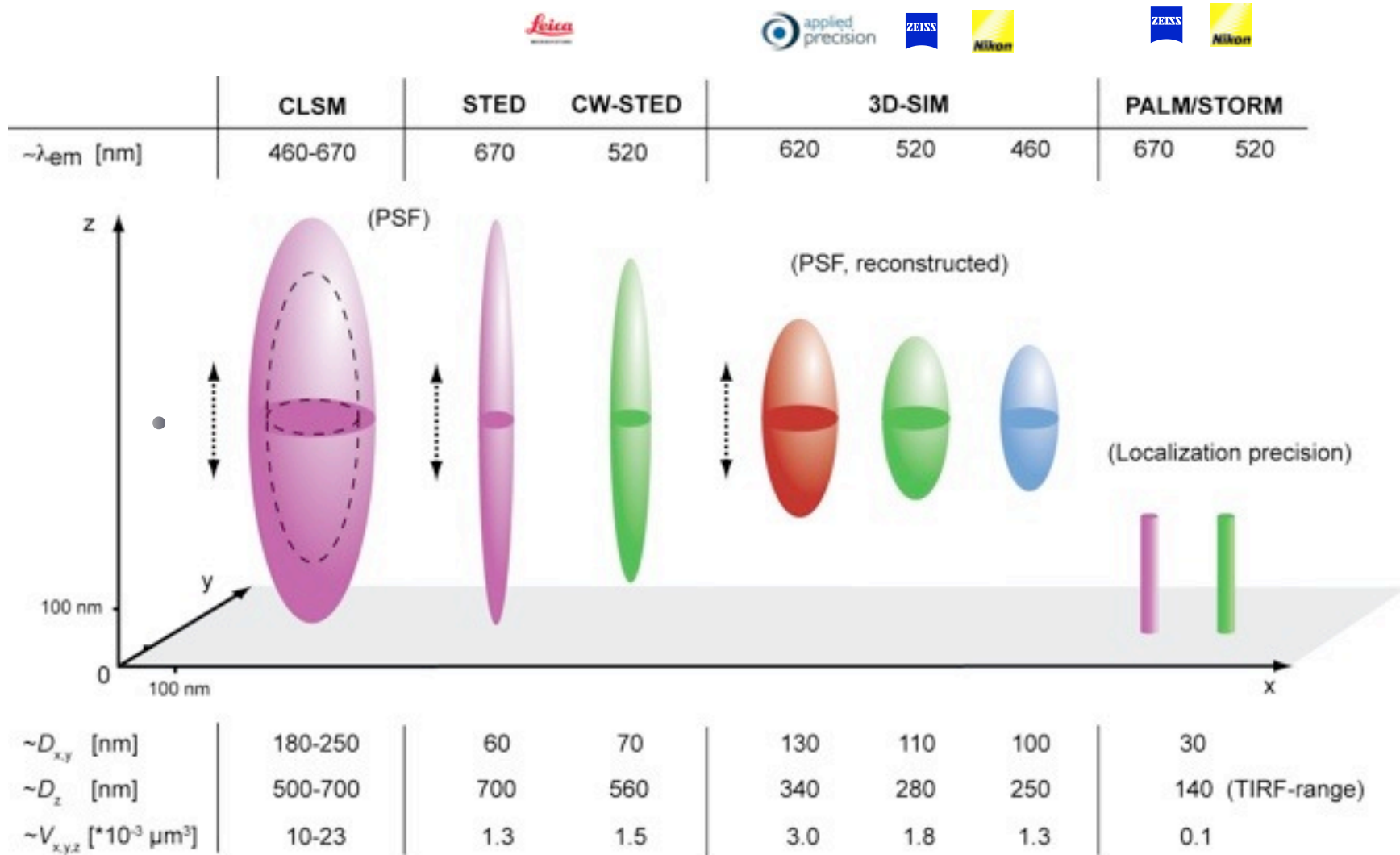


	CLSM	STED	CW-STED	3D-SIM			PALM/STORM	
$\sim\lambda_{em}$ [nm]	460-670	670	520	620	520	460	670	520



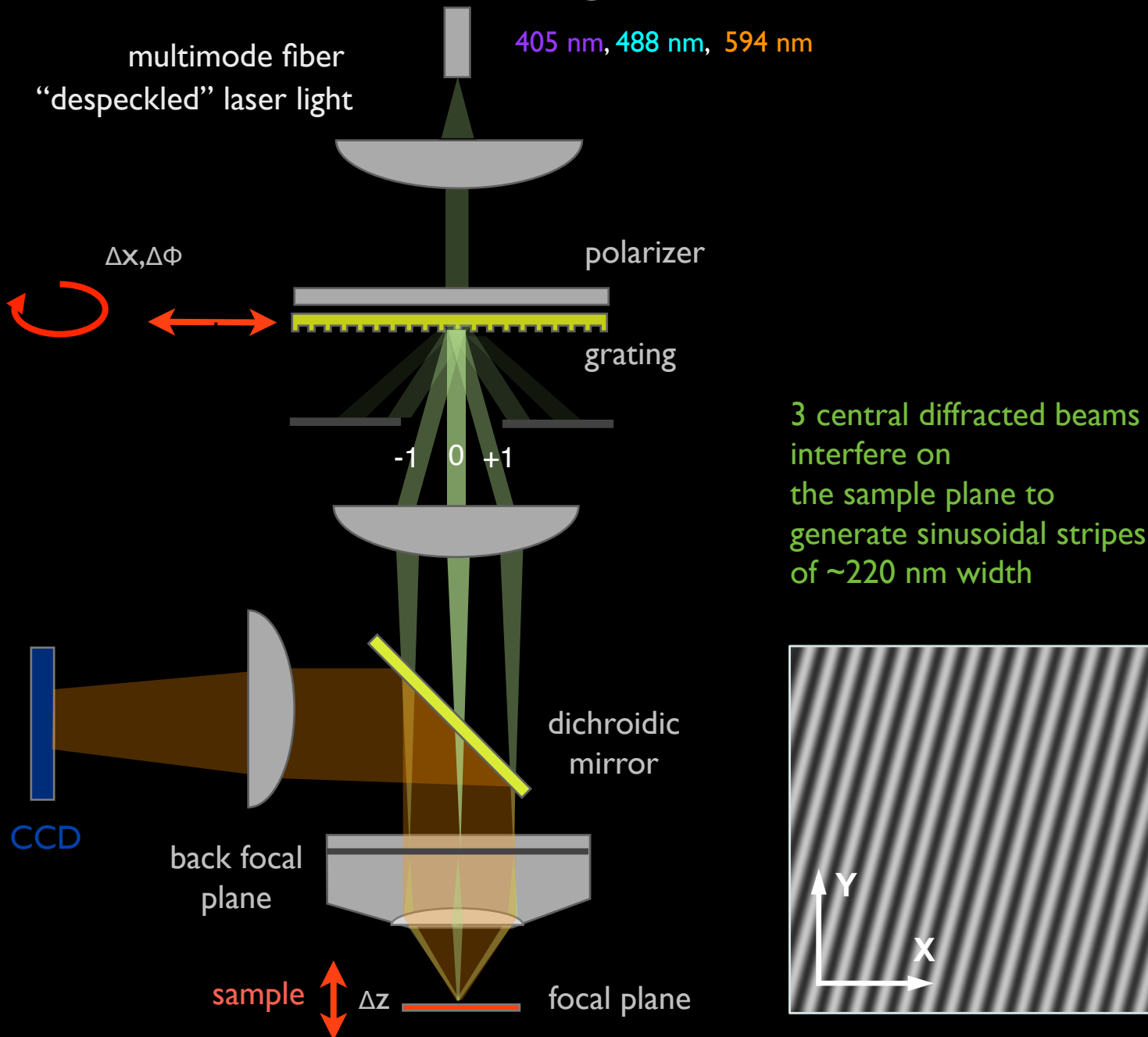
$\sim D_{x,y}$ [nm]	180-250	60	70	130	110	100	30
$\sim D_z$ [nm]	500-700	700	560	340	280	250	140 (TIRF-range)
$\sim V_{x,y,z}$ [$\cdot 10^{-3} \mu m^3$]	10-23	1.3	1.5	3.0	1.8	1.3	0.1

Resolving power of current commercial setups



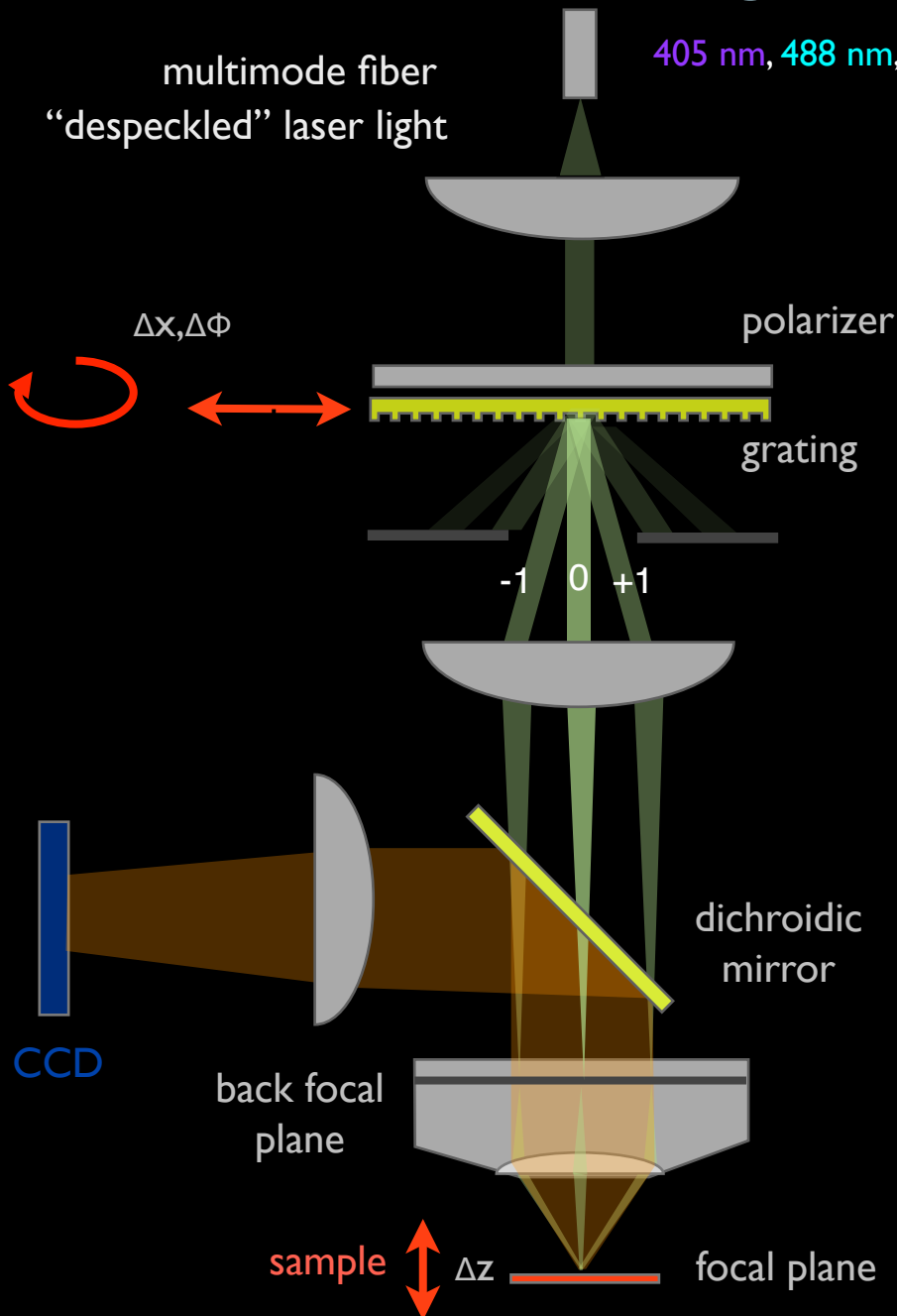
3D-SIM resolves ~ 8 -fold smaller volumes than confocal laser scanning microscopy (CLSM)

Generating 3D-structured illumination

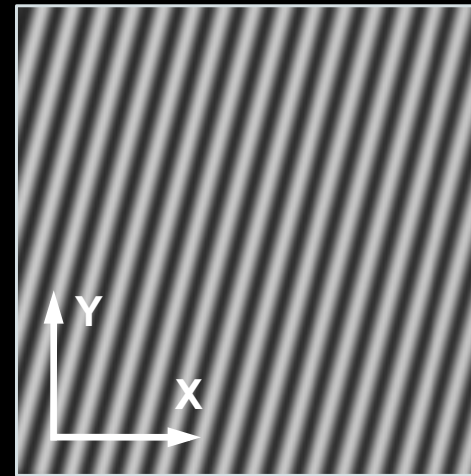


adapted from Gustafsson et al. (2008) *BiophysJ*, 94

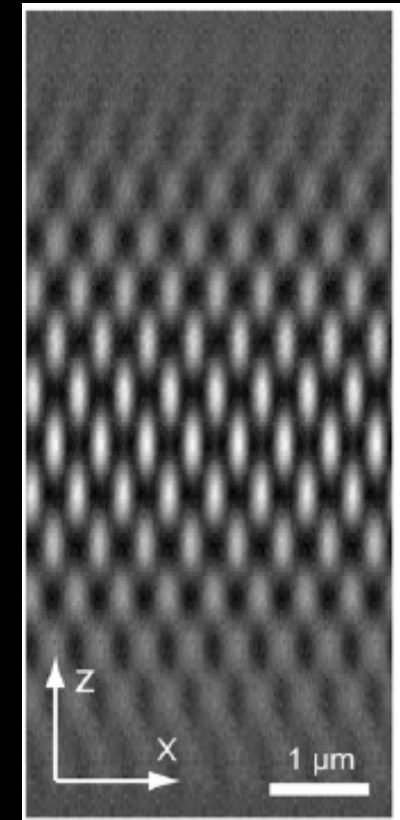
Generating 3D-structured illumination



3 central diffracted beams interfere on the sample plane to generate sinusoidal stripes of ~ 220 nm width



axial modulation



OMX: Housing

Dust filter

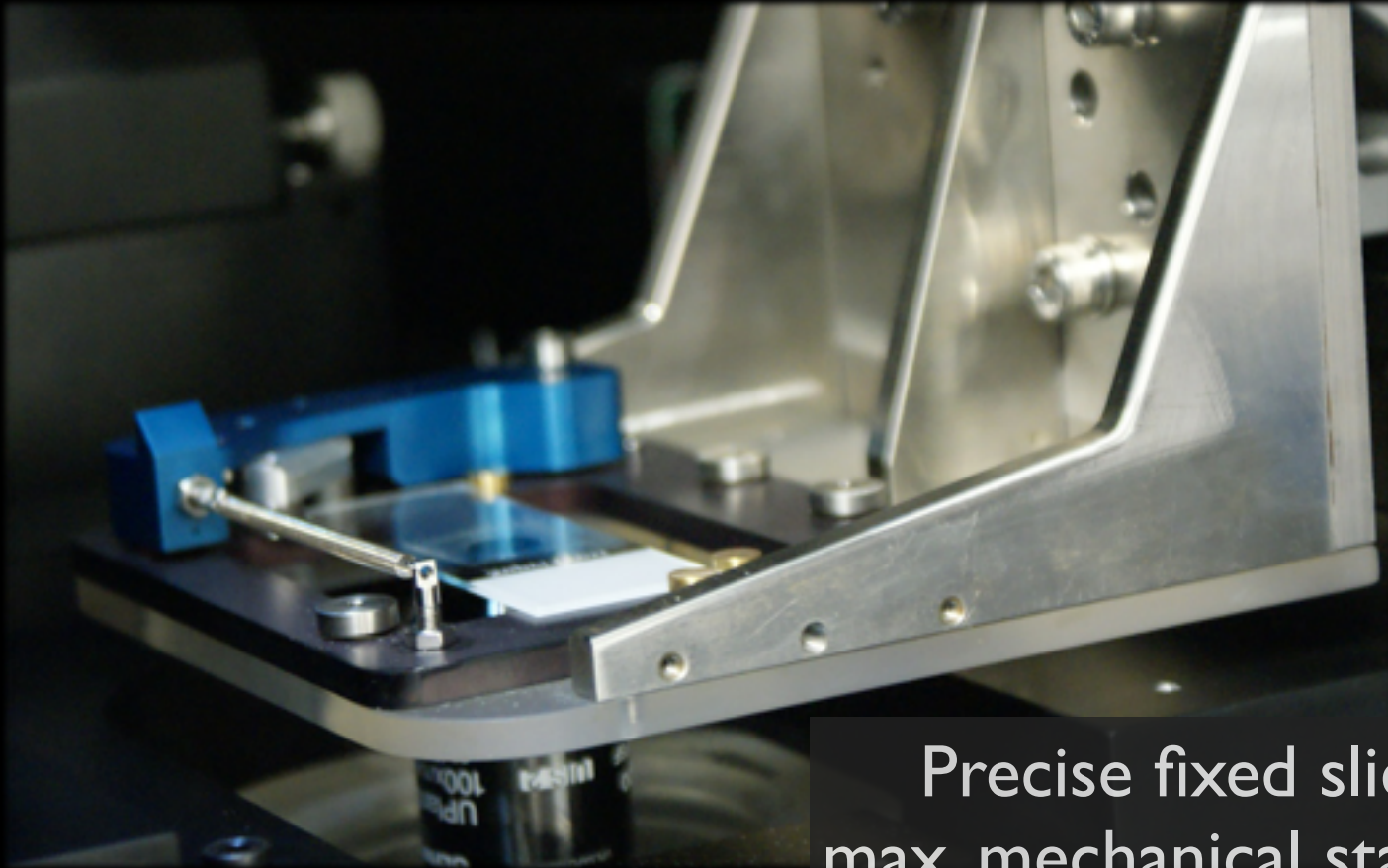
vibration-cushioned
table & housing

Optical filters

inside ?

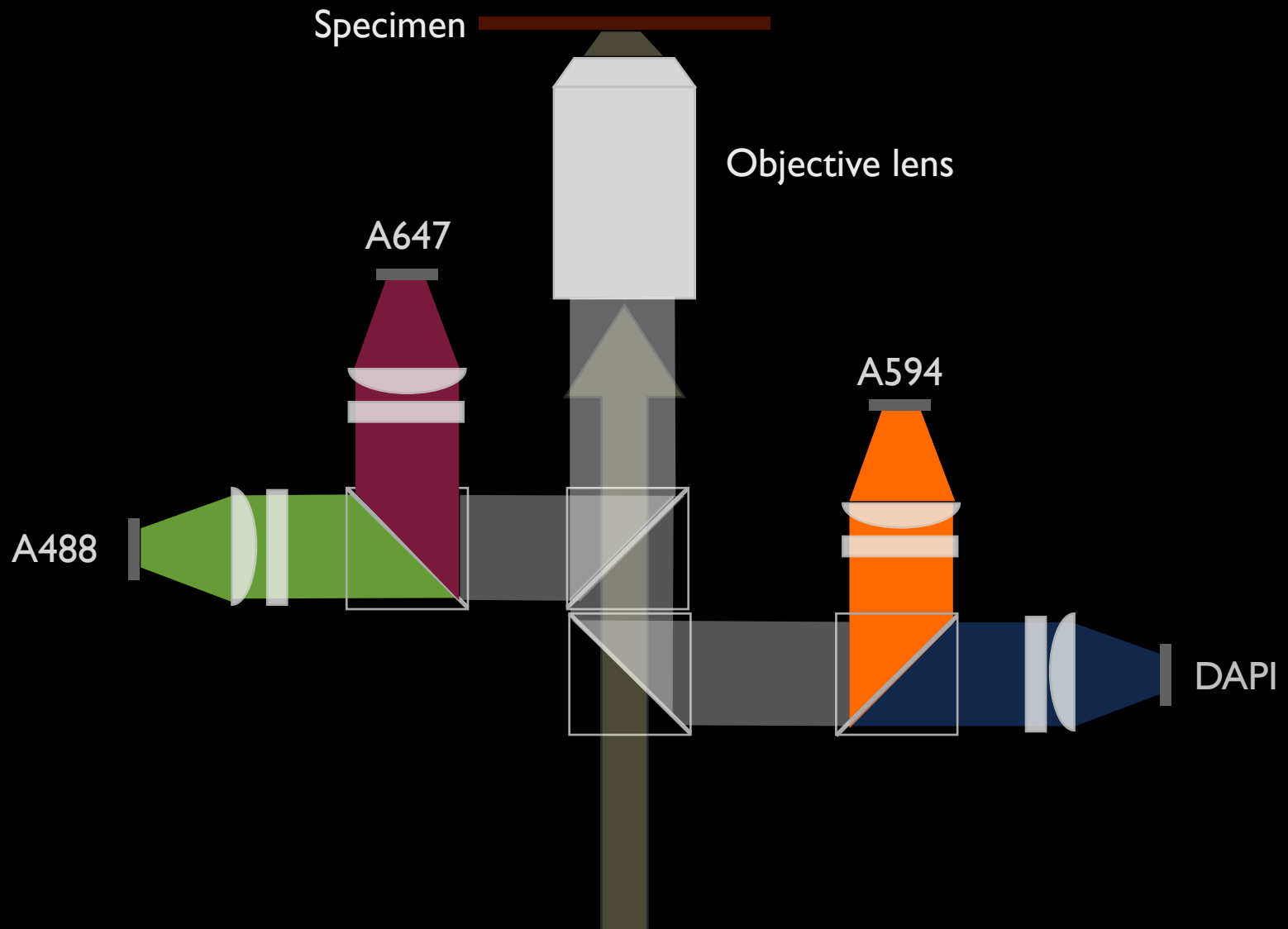


OMX: Stage

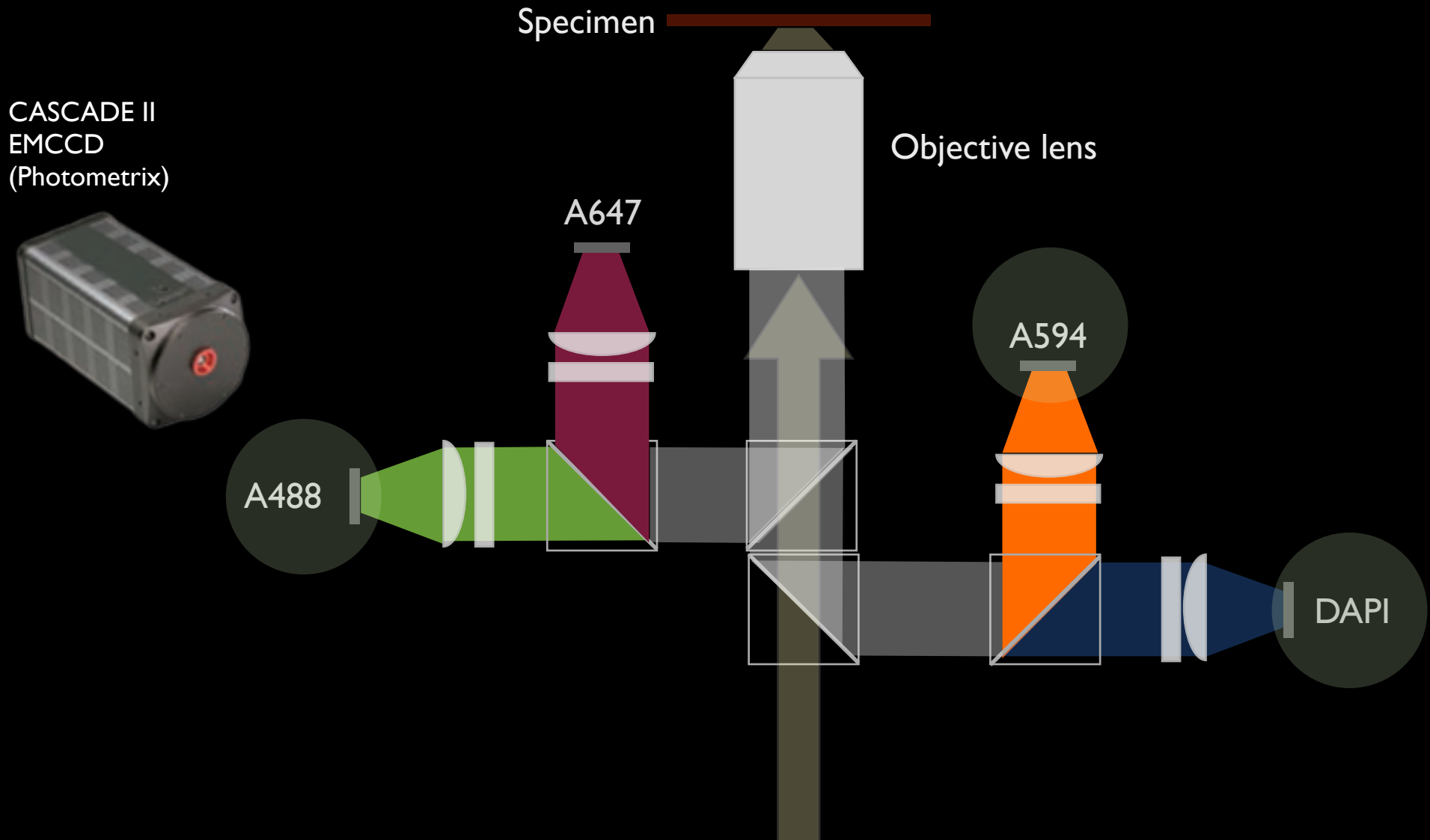


Precise fixed slide
max. mechanical stability
low thermal drift

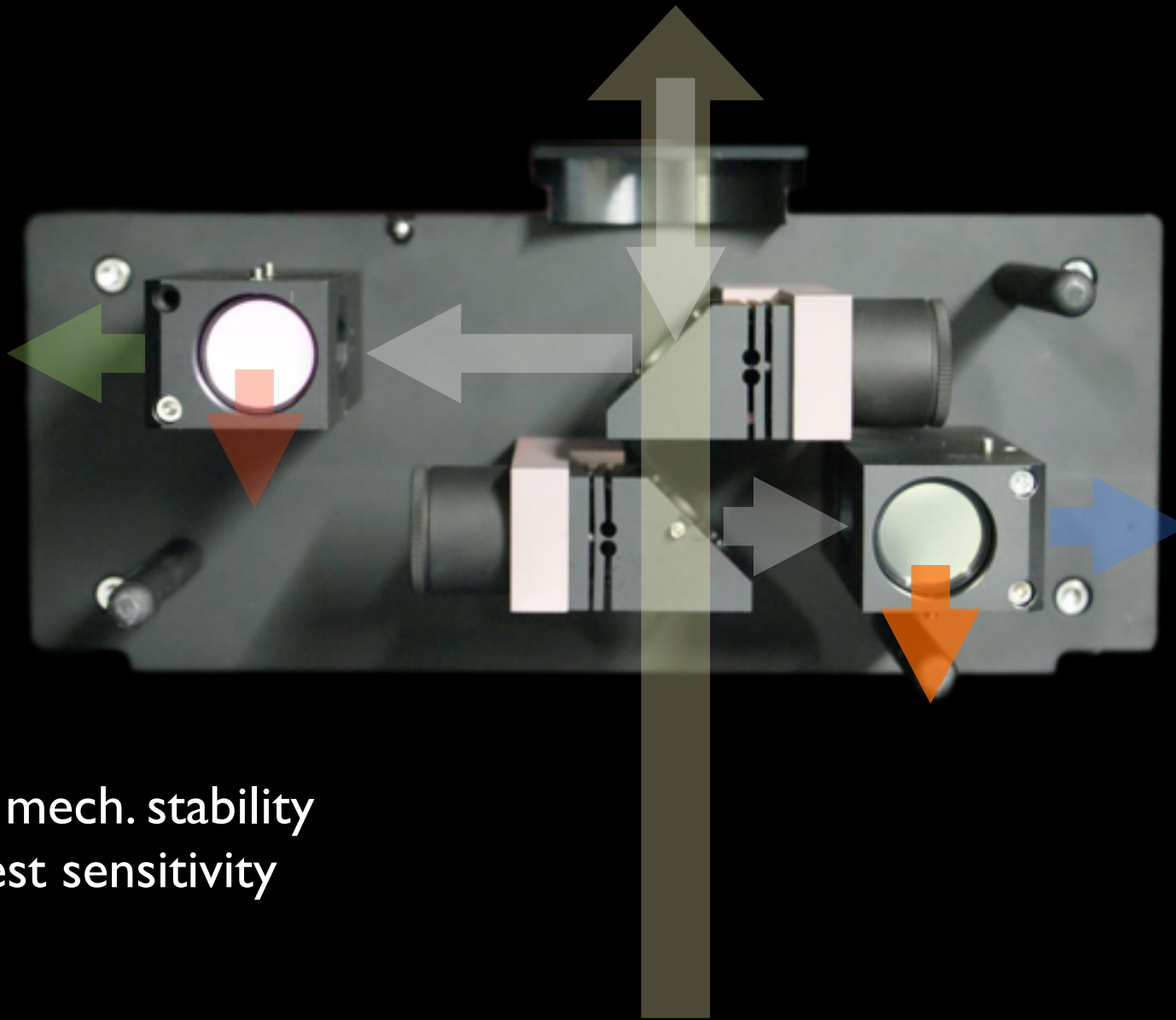
OMX: Filter Drawer Design



OMX: Filter Drawer Design

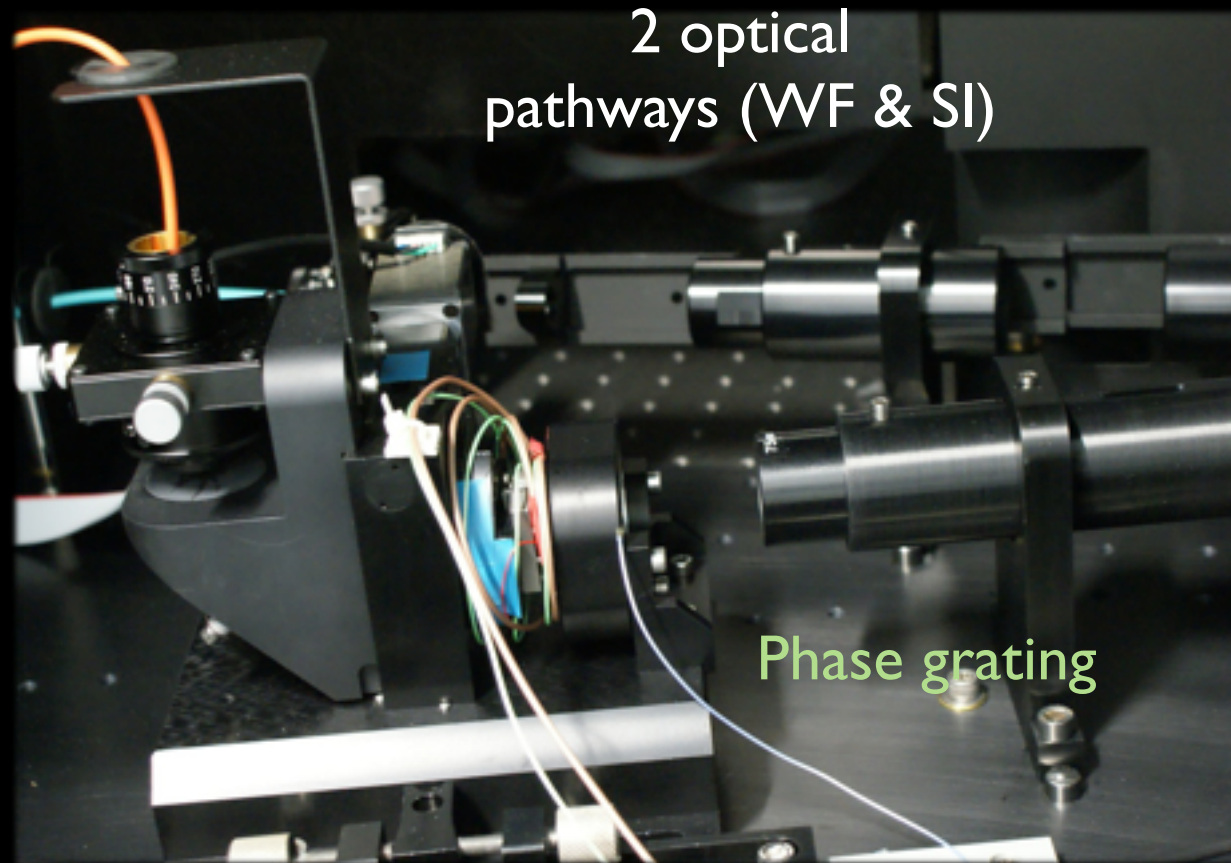


OMX: Filter Drawer Design



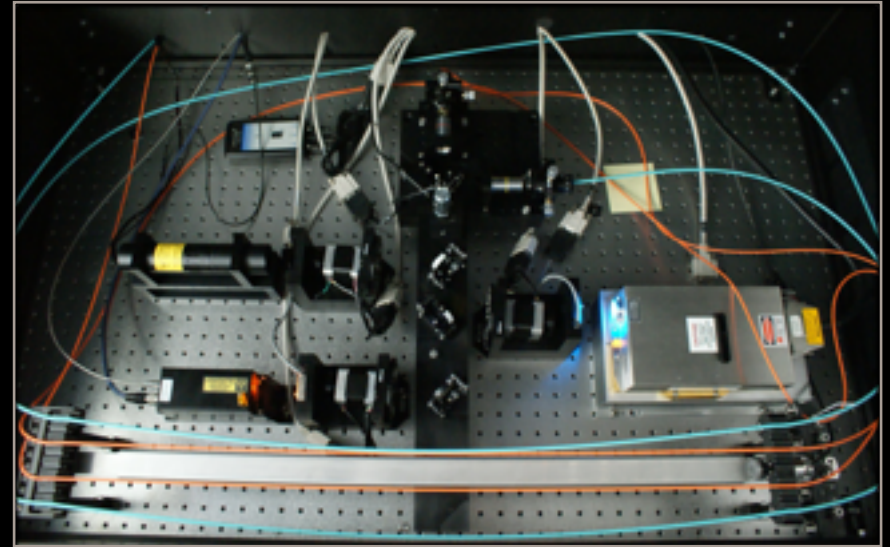
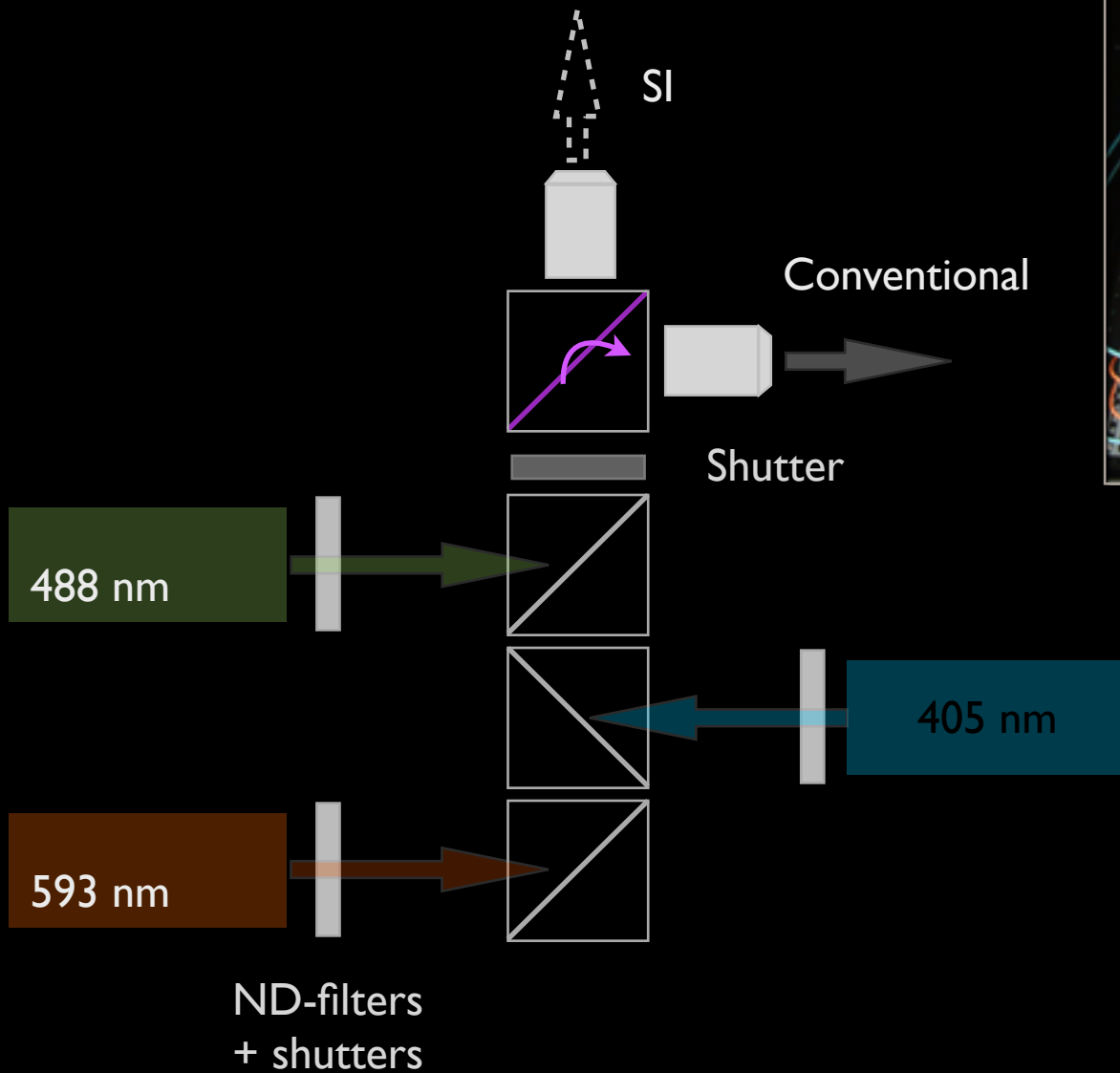
max. mech. stability
highest sensitivity

OMX: Dual illumination pathways



OMX: Laser unit

extendible / adaptable bread-board setup

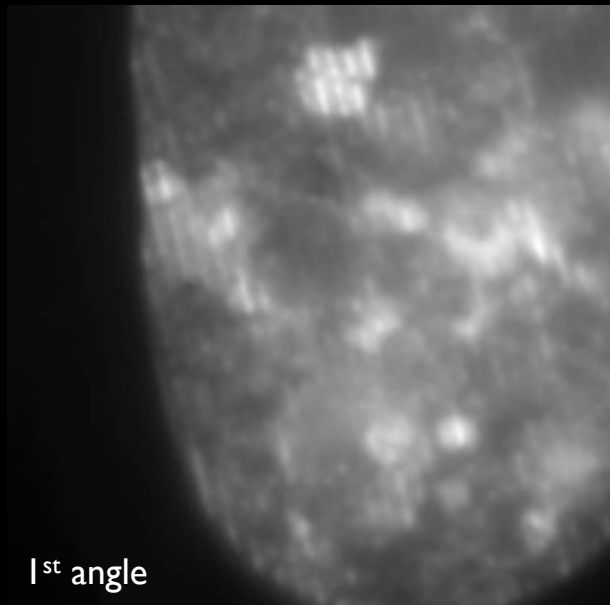


OMX: Electronics rack



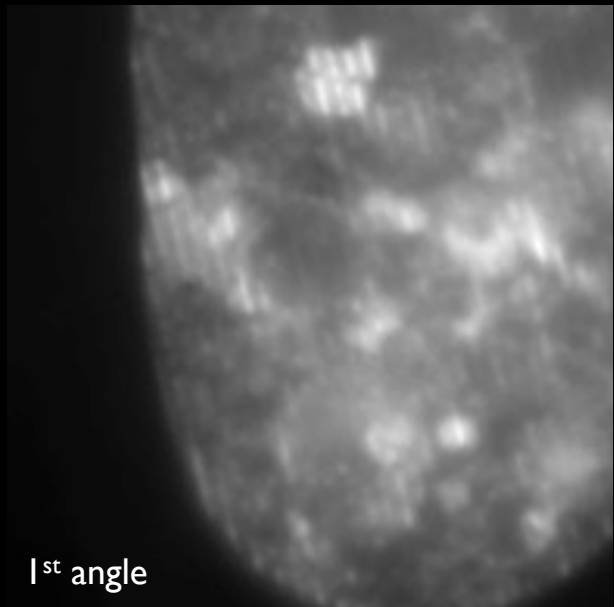
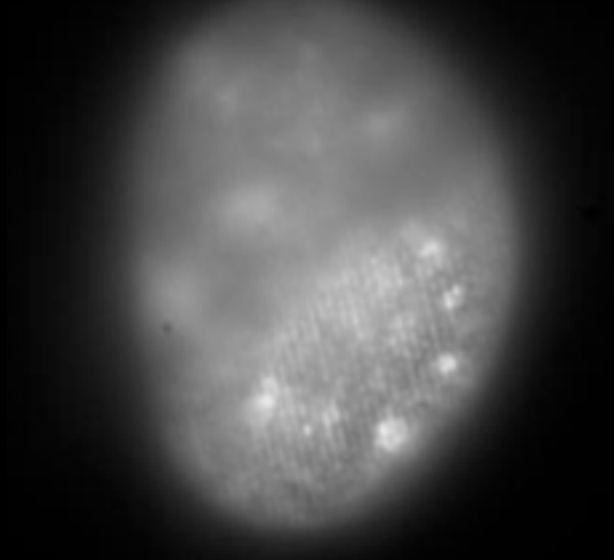
3D-SIM image acquisition and reconstruction

5 phases, 3 stacks



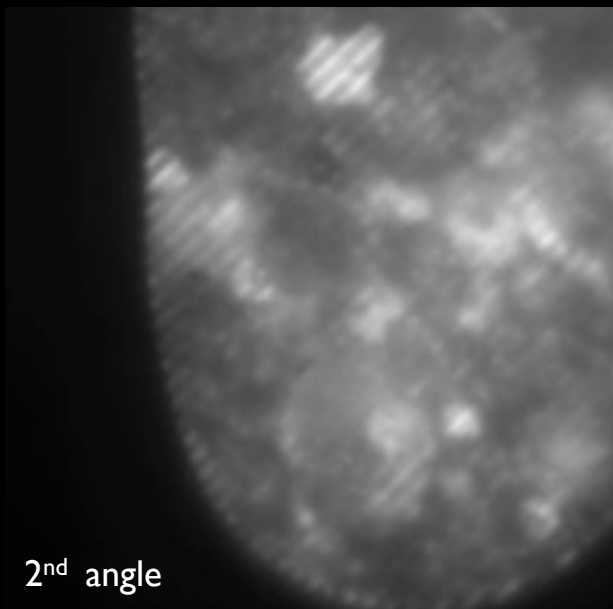
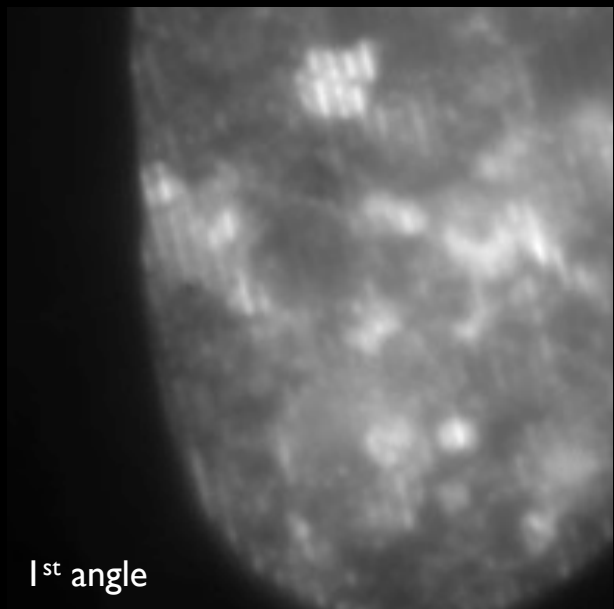
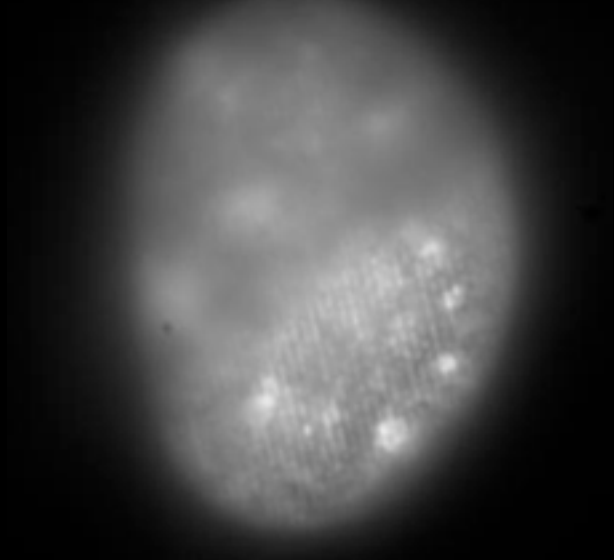
3D-SIM image acquisition and reconstruction

5 phases, 3 stacks



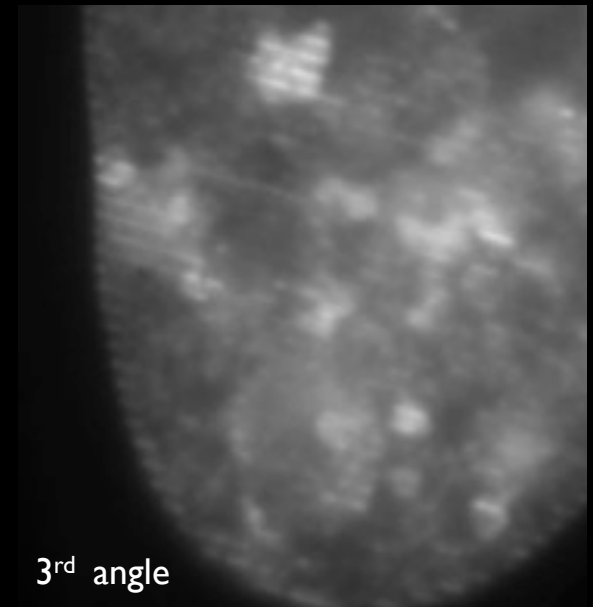
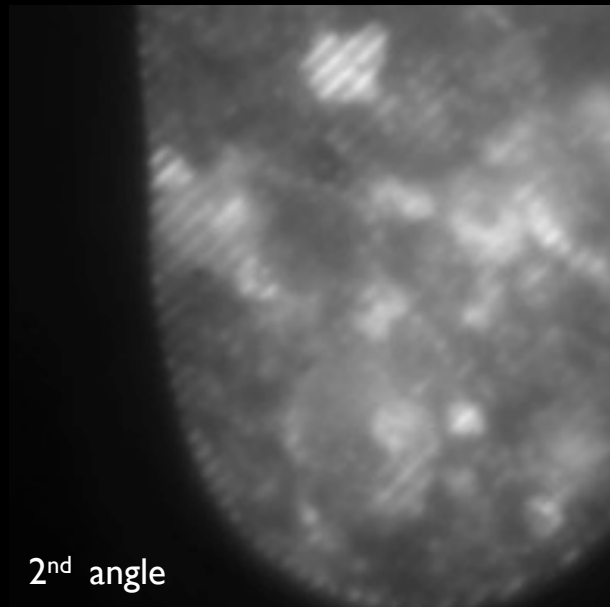
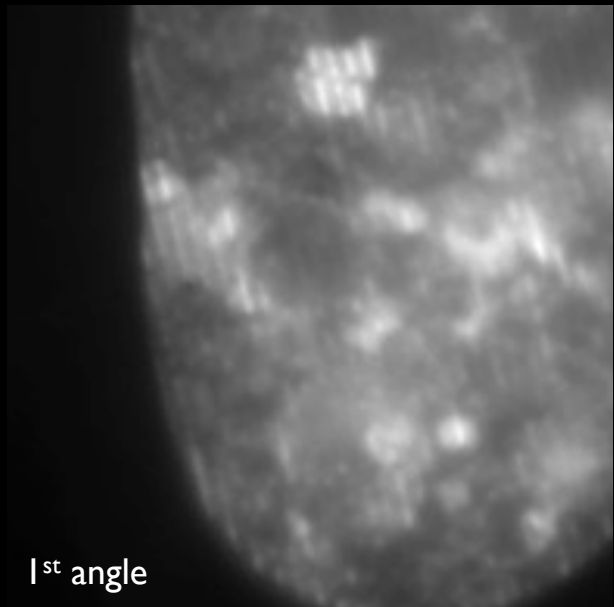
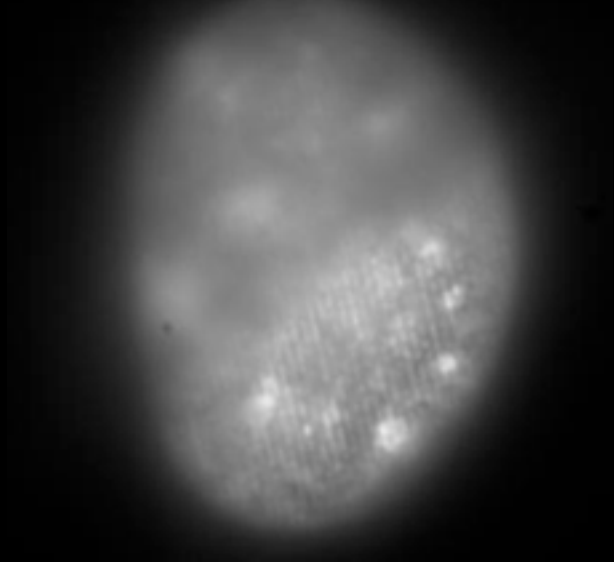
3D-SIM image acquisition and reconstruction

5 phases, 3 stacks



3D-SIM image acquisition and reconstruction

5 phases, 3 stacks



3D-SIM image acquisition and reconstruction

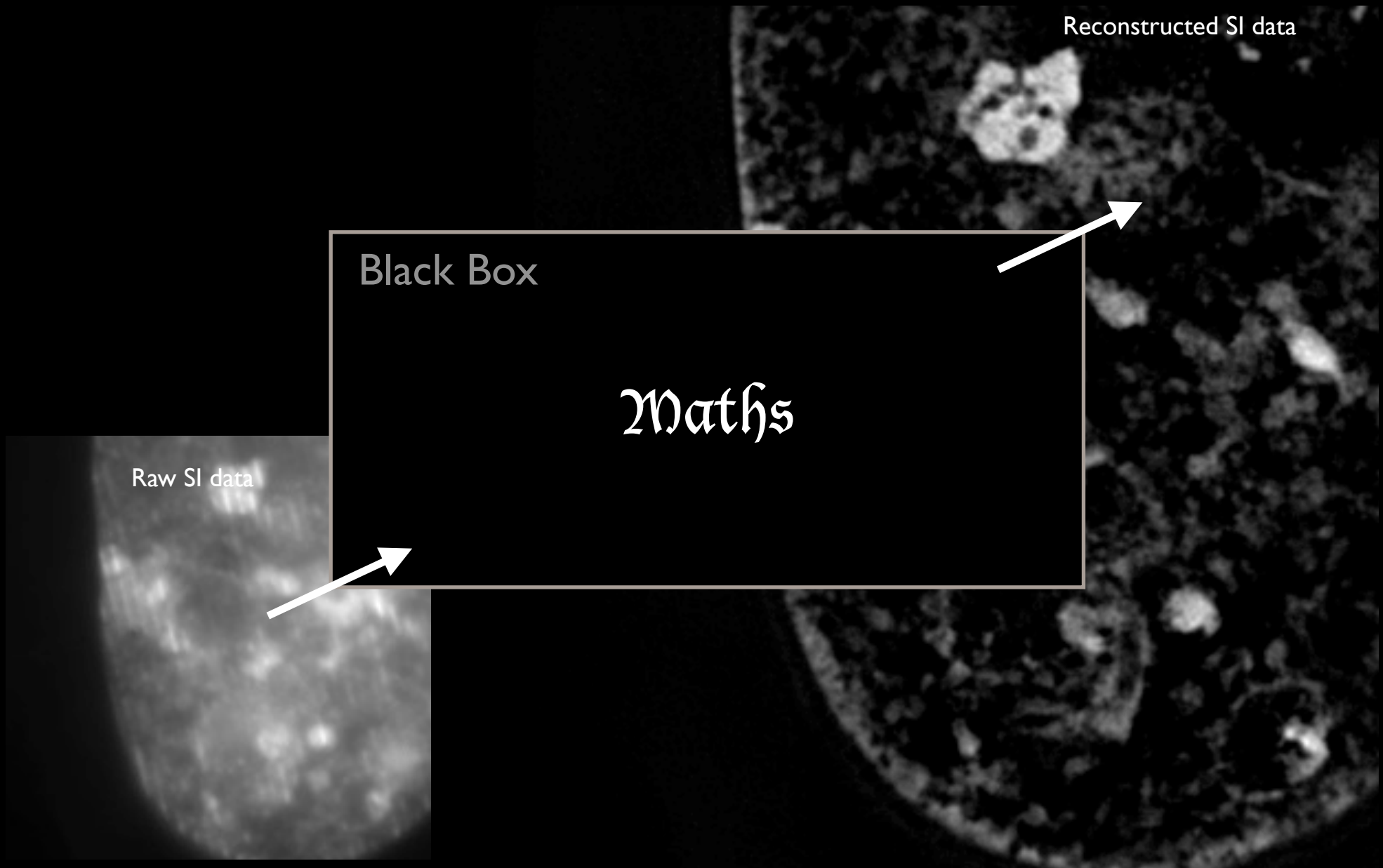
5 phases, 3 stacks

Reconstructed optical section

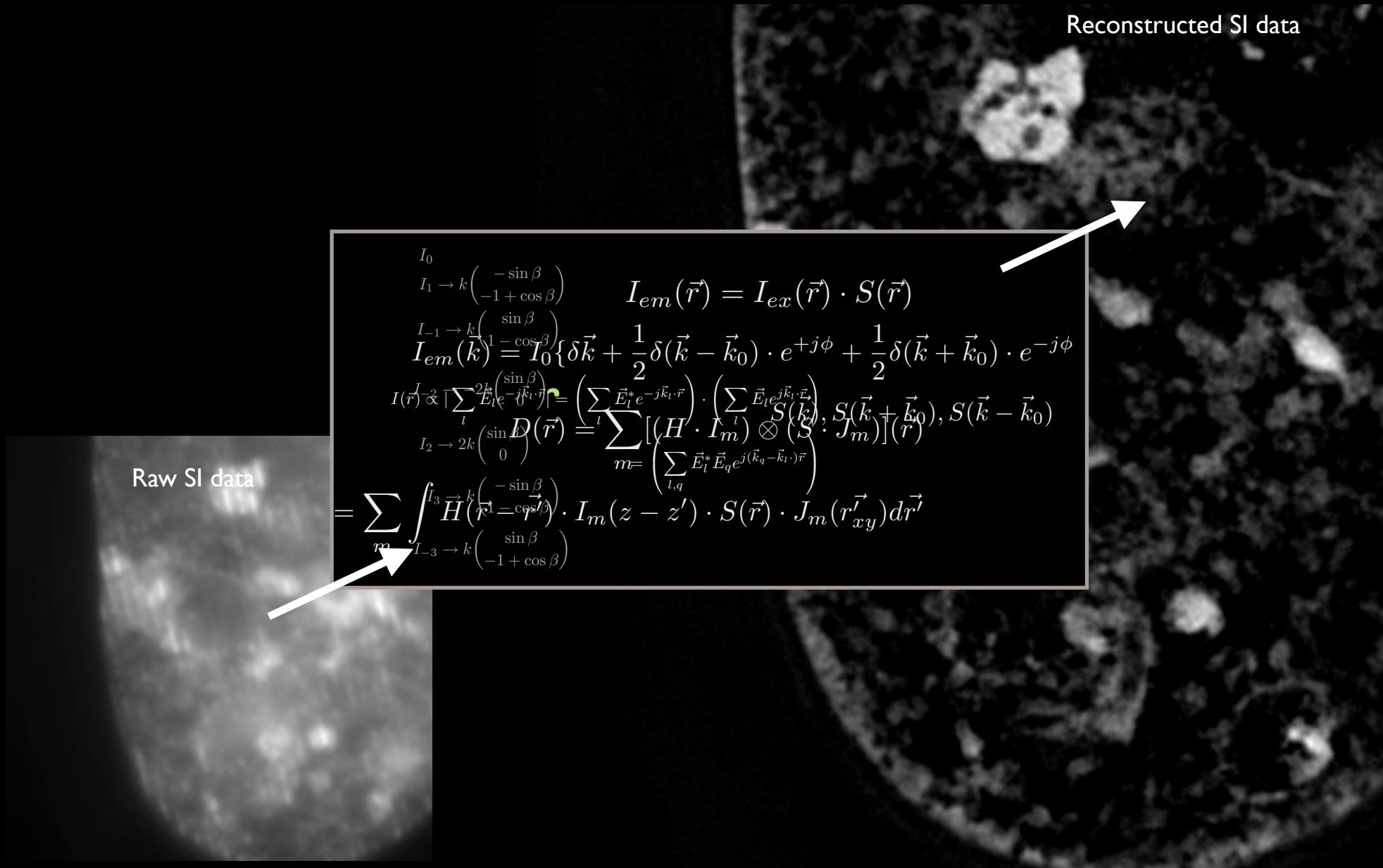
- ▶ each optical plane is recorded 15x ! (5 phases + 3 angles)
- ▶ typically ~1000 exposures per 8 μm stack (per wavelength)
- ▶ exposure time 10-100 ms; stack acquisition time few 10 seconds to minutes

1st angle

3D-SIM image acquisition and reconstruction



3D-SIM image acquisition and reconstruction

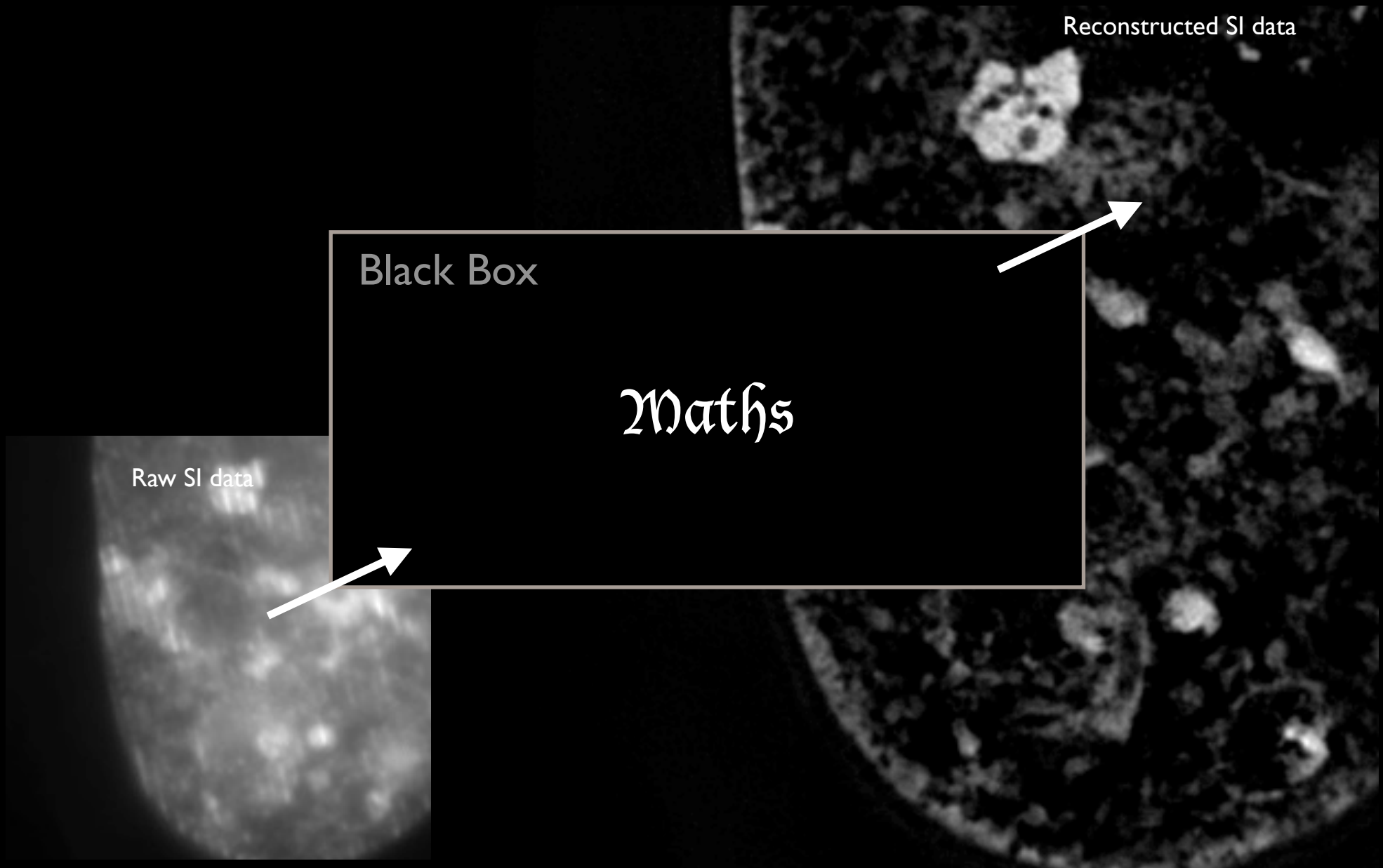


Reconstructed SI data

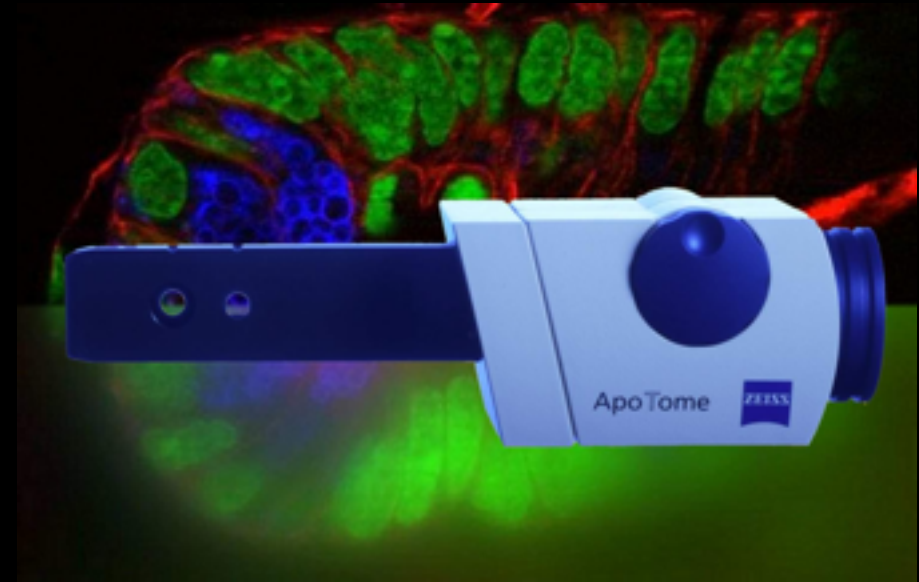
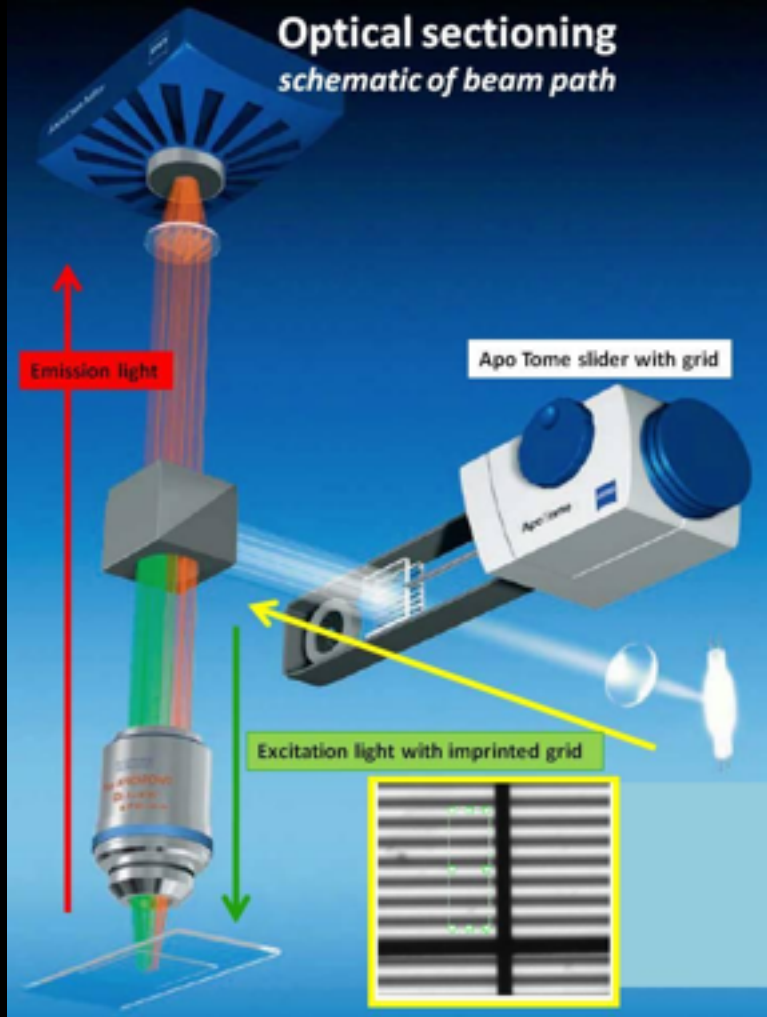
Raw SI data

$$\begin{aligned}
 I_0 & \rightarrow k \begin{pmatrix} -\sin \beta \\ -1 + \cos \beta \end{pmatrix} & I_{em}(\vec{r}) &= I_{ex}(\vec{r}) \cdot S(\vec{r}) \\
 I_{-1} & \rightarrow k \begin{pmatrix} \sin \beta \\ 1 - \cos \beta \end{pmatrix} & I_{em}(\vec{k}) &= I_0 \left\{ \delta(\vec{k}) + \frac{1}{2} \delta(\vec{k} - \vec{k}_0) \cdot e^{+j\phi} + \frac{1}{2} \delta(\vec{k} + \vec{k}_0) \cdot e^{-j\phi} \right\} \\
 I & \rightarrow k \begin{pmatrix} \sin \beta \\ 0 \end{pmatrix} & I(\vec{r}) &\propto \left[\sum_l \vec{E}_l e^{-j\vec{k}_l \cdot \vec{r}} \right] = \left(\sum_l \vec{E}_l^* e^{-j\vec{k}_l \cdot \vec{r}} \right) \cdot \left(\sum_l \vec{E}_l e^{j\vec{k}_l \cdot \vec{r}} \right) \\
 I_2 & \rightarrow 2k \begin{pmatrix} \sin \beta \\ 0 \end{pmatrix} & D(\vec{r}) &= \sum_{m=1}^l \left[(\vec{H} \cdot \vec{I}_m) \otimes (\vec{S} \cdot \vec{J}_m) \right] (\vec{r}) \\
 & & &= \sum_{l,q} \left(\sum_{l,q} \vec{E}_l^* \vec{E}_q e^{j(\vec{k}_q - \vec{k}_l) \cdot \vec{r}} \right) \\
 & & &= \sum_m \int_{-3}^3 \vec{H}(\vec{r} = c\vec{e}_z/\beta) \cdot I_m(z - z') \cdot S(\vec{r}) \cdot J_m(r'_{xy}) dr'
 \end{aligned}$$

3D-SIM image acquisition and reconstruction



ApoTome uses coarse SI to remove out-of-focus blur

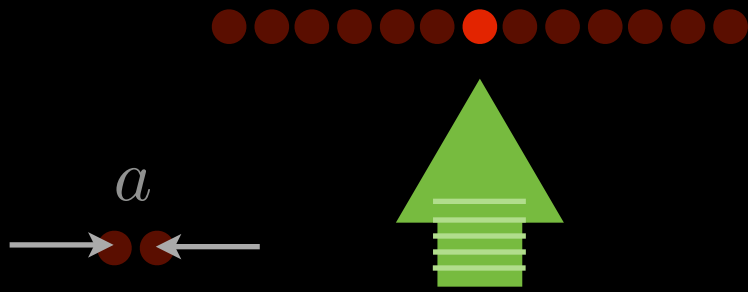


„Poor man's confocal“
No super-resolution!

The basic principle: Abbe's view

Sample = Structure

→ Periodicity

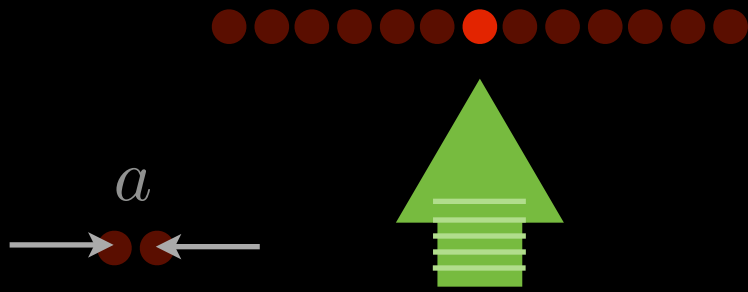


http://de.wikipedia.org/wiki/Ernst_Abbe

The basic principle: Abbe's view

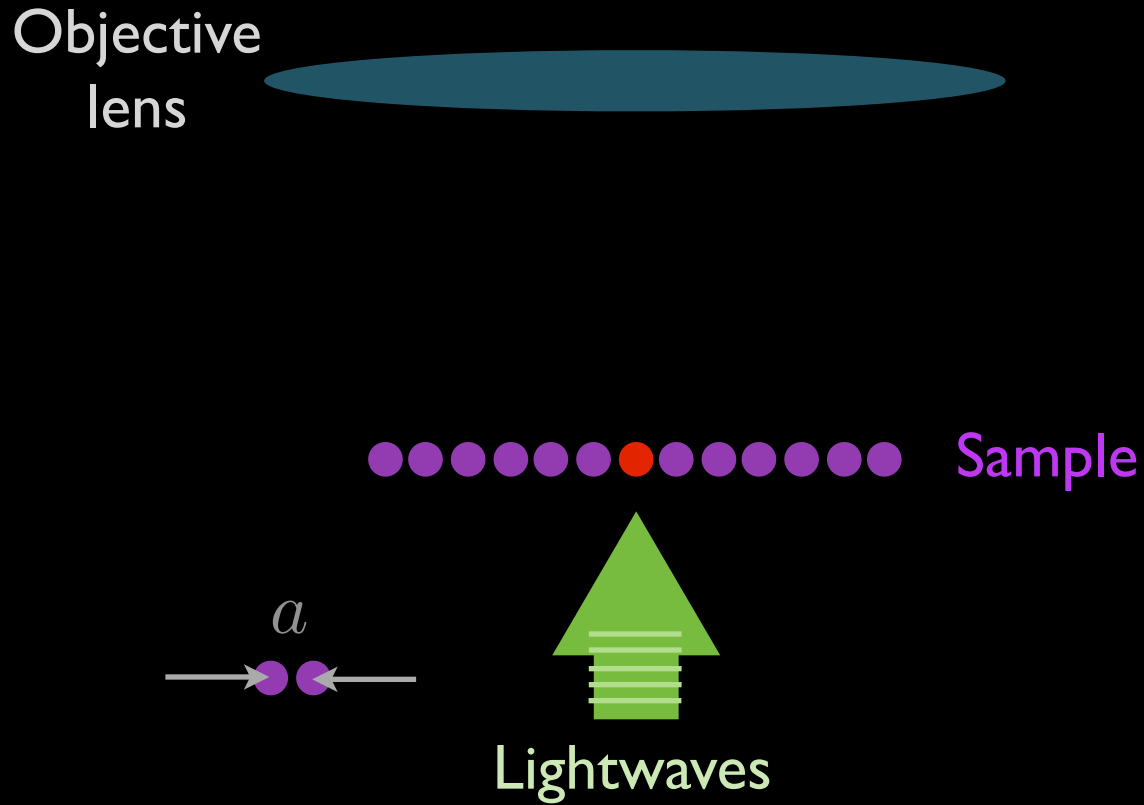
Sample = Structure

→ Periodicity

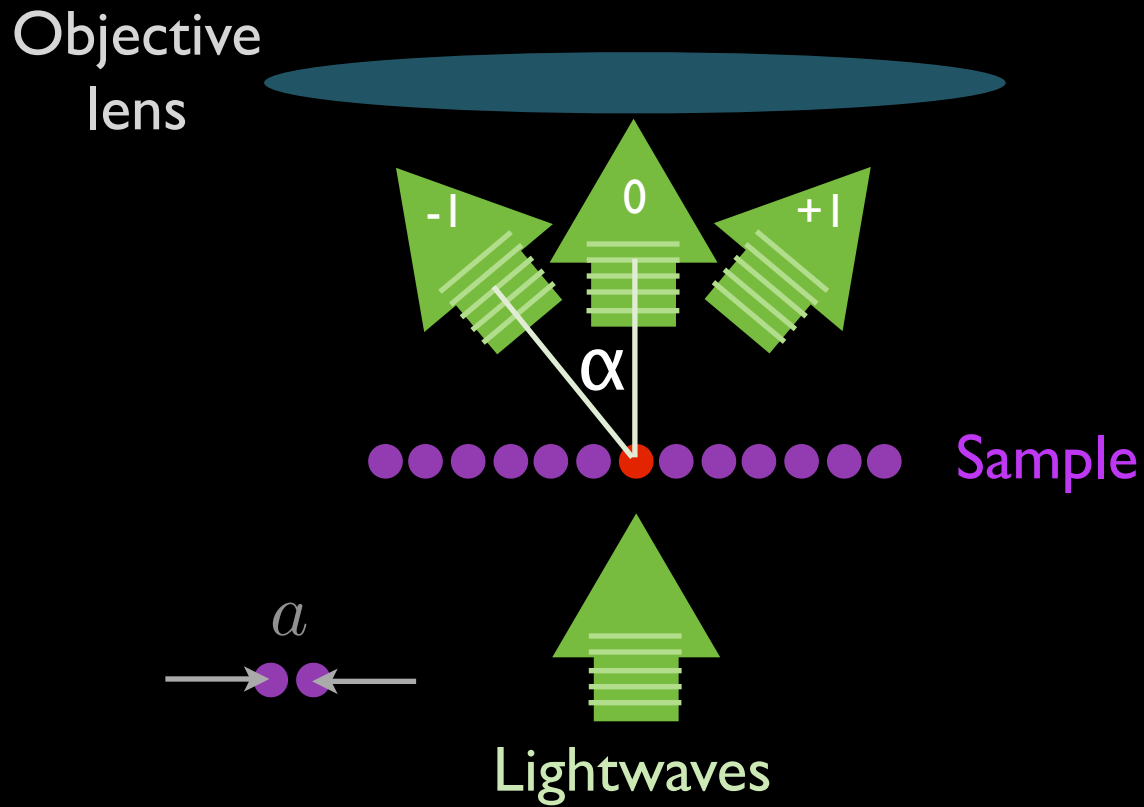


http://de.wikipedia.org/wiki/Ernst_Abbe

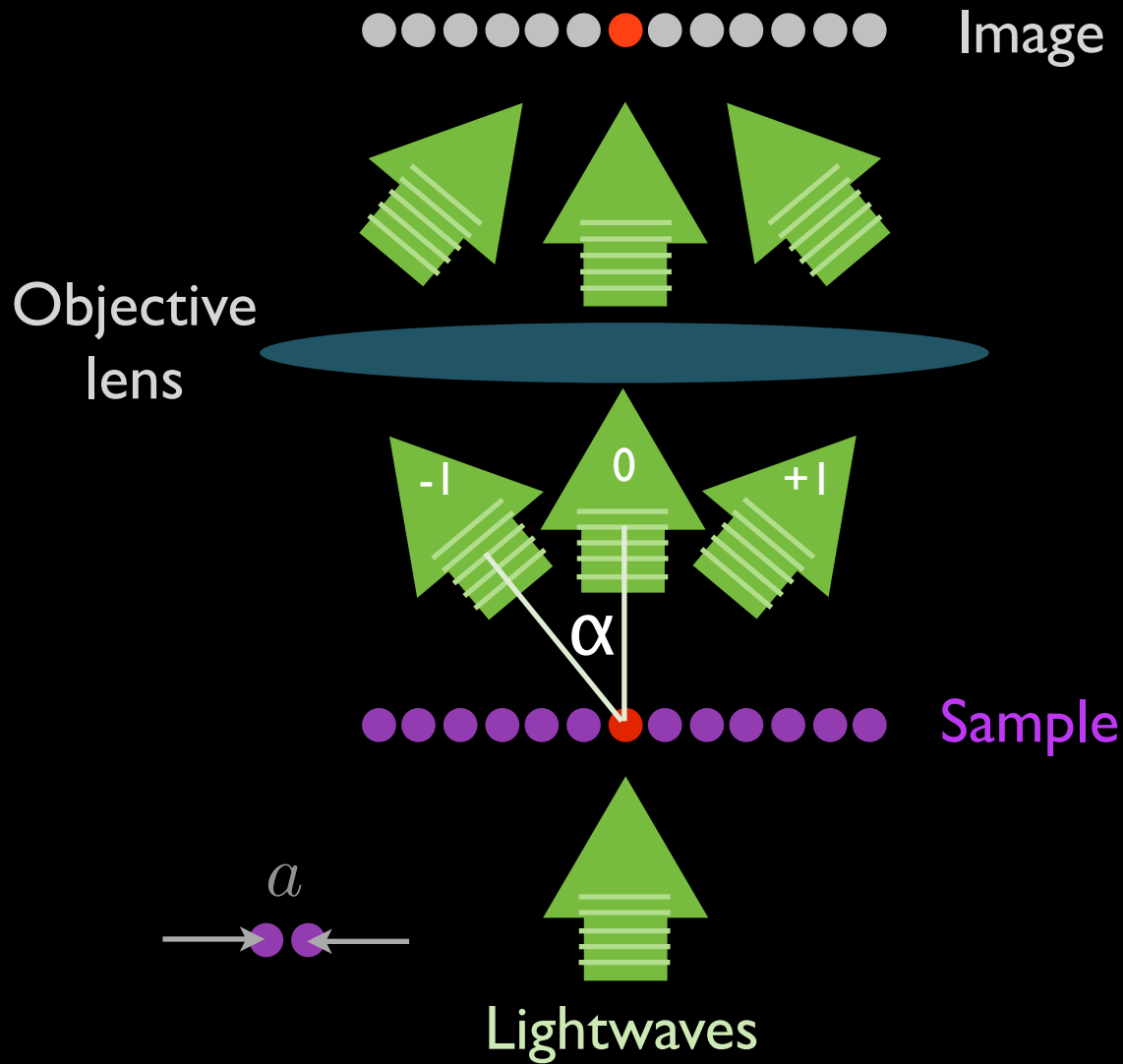
The basic principle: Abbe's view



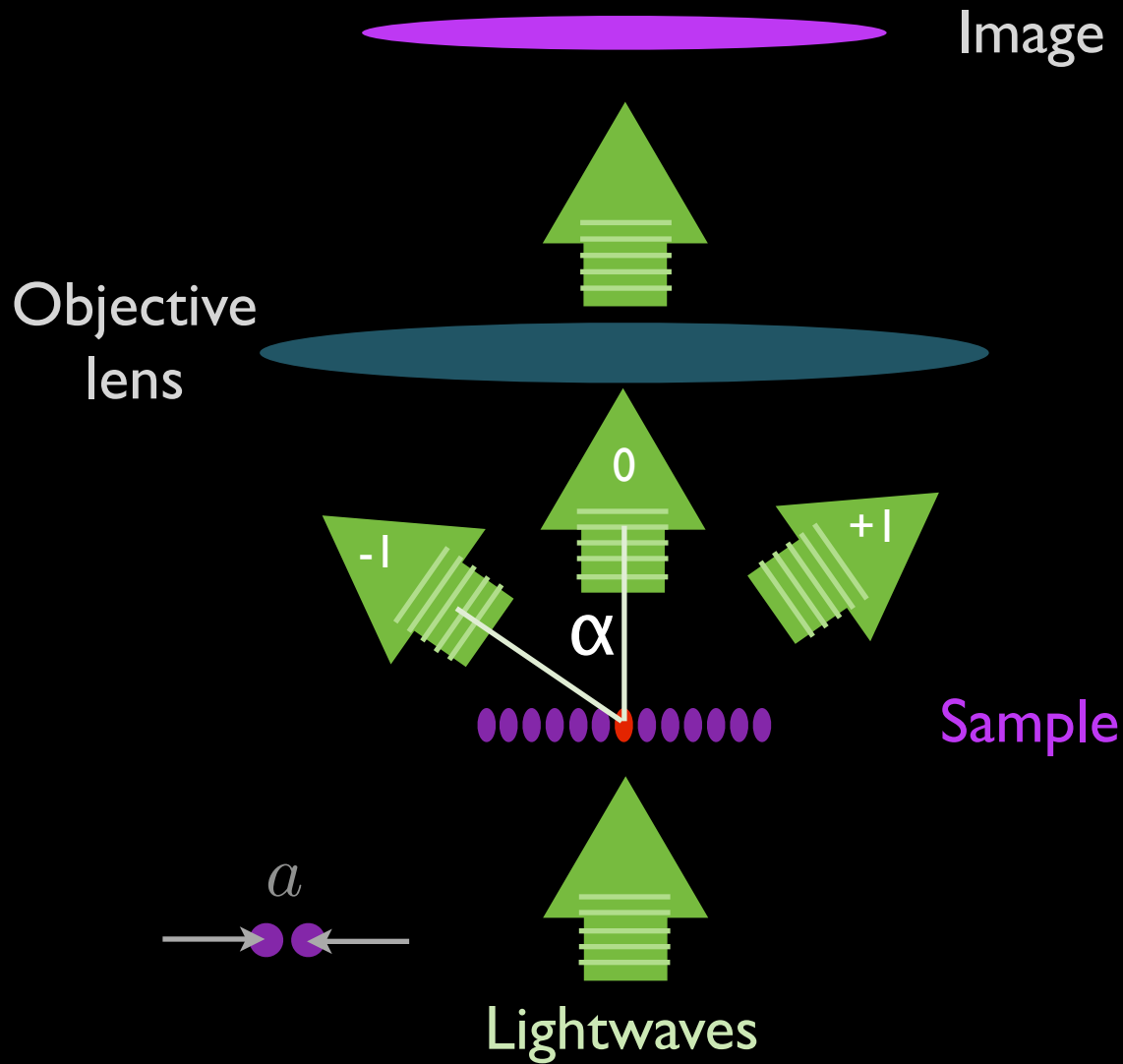
The basic principle: Abbe's view



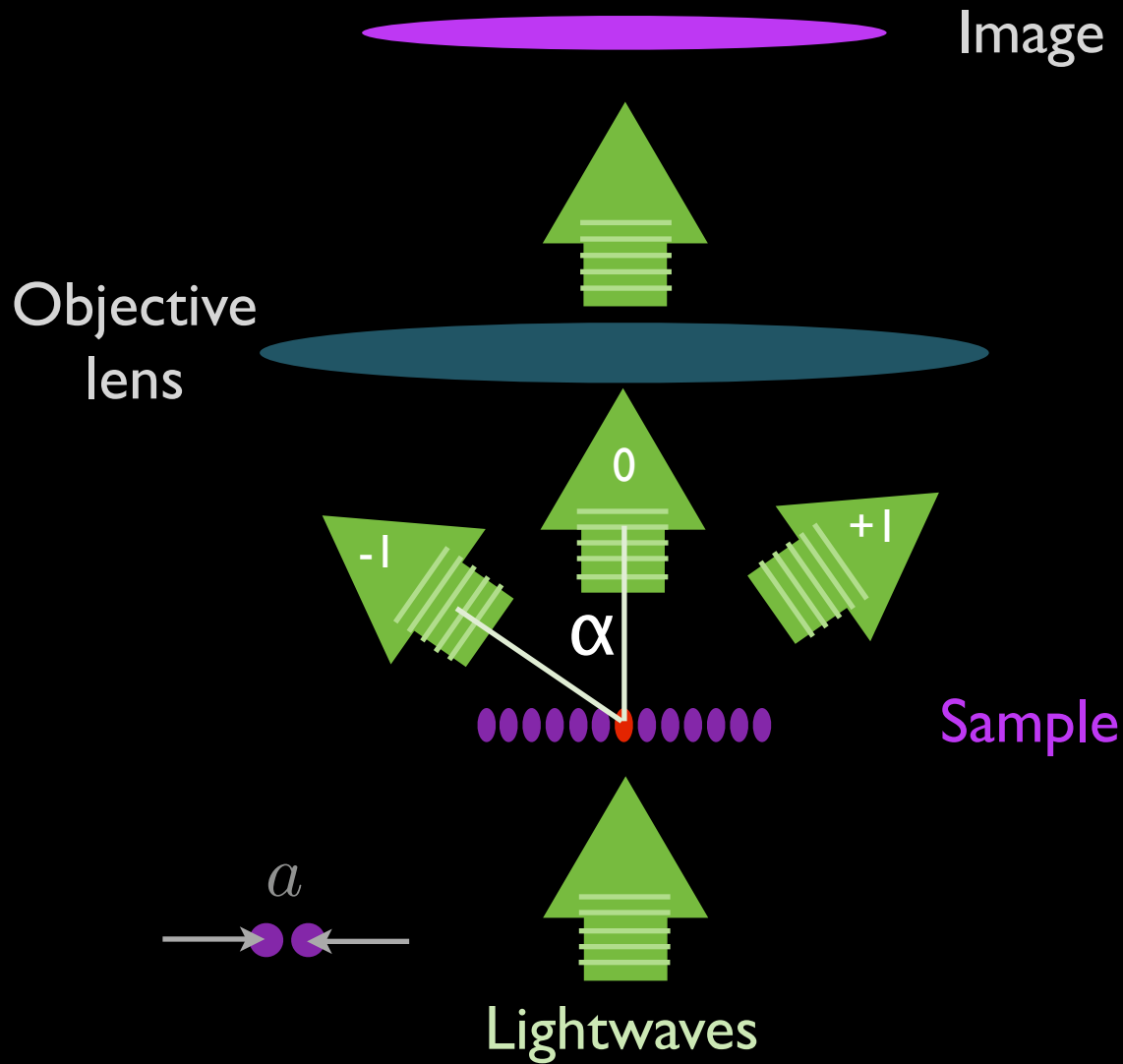
The basic principle: Abbe's view



The basic principle: Abbe's view



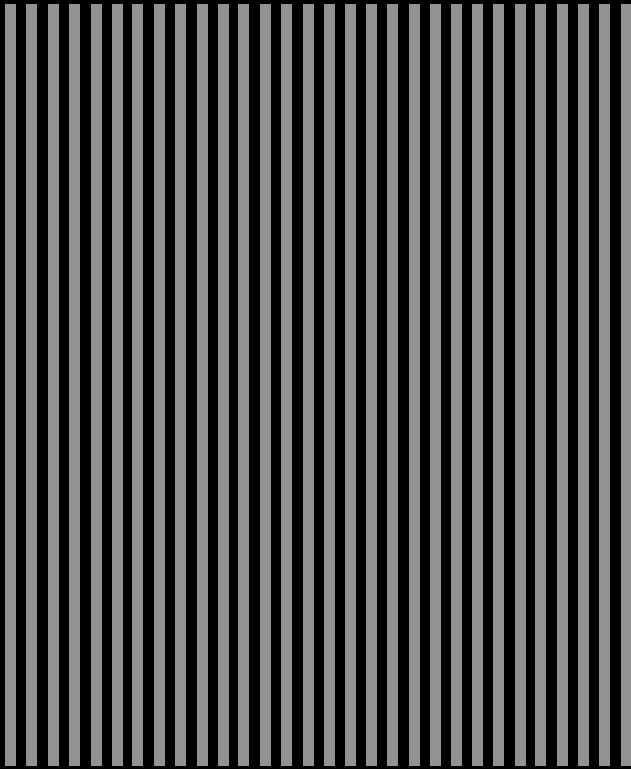
The basic principle: Abbe's view



highest frequencies
(biggest α)
→
smallest structures

The basic SI principle: Moiré fringes

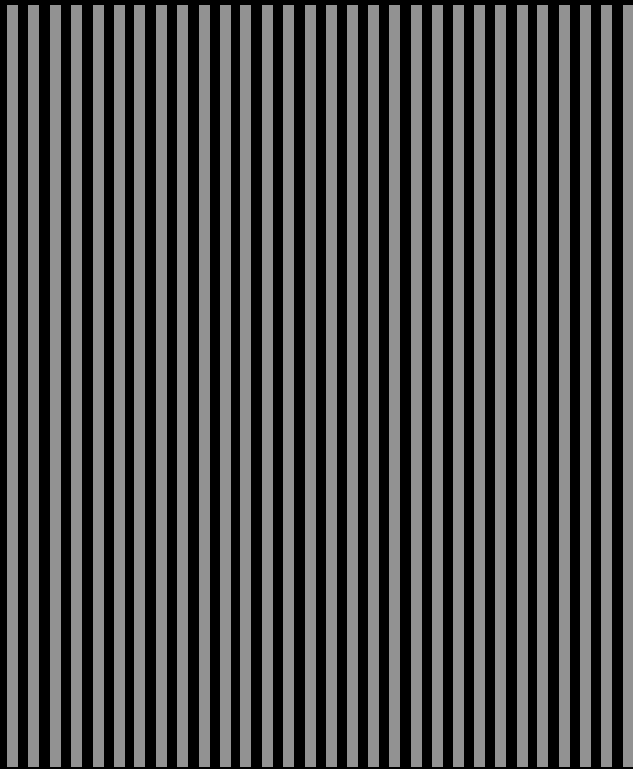
$$f_i = 30 \text{ Stripes} / 300 \text{ Pixels} = 0.1 \text{ S/P}$$



Illumination with known
periodicity

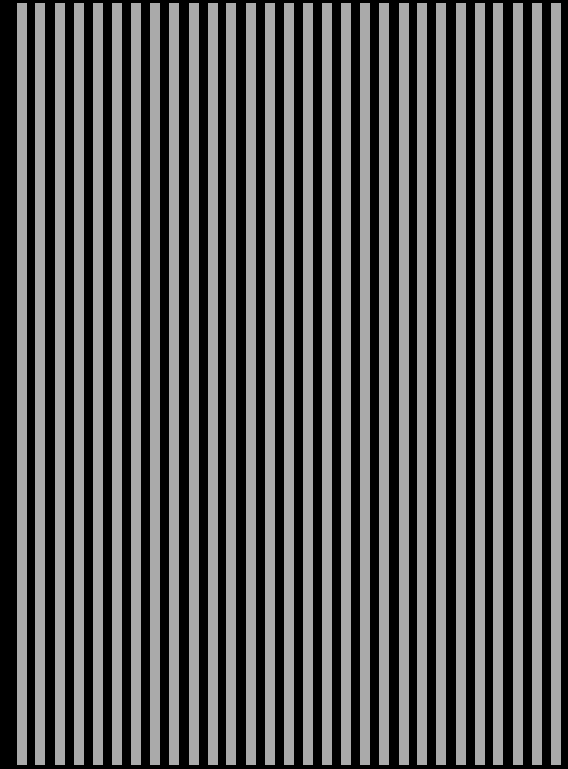
The basic SI principle: Moiré fringes

$$f_1 = 30 \text{ Stripes} / 300 \text{ Pixels} = 0.1 \text{ S/P}$$



Illumination with known
periodicity

$$f_2 = 30 \text{ Stripes} / 270 \text{ Pixels} = 0.11 \text{ S/P}$$



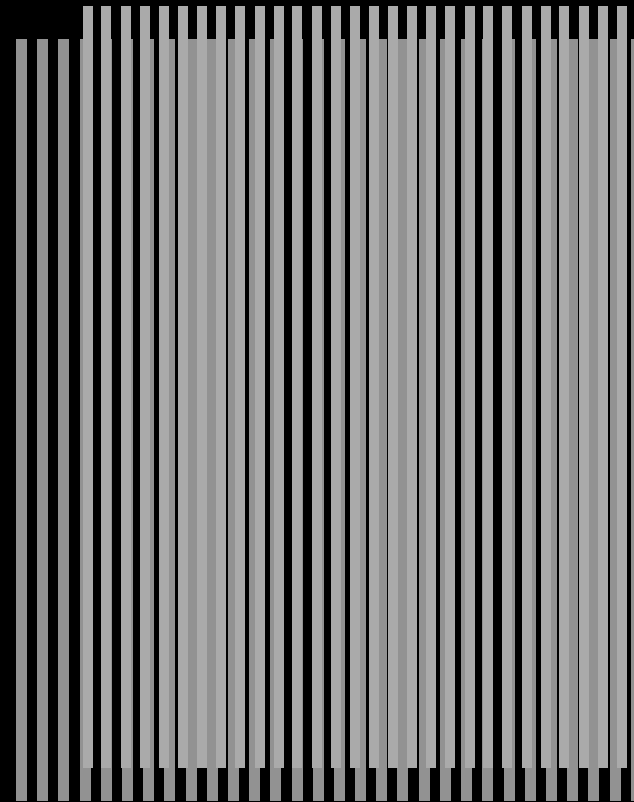
SAMPLE with
“unknown” periodicity

The basic SI principle: Moiré fringes

$$f_1 = 30 \text{ Stripes} / 300 \text{ Pixels} = 0.1 \text{ S/P}$$

$$f_2 = 30 \text{ Stripes} / 270 \text{ Pixels} = 0.11 \text{ S/P}$$

$$\Delta f = 0.01 \text{ S/P}$$



Illumination with known
periodicity

SAMPLE with
“unknown” periodicity

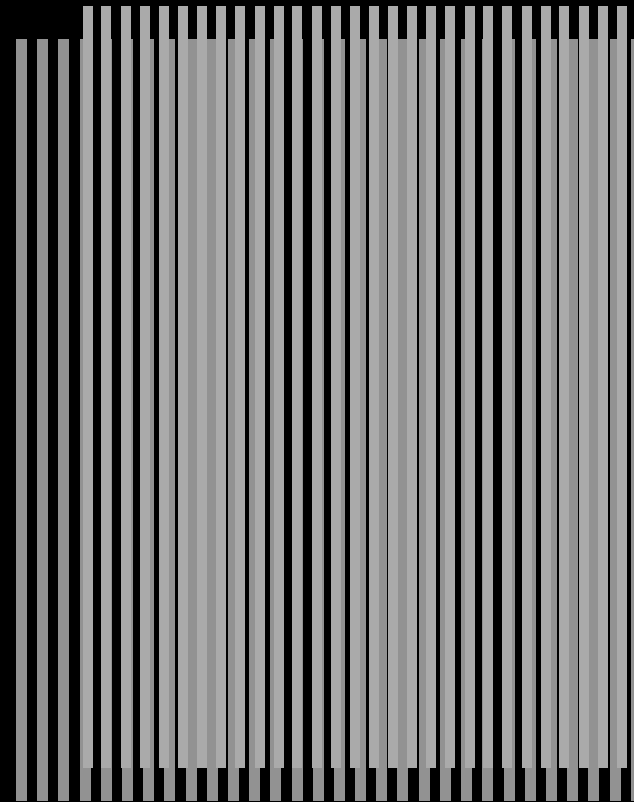
The basic SI principle: Moiré fringes

$$f_1 = 30 \text{ Stripes} / 300 \text{ Pixels} = 0.1 \text{ S/P}$$

$$f_2 = 30 \text{ Stripes} / 270 \text{ Pixels} = 0.11 \text{ S/P}$$

**MOIRE-
PATTERNS** are
generated by
“multiplication”
**SAMPLE
PERIODICITY**
can be calculated!

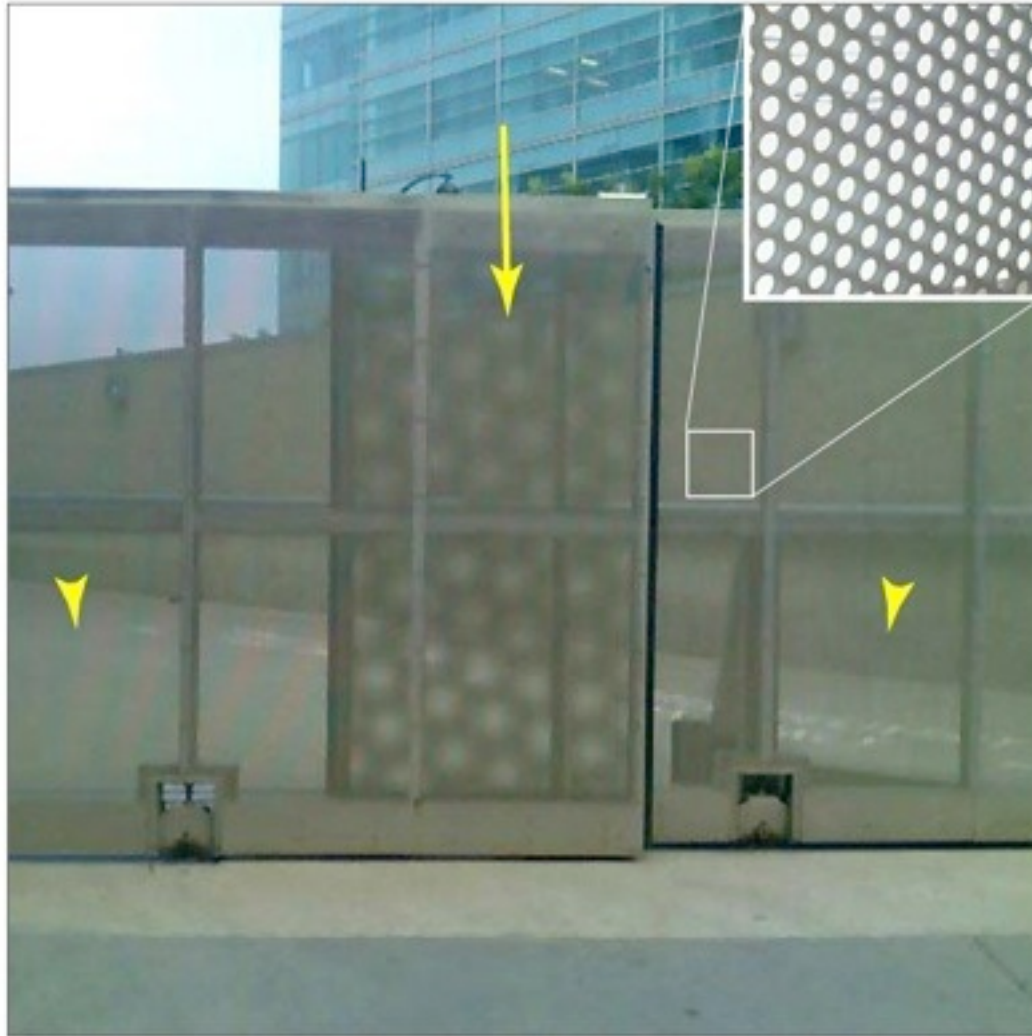
$$\Delta f = 0.011 \text{ S/P}$$



Illumination with known
periodicity

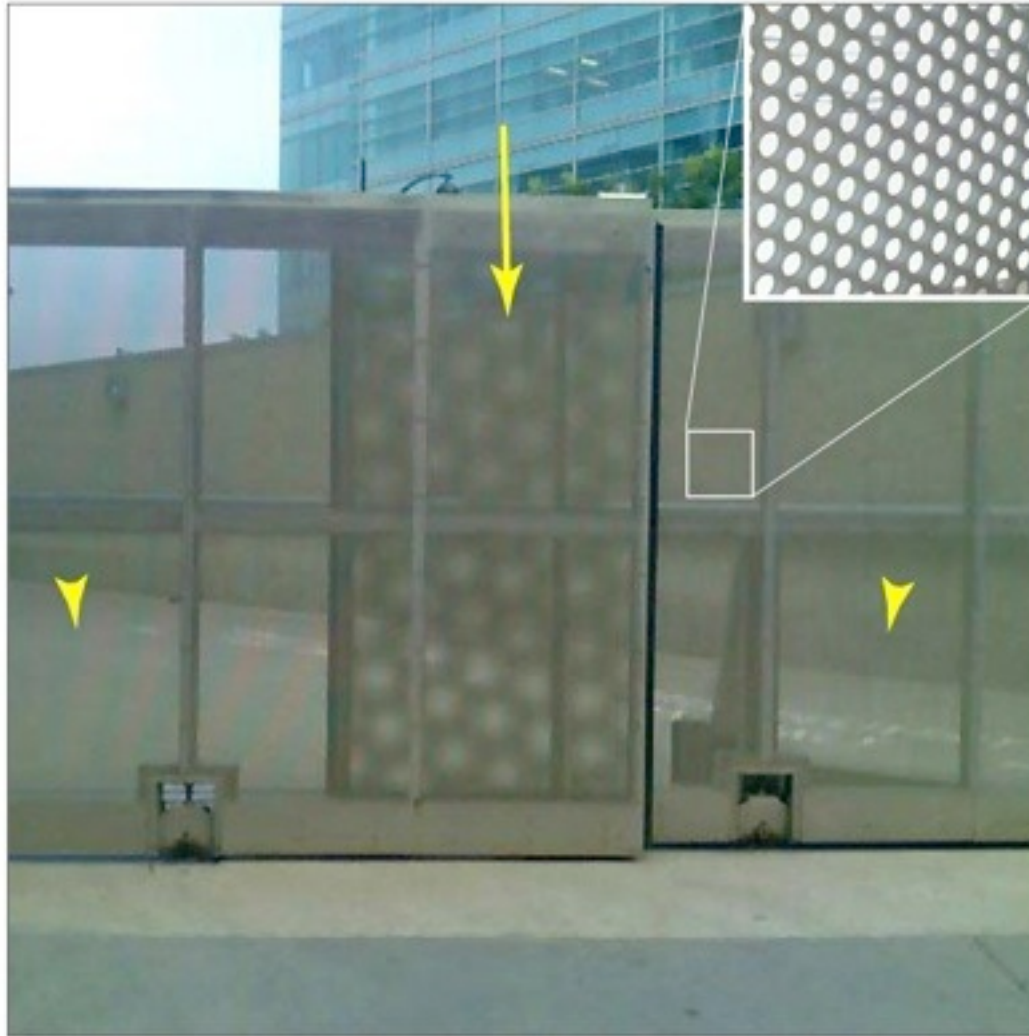
SAMPLE with
“unknown” periodicity

The basic SI principle: Moiré fringes



high frequency information is shifted/encoded to a lower frequency, that can be resolved.

The basic SI principle: Moiré fringes



high frequency information is shifted/encoded to a lower frequency, that can be resolved.

Fourier transform of the measured image

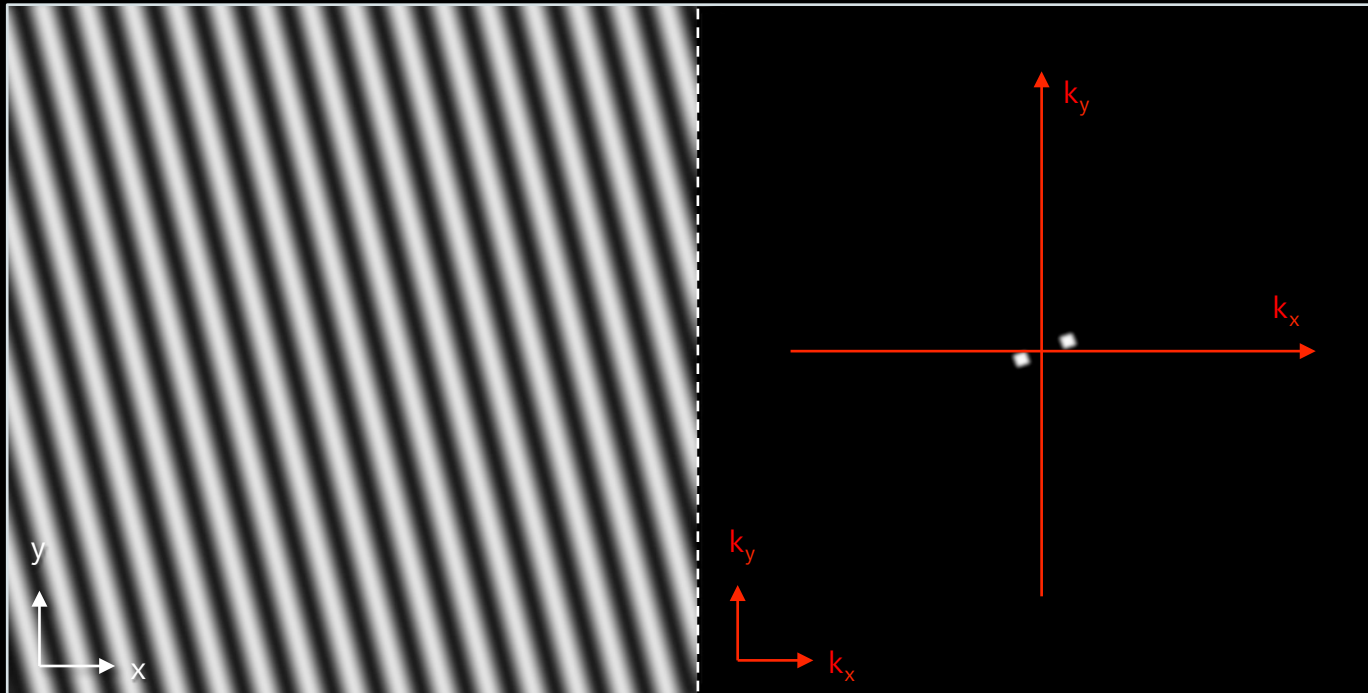
unknown structure

$$F\{f \times g\} = F\{f\} \otimes F\{g\} \longrightarrow F\{f\} = F\{f \times g\} \otimes^{-1} F\{g\}$$

known illumination function

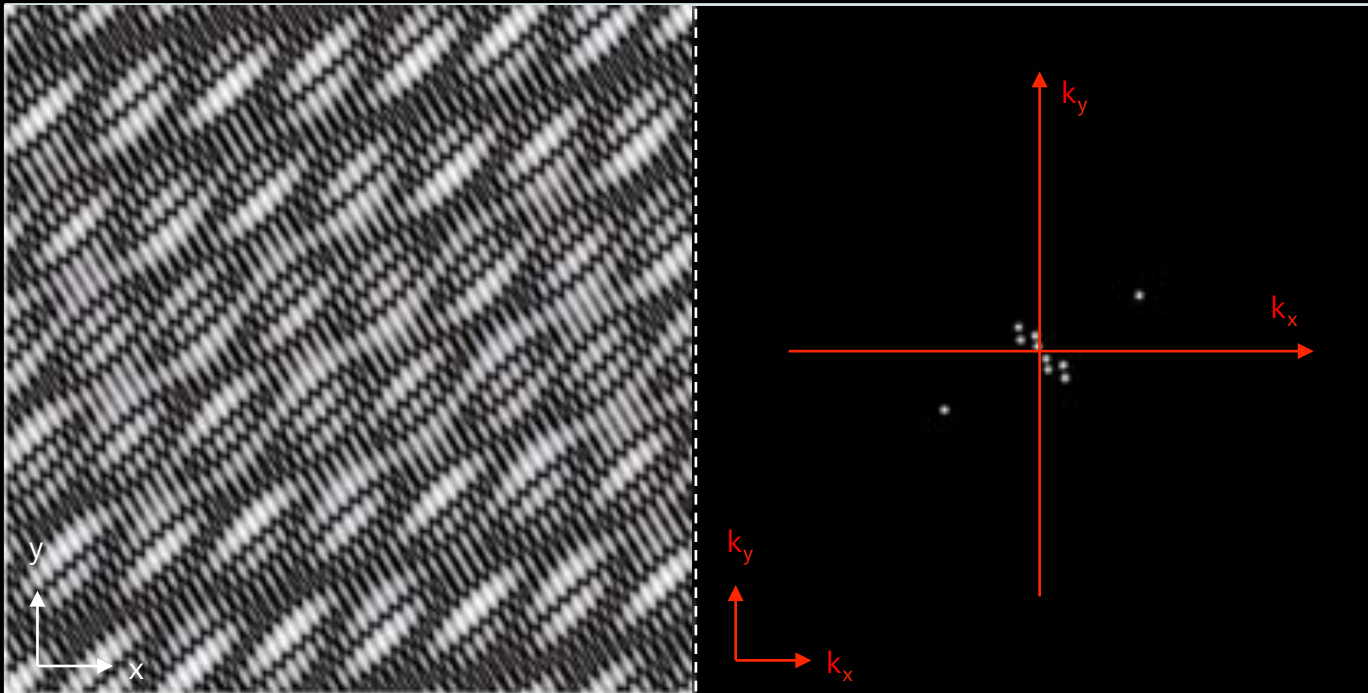
SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space

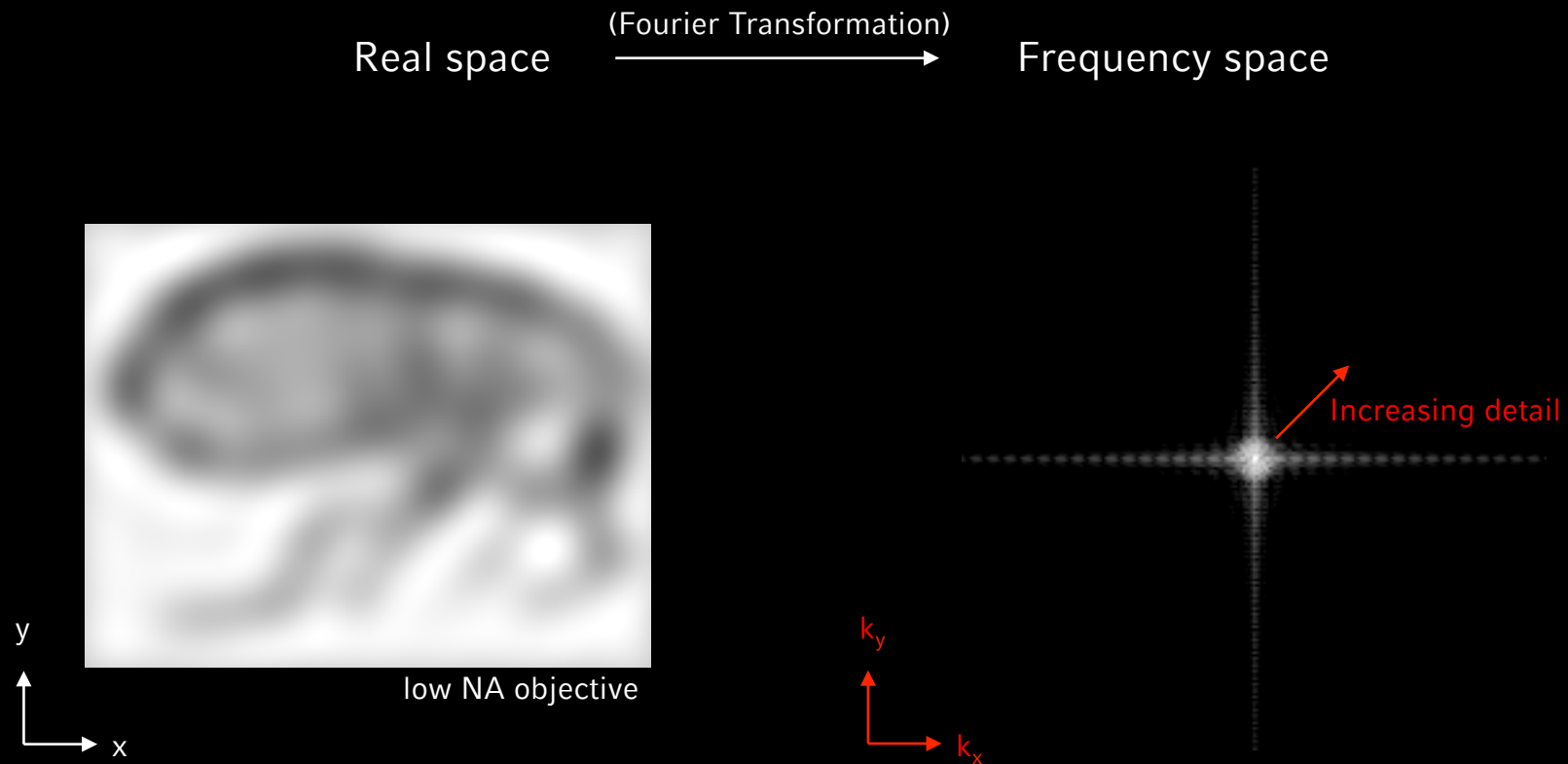


SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space

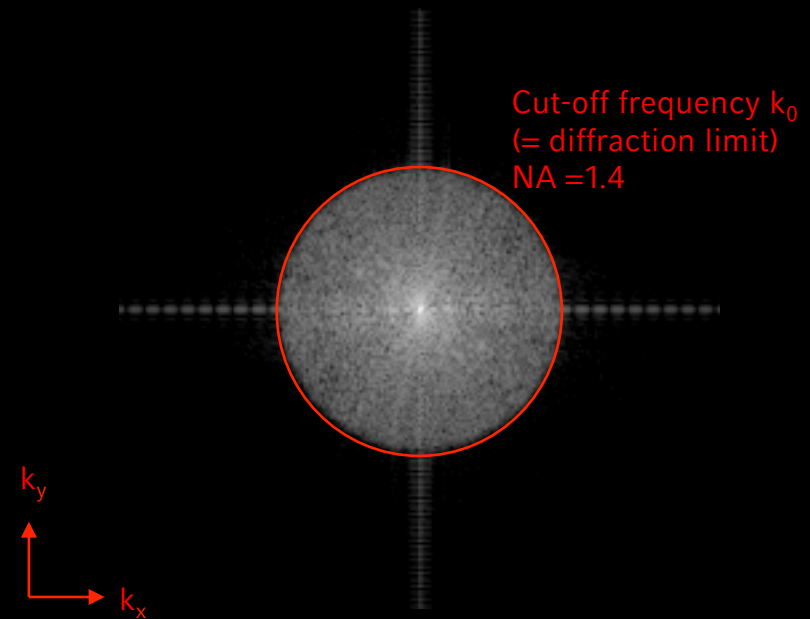


SI image reconstruction in Fourier space



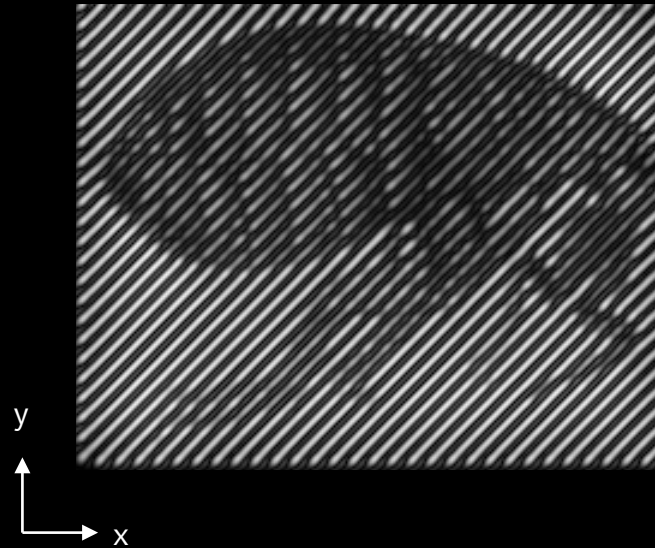
SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space

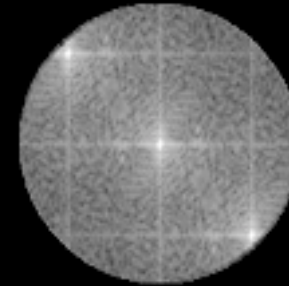


SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space

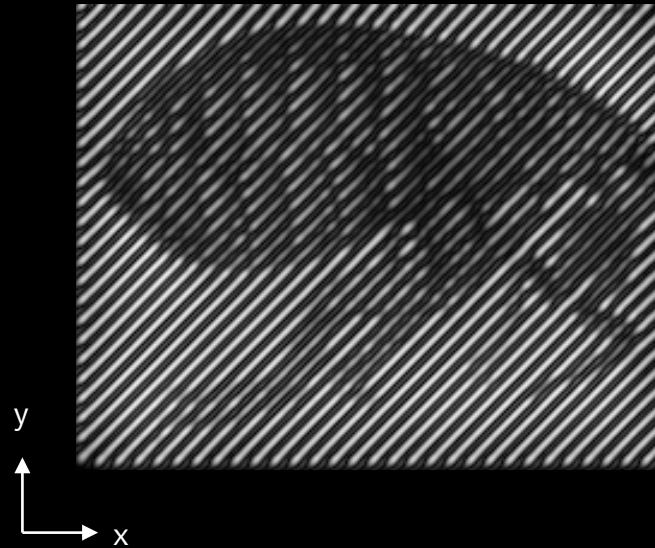


Illumination with known
periodicity

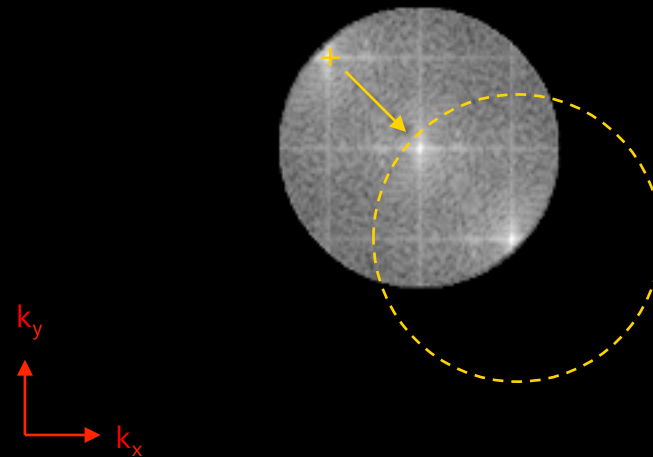


SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space

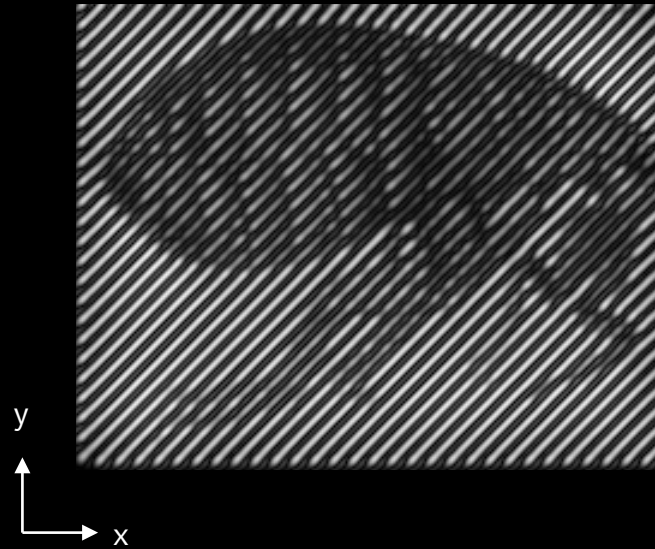


Illumination with known periodicity

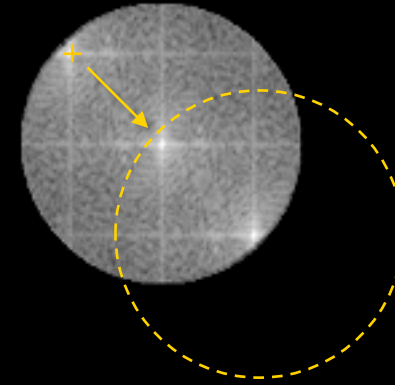


SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space



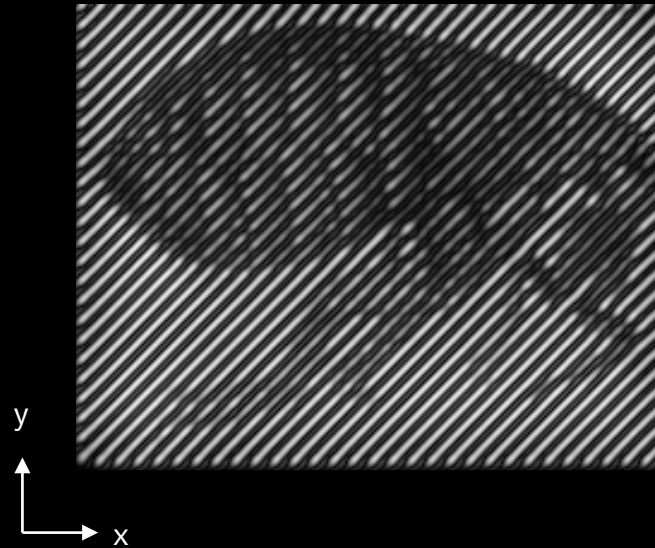
Illumination with known periodicity



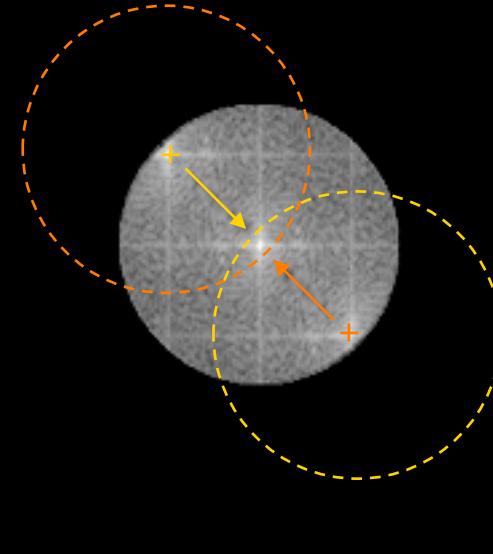
“New” information is generated...

SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space



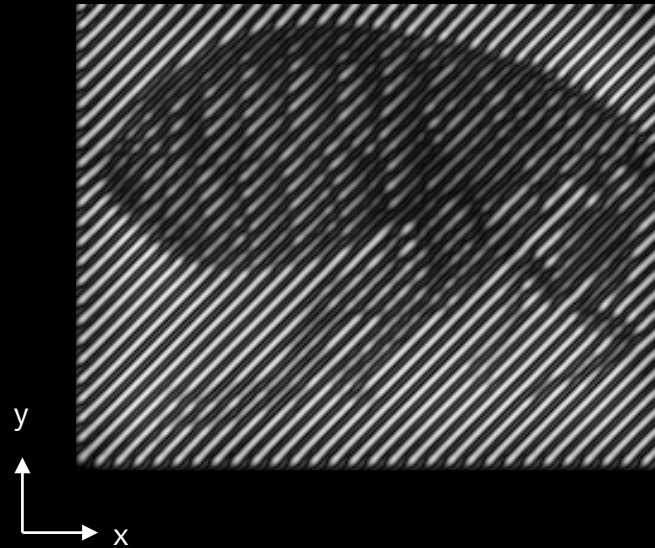
Illumination with known periodicity



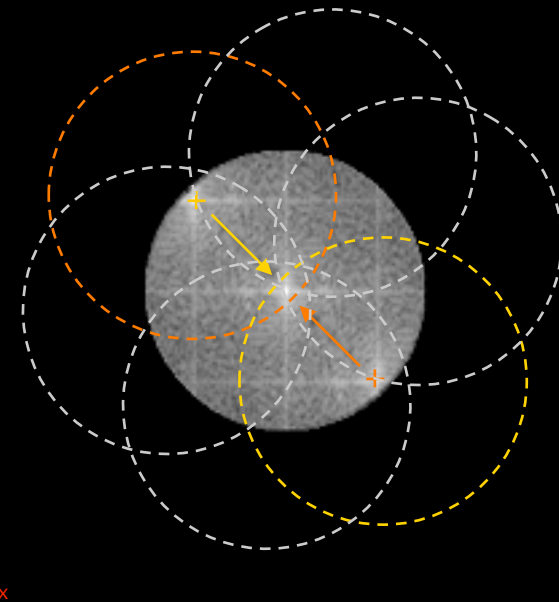
“New” information is generated...

SI image reconstruction in Fourier space

Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space



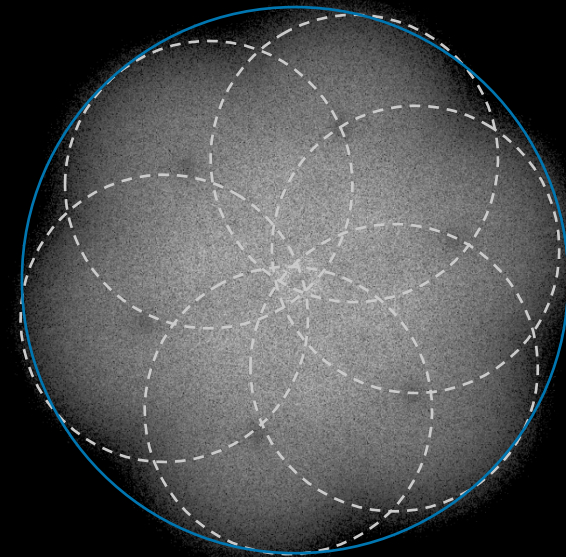
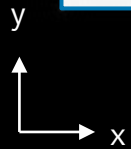
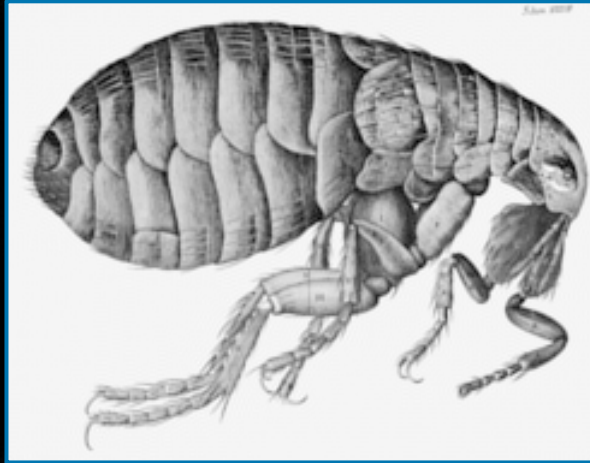
Illumination with known periodicity



“New” information is generated...

SI image reconstruction in Fourier space

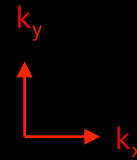
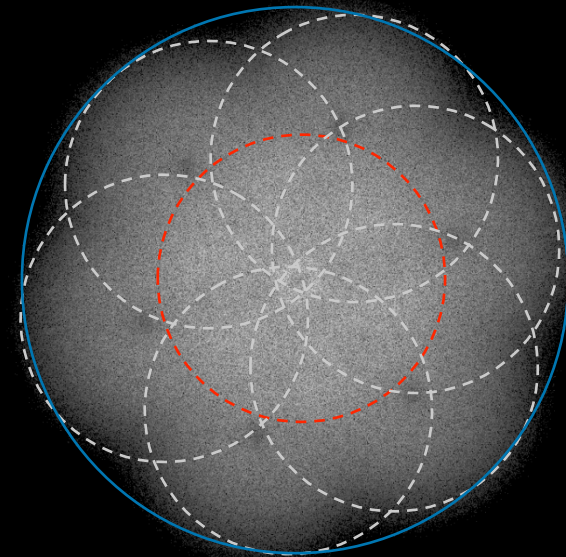
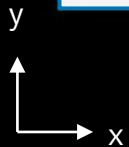
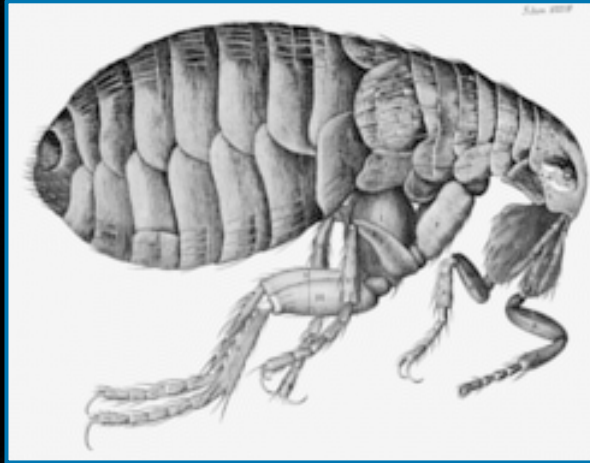
Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space
 $\xleftarrow{\text{(reverse FT)}}$



Equivalent to $NA=2.35$

SI image reconstruction in Fourier space

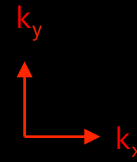
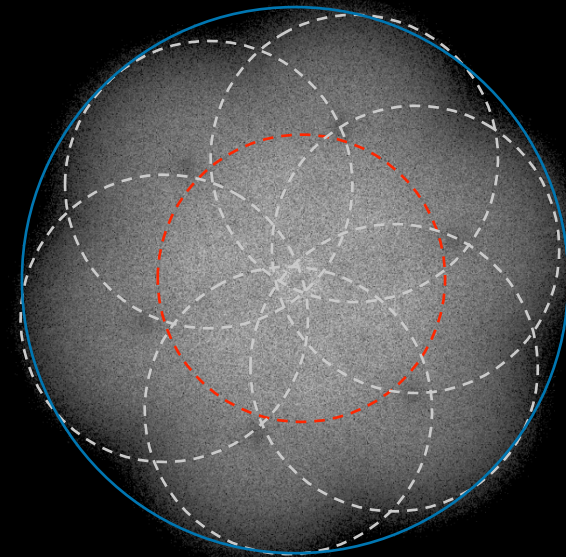
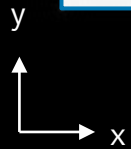
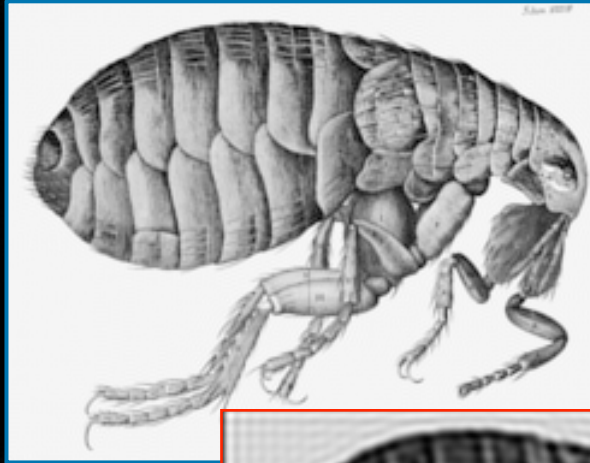
Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space
 $\xleftarrow{\text{(reverse FT)}}$



Equivalent to NA=2.35

SI image reconstruction in Fourier space

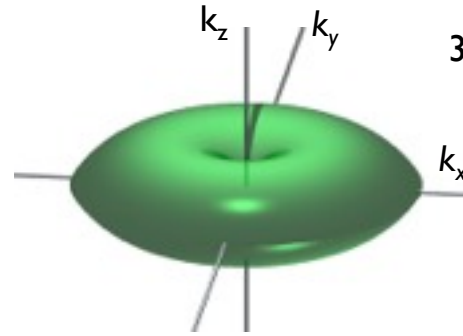
Real space $\xrightarrow{\text{(Fourier Transformation)}}$ Frequency space
 $\xleftarrow{\text{(reverse FT)}}$



Equivalent to $NA=2.35$

Support in 3D-frequency space

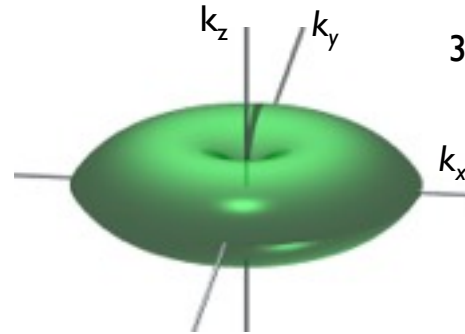
Widefield illumination



3D rendering illustrates cut-off frequency
(= Resolution limit)

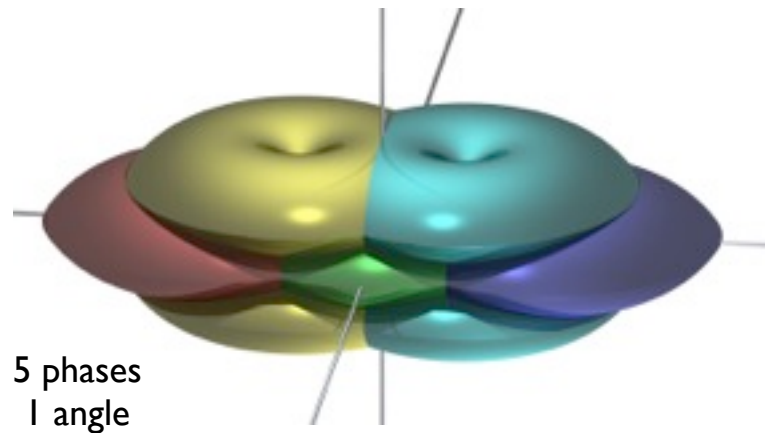
Support in 3D-frequency space

Widefield illumination

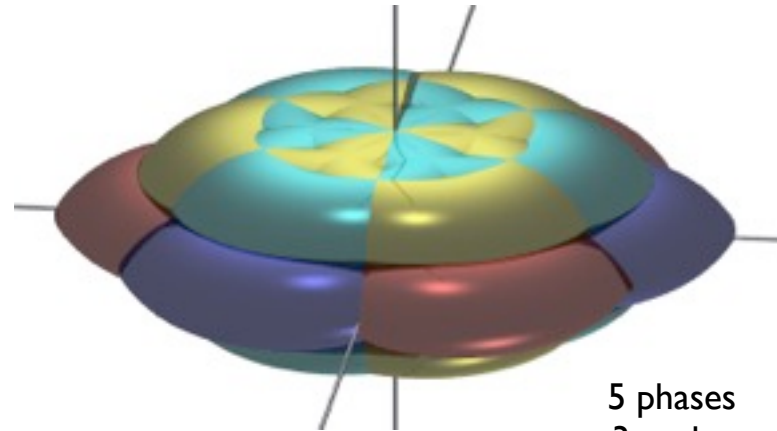


3D rendering illustrates cut-off frequency
(= Resolution limit)

3D Structured illumination



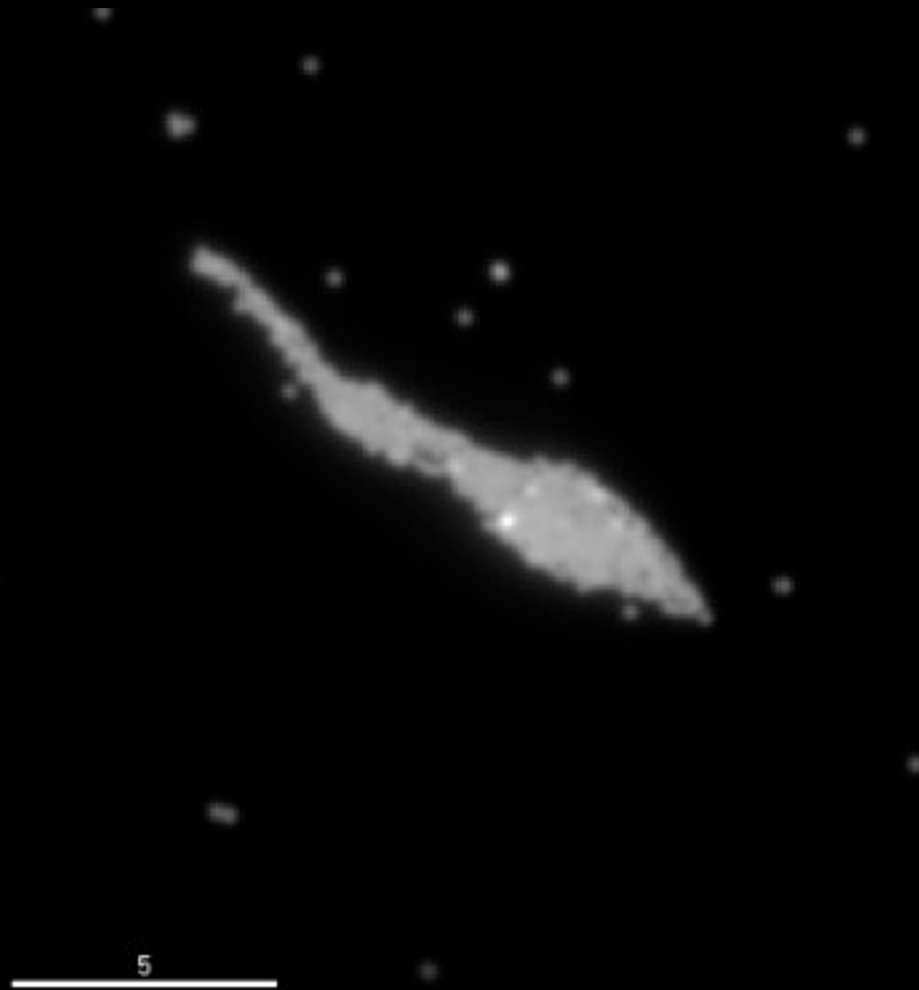
5 phases
1 angle



5 phases
3 angles

**Filling of “missing cone” -> z-sectioning
2x higher lateral and axial resolution**

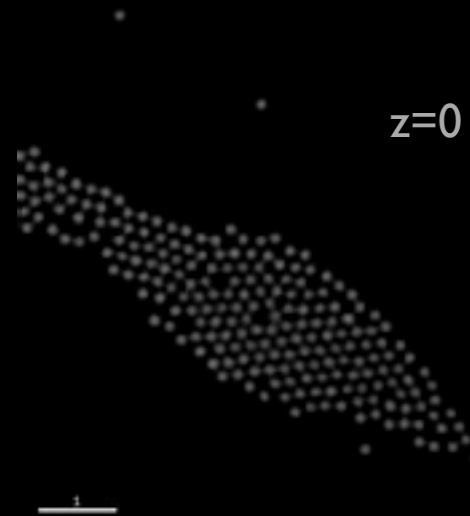
Example: 170 nm PS-Beads



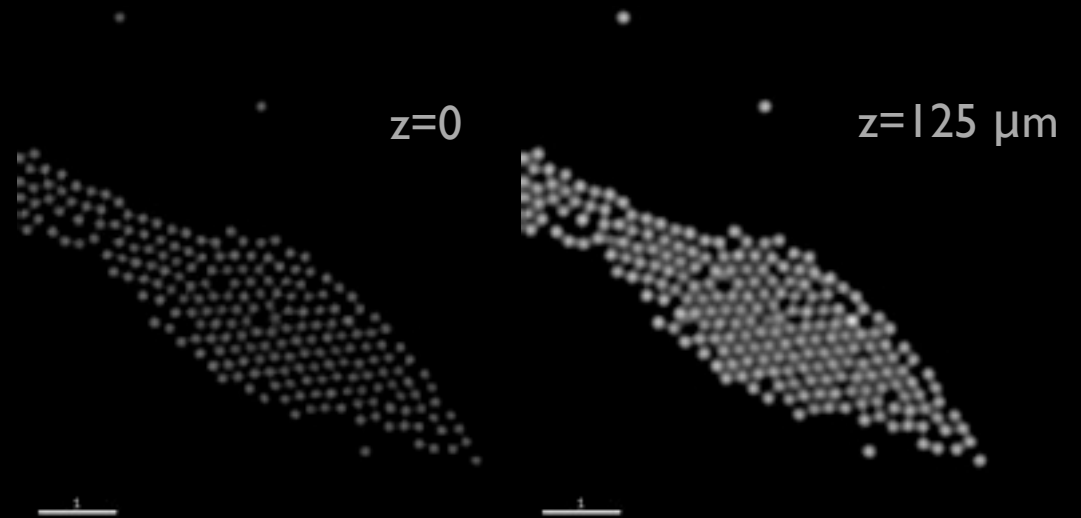
Example: 170 nm PS-Beads



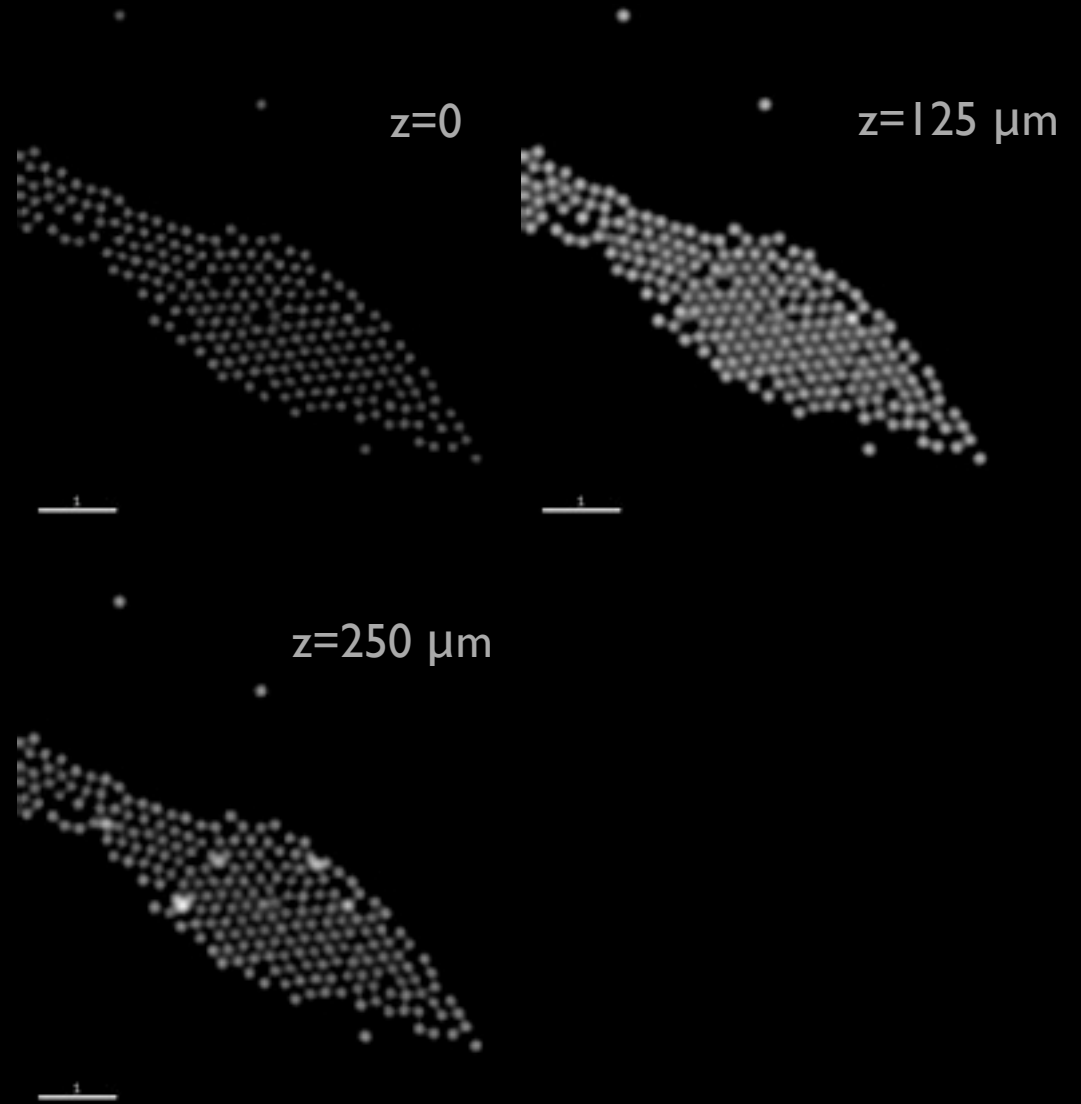
170 nm PS-Beads



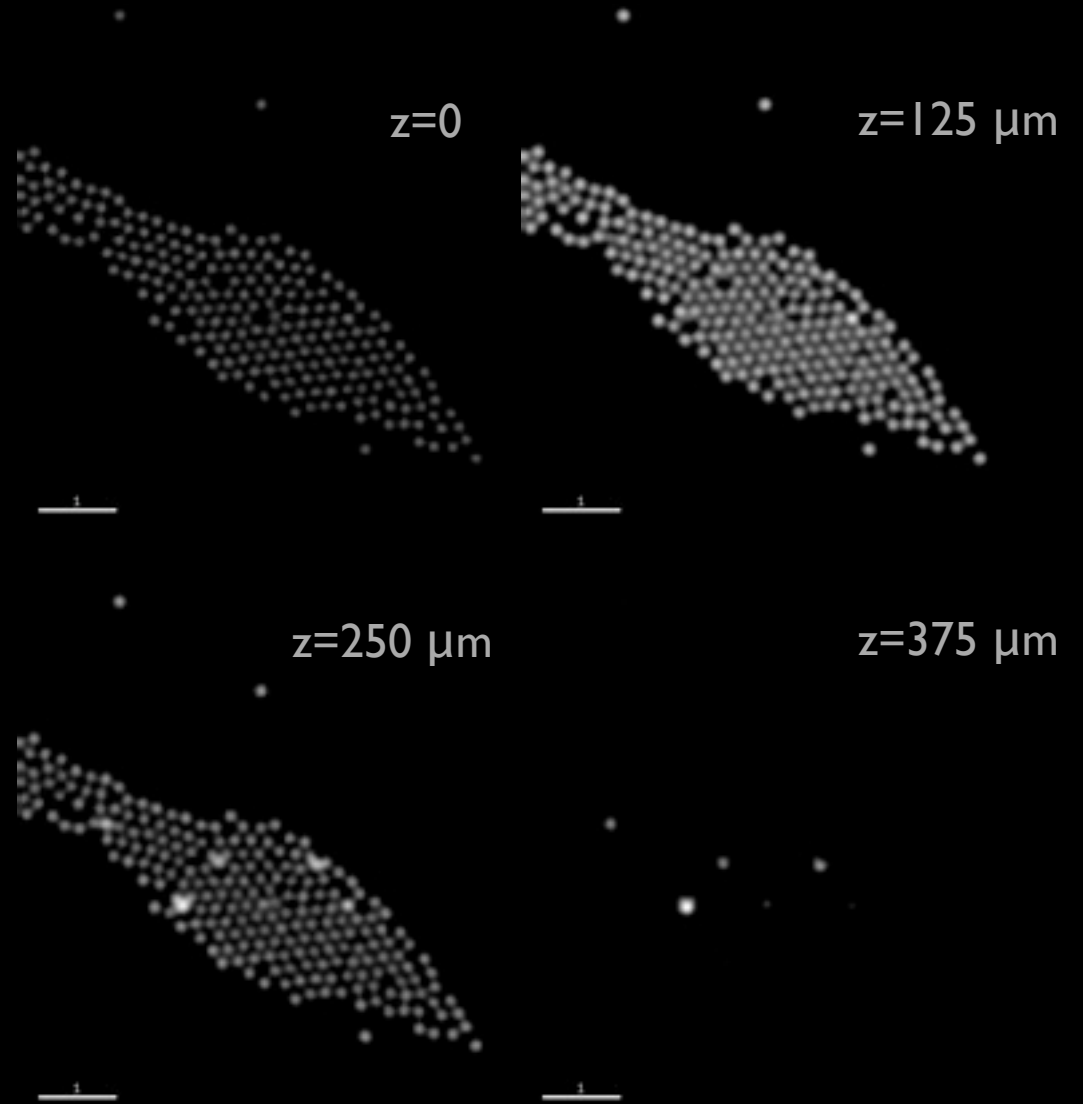
170 nm PS-Beads



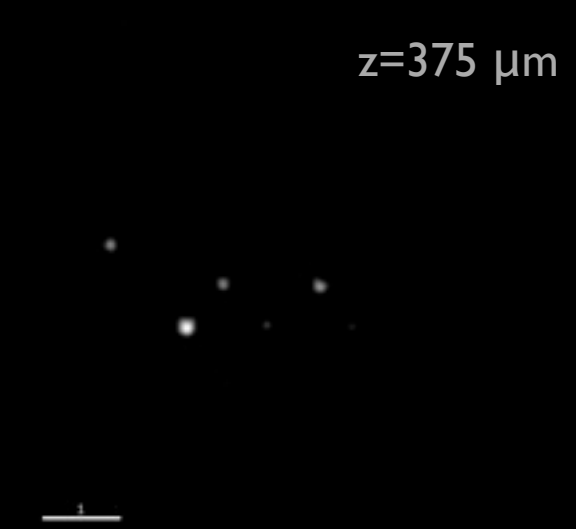
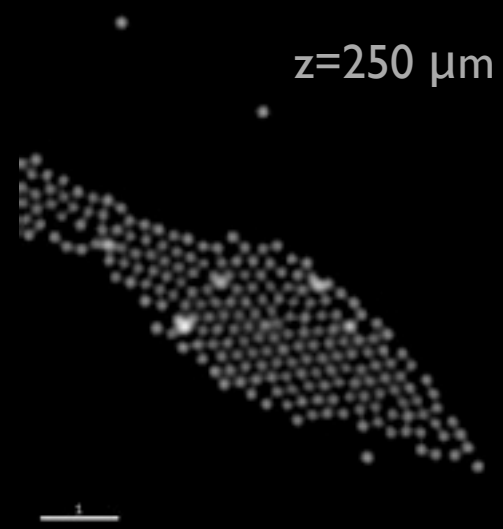
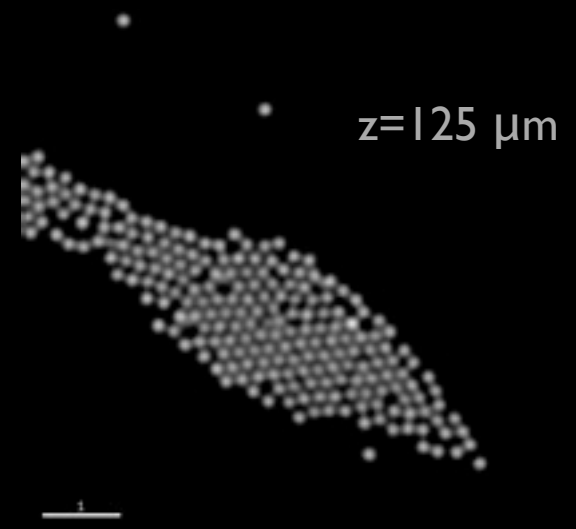
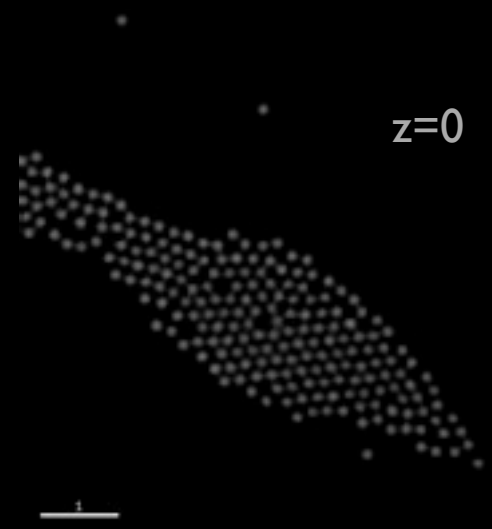
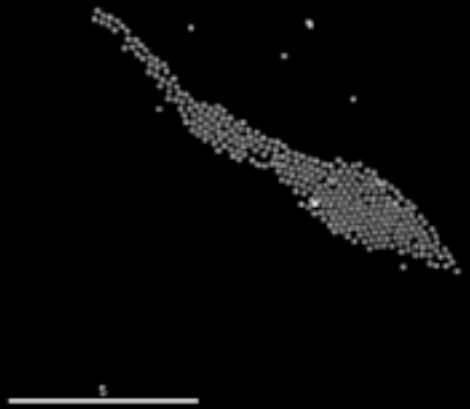
170 nm PS-Beads



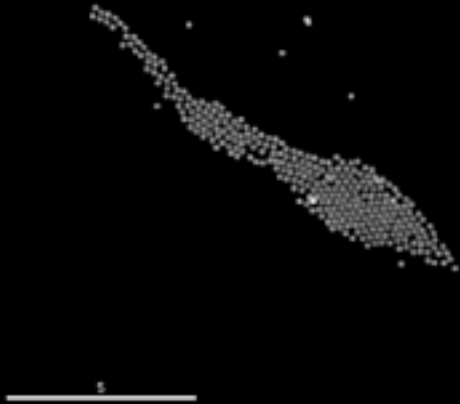
170 nm PS-Beads



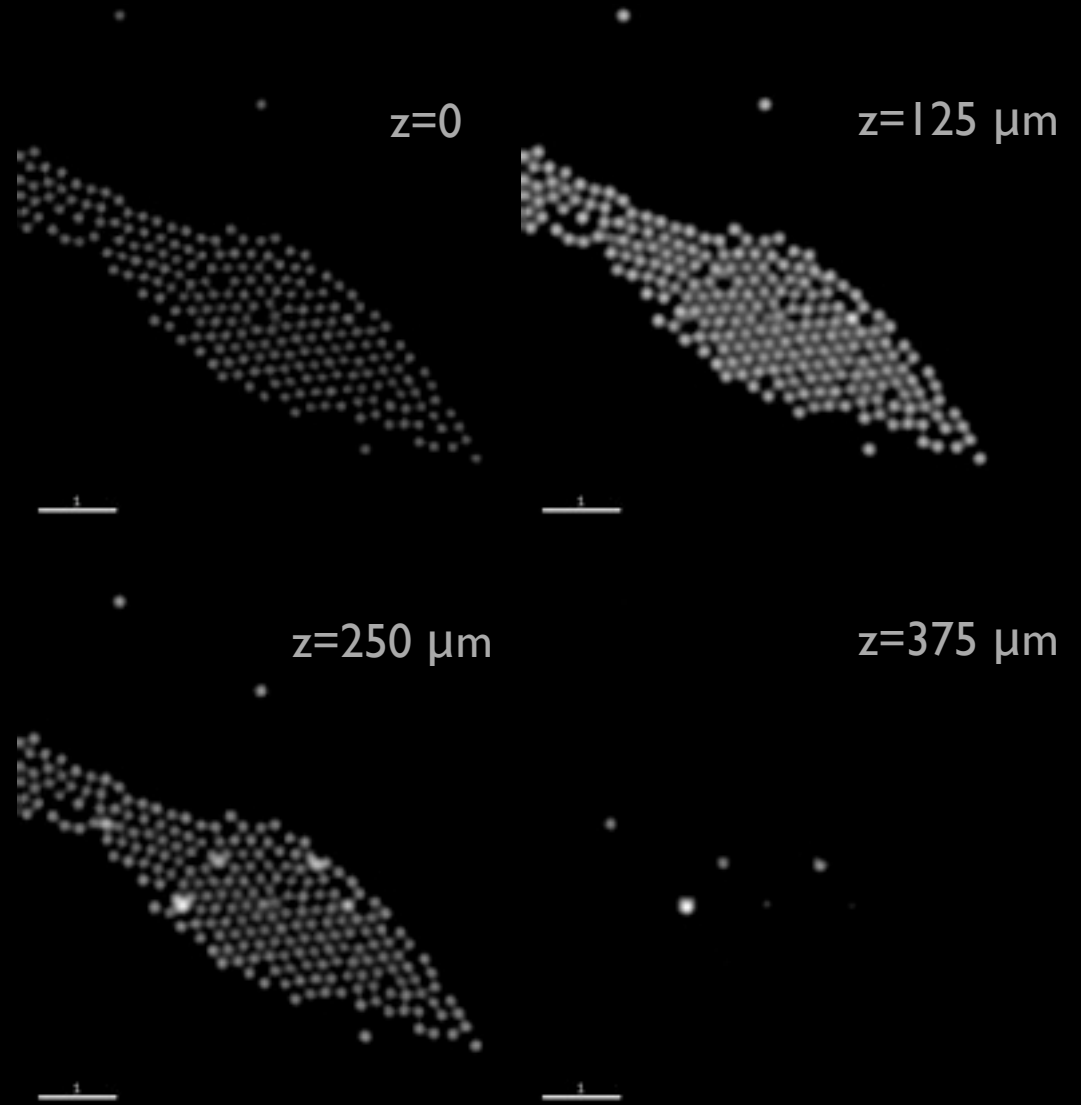
170 nm PS-Beads



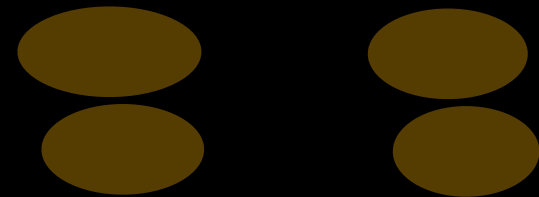
170 nm PS-Beads



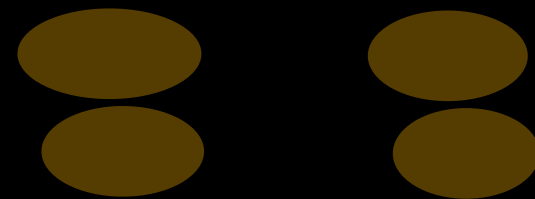
High sectioning quality!



What could this be?

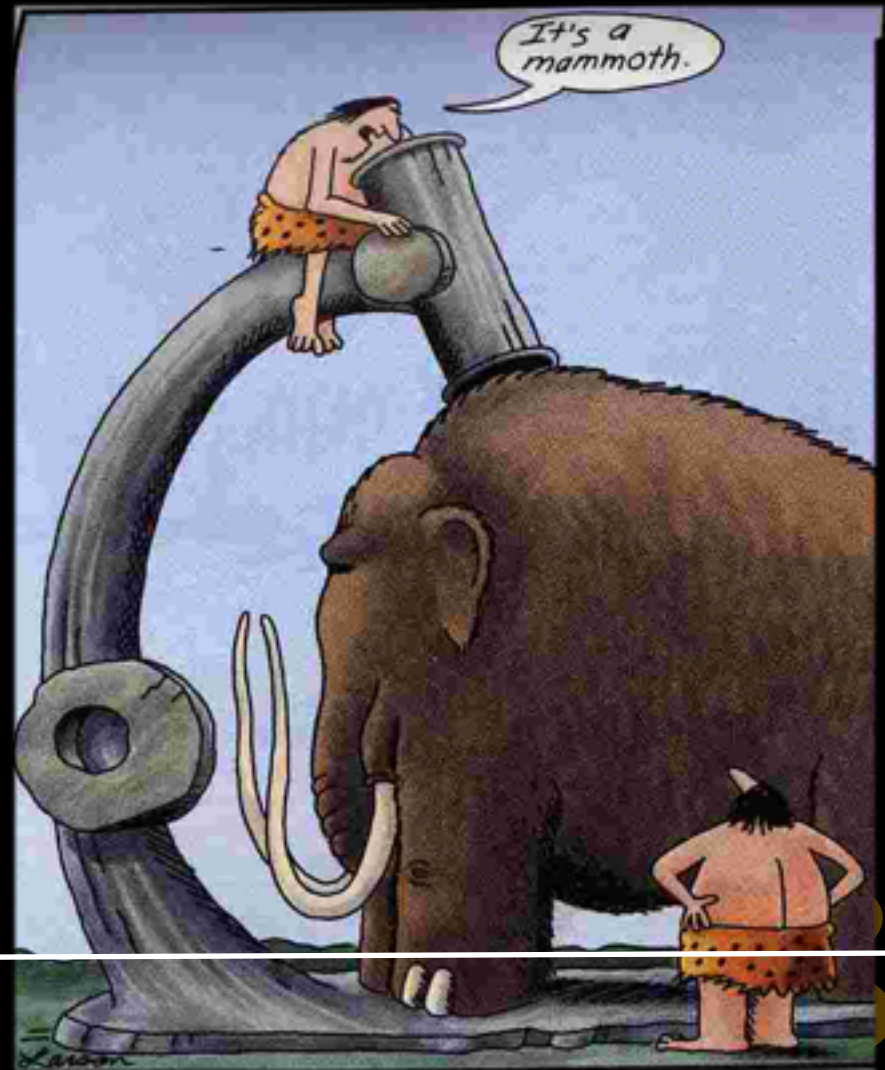


What could this be?



3D information (z-res., optical sectioning, z-depth) !

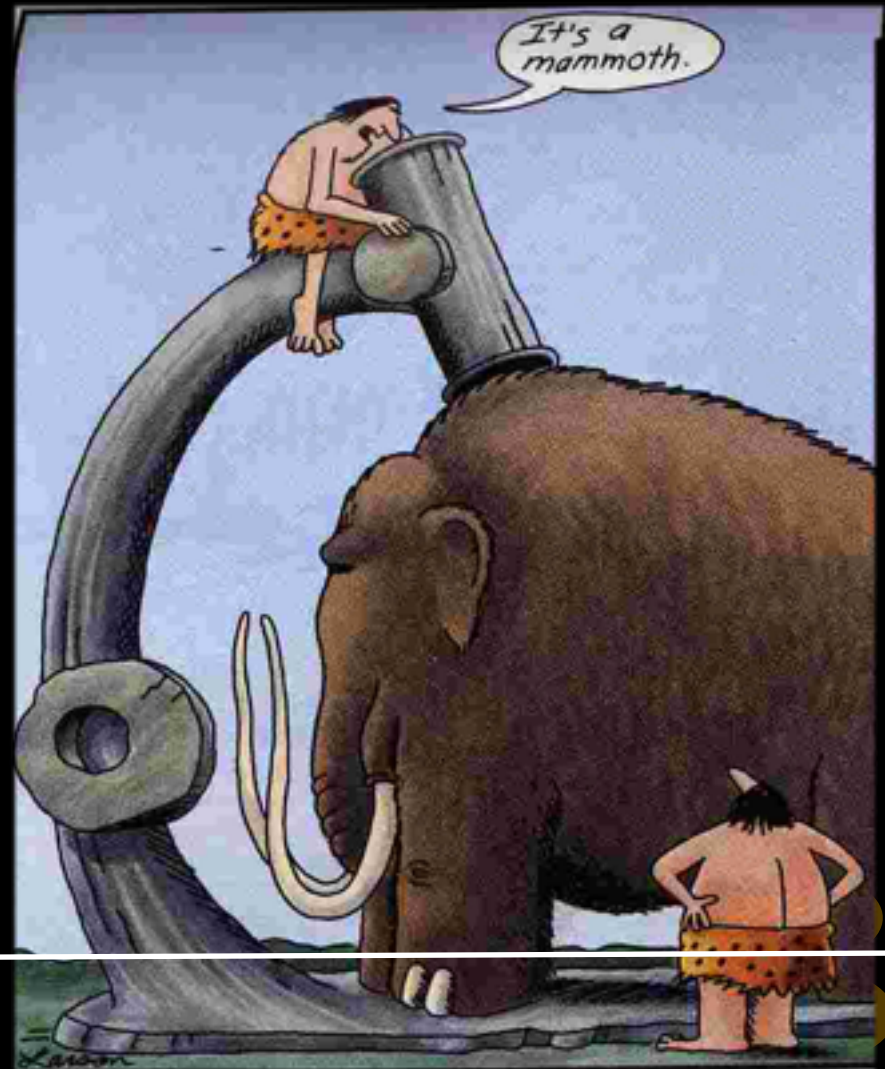
What could this be?



3D information (z-res., optical sectioning, z-depth) !

Not only resolution but also context matters! (I)

What could this be?

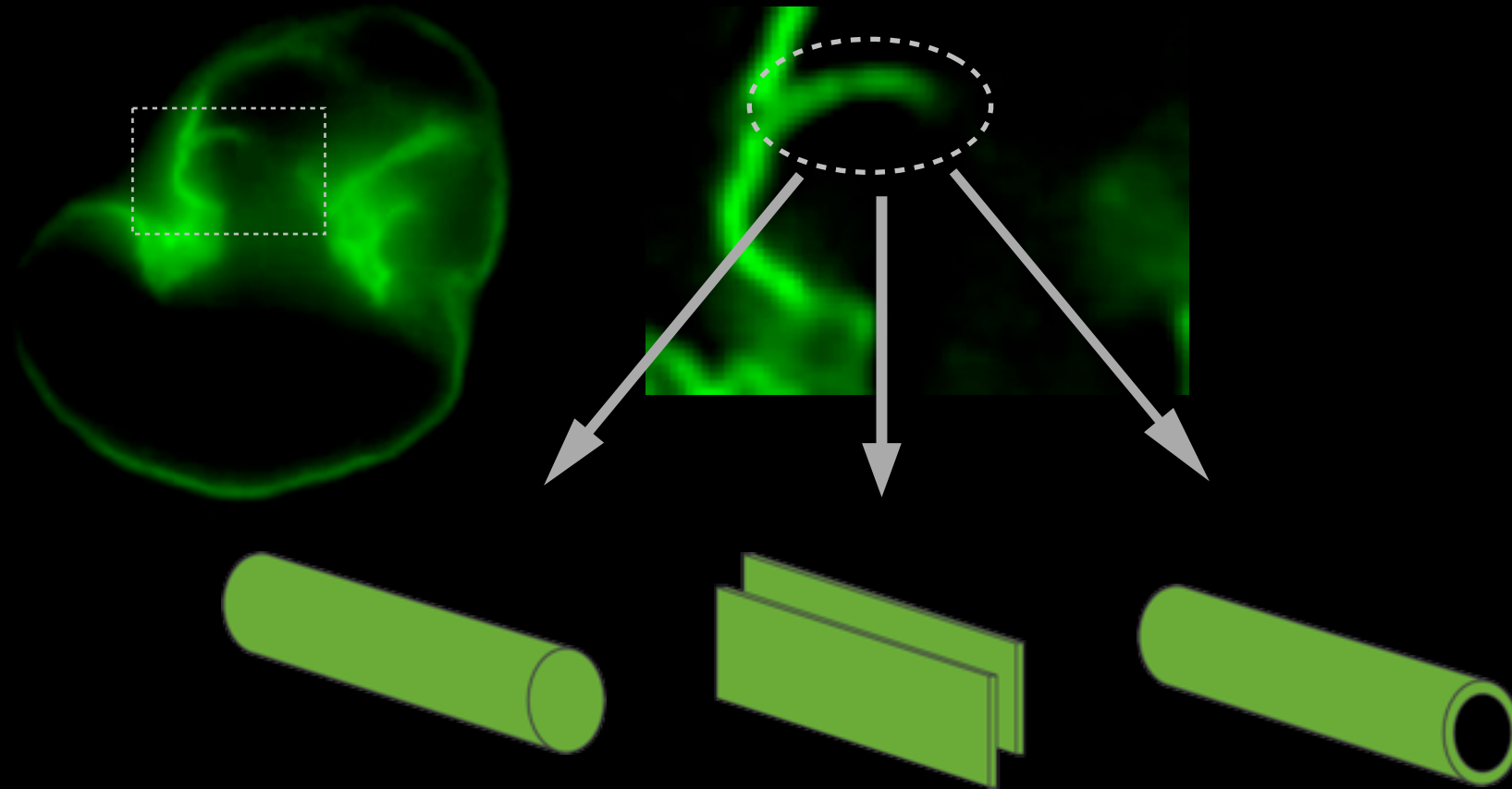


3D information (z-res., optical sectioning, z-depth) !

Not only resolution but also context matters! (III)

Wide-field

Lamin B



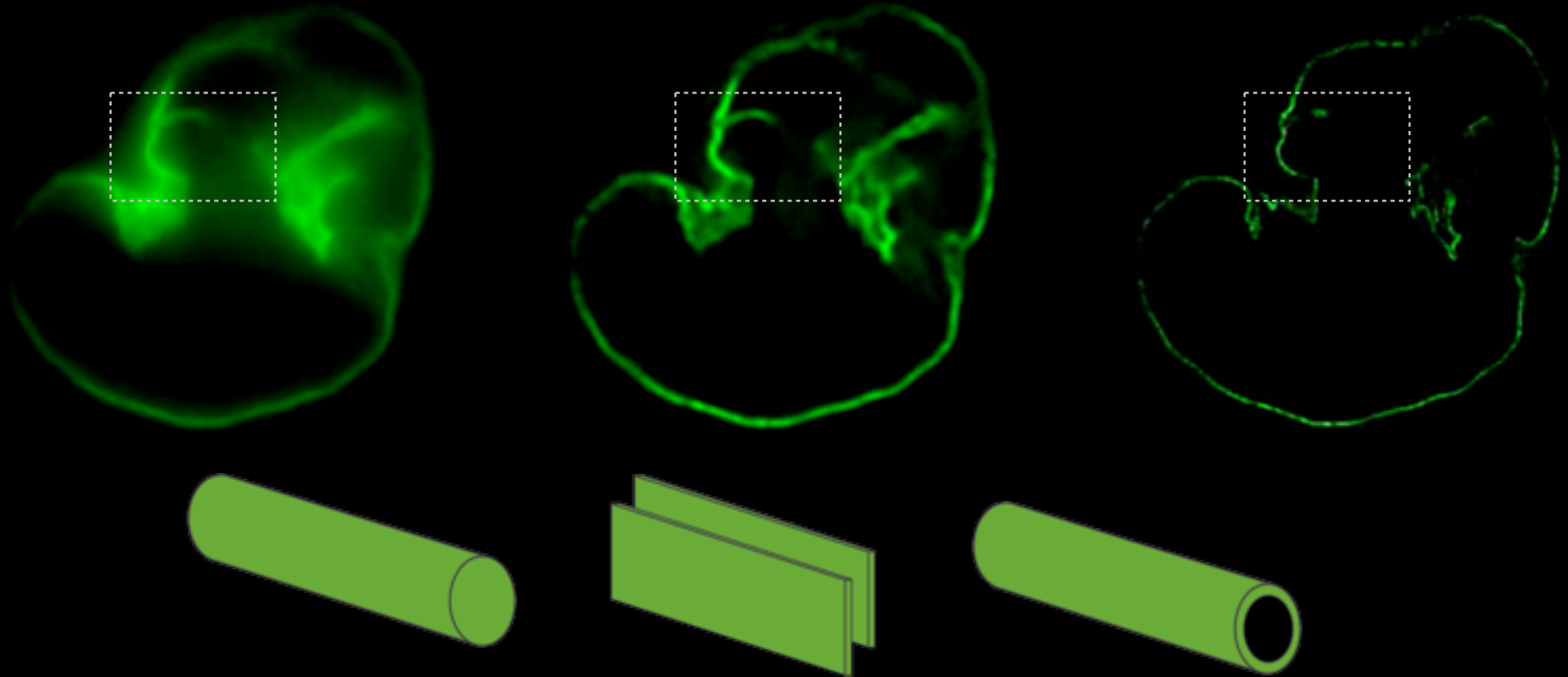
Not only resolution but also context matters! (III)

Wide-field

Wide-field deconvolution

3D-SIM

Lamin B



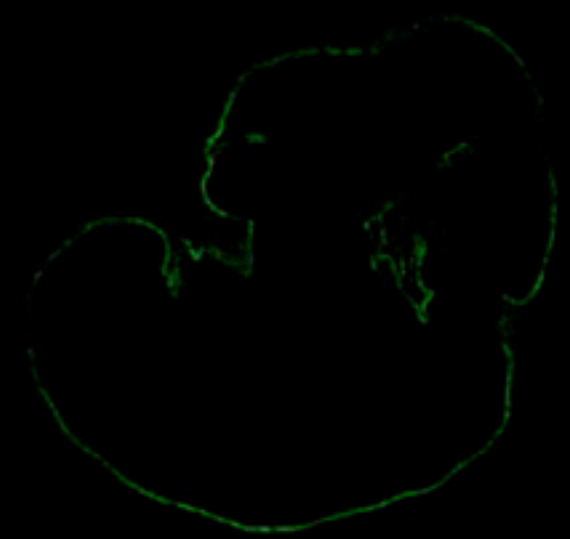
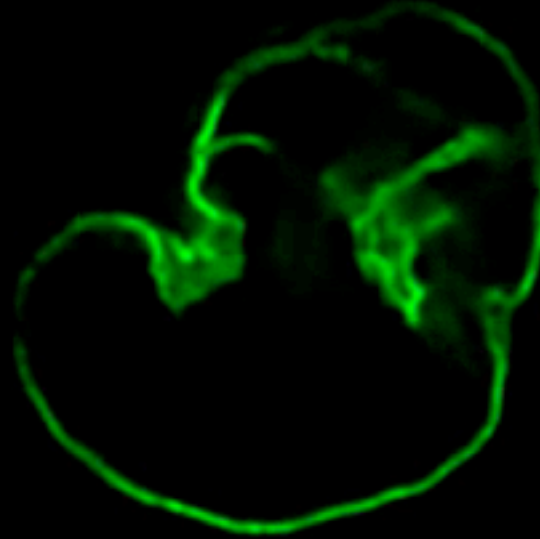
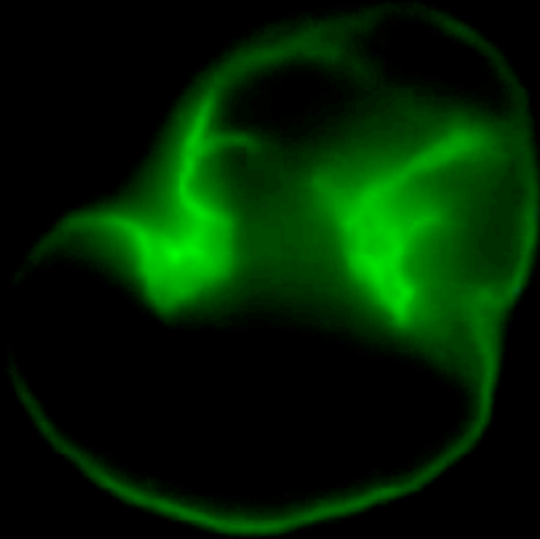
Not only resolution but also context matters! (III)

Wide-field

Wide-field deconvolution

3D-SIM

Lamin B



3D context by z-sectioning...

Not only resolution but also context matters! (III)

Wide-field

Wide-field deconvolution

3D-SIM

Lamin B
Tubulin
DAPI

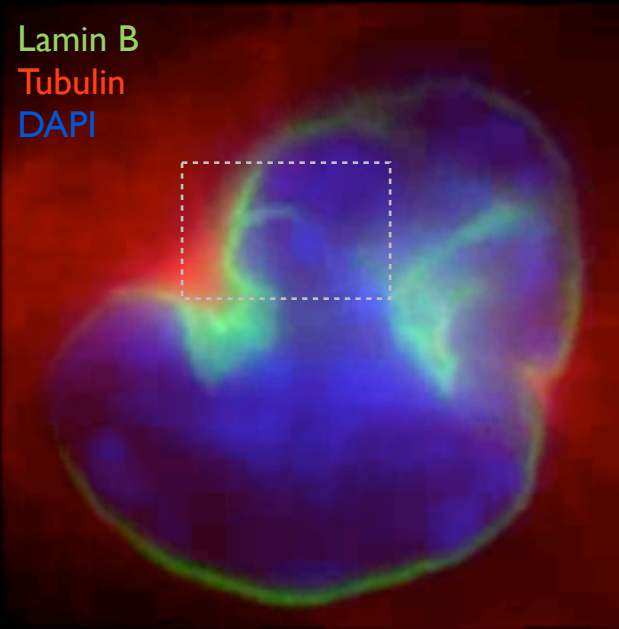


...more context by 3D **multicolor** sectioning

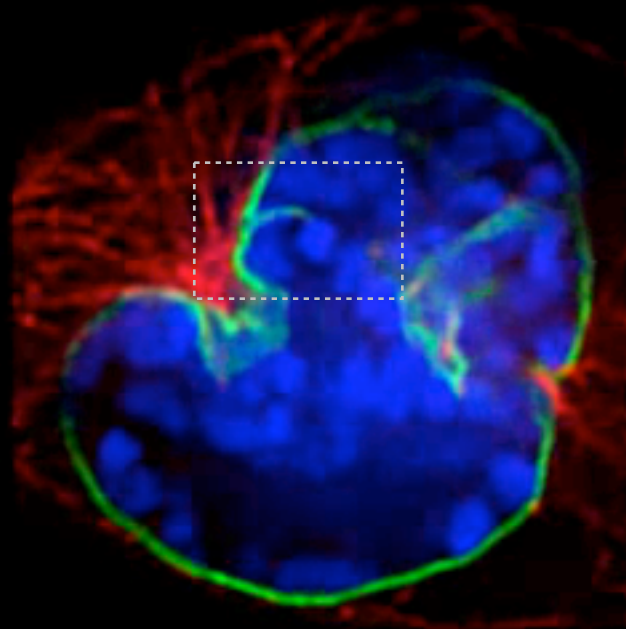
Not only resolution but also context matters! (III)

Wide-field

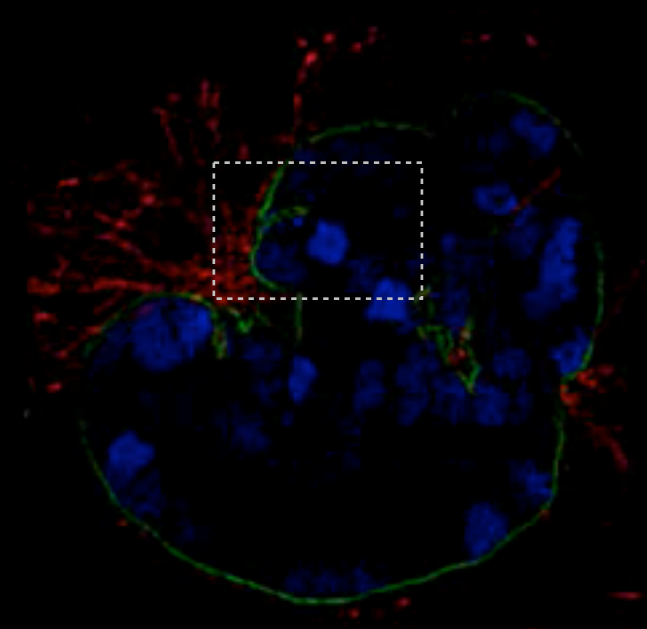
Lamin B
Tubulin
DAPI



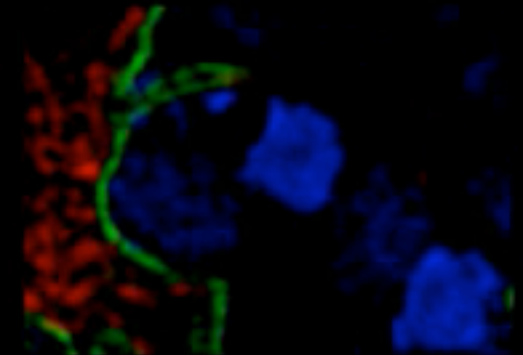
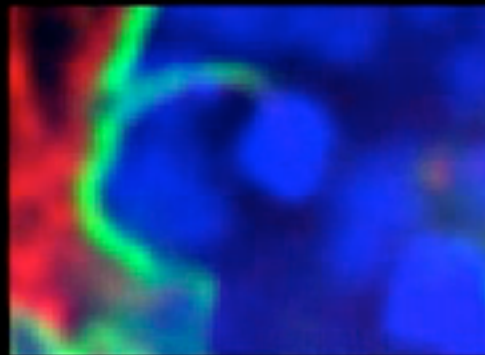
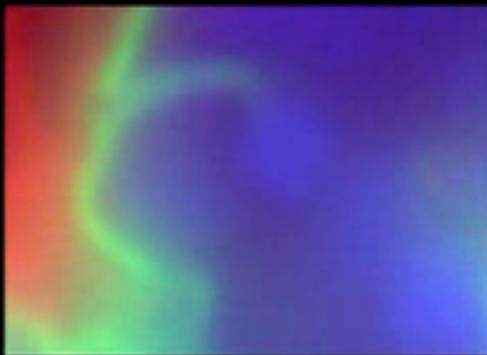
Wide-field deconvolution



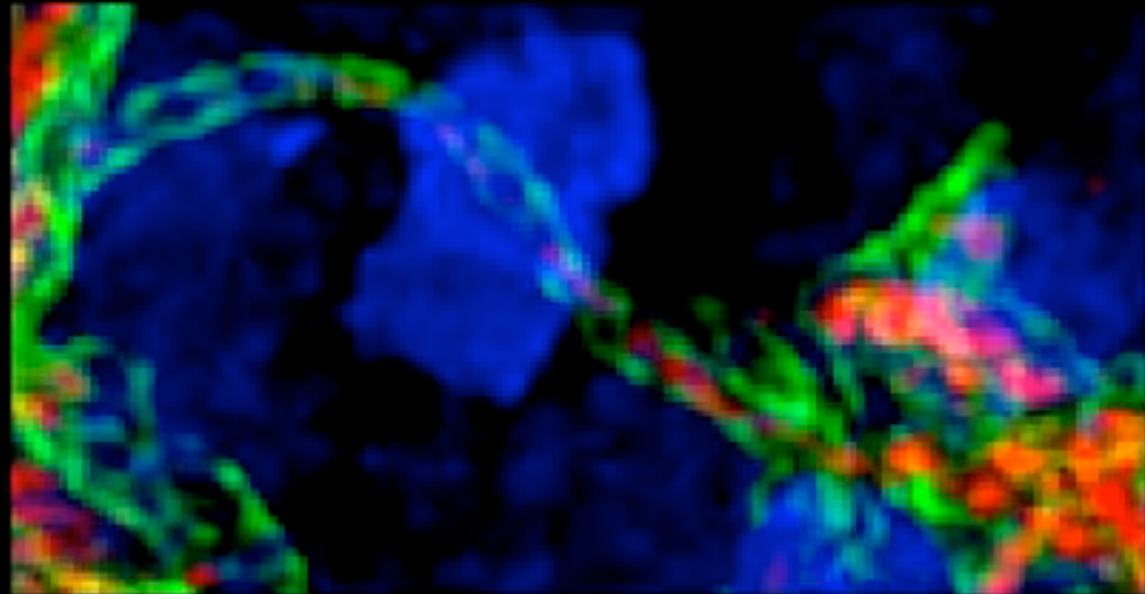
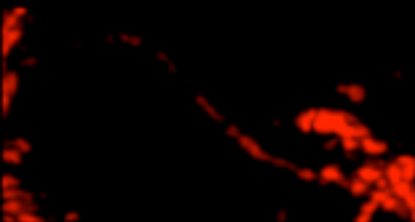
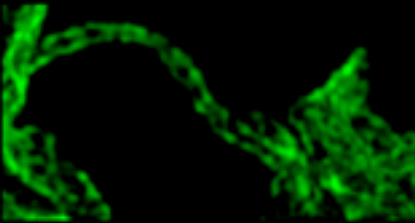
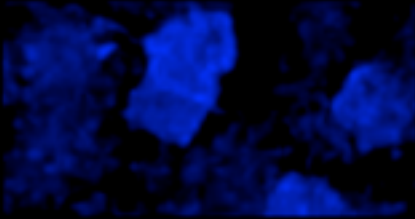
3D-SIM



...more context by 3D **multicolor** sectioning



Not only resolution but also context matters! (III)



1 μm



3D SIM example: Prophase

Lamin B

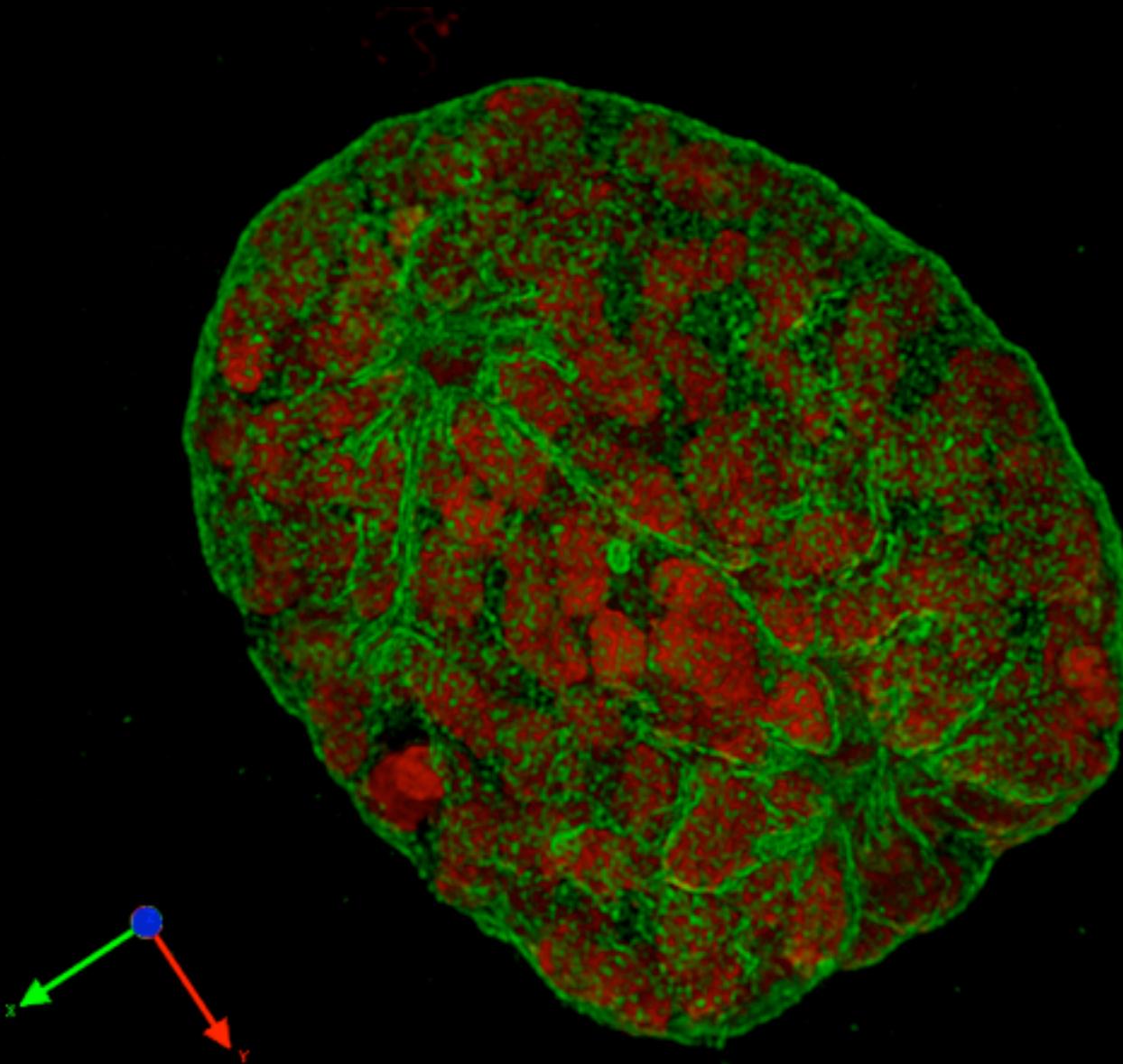
DAPI

3D volume
rendering

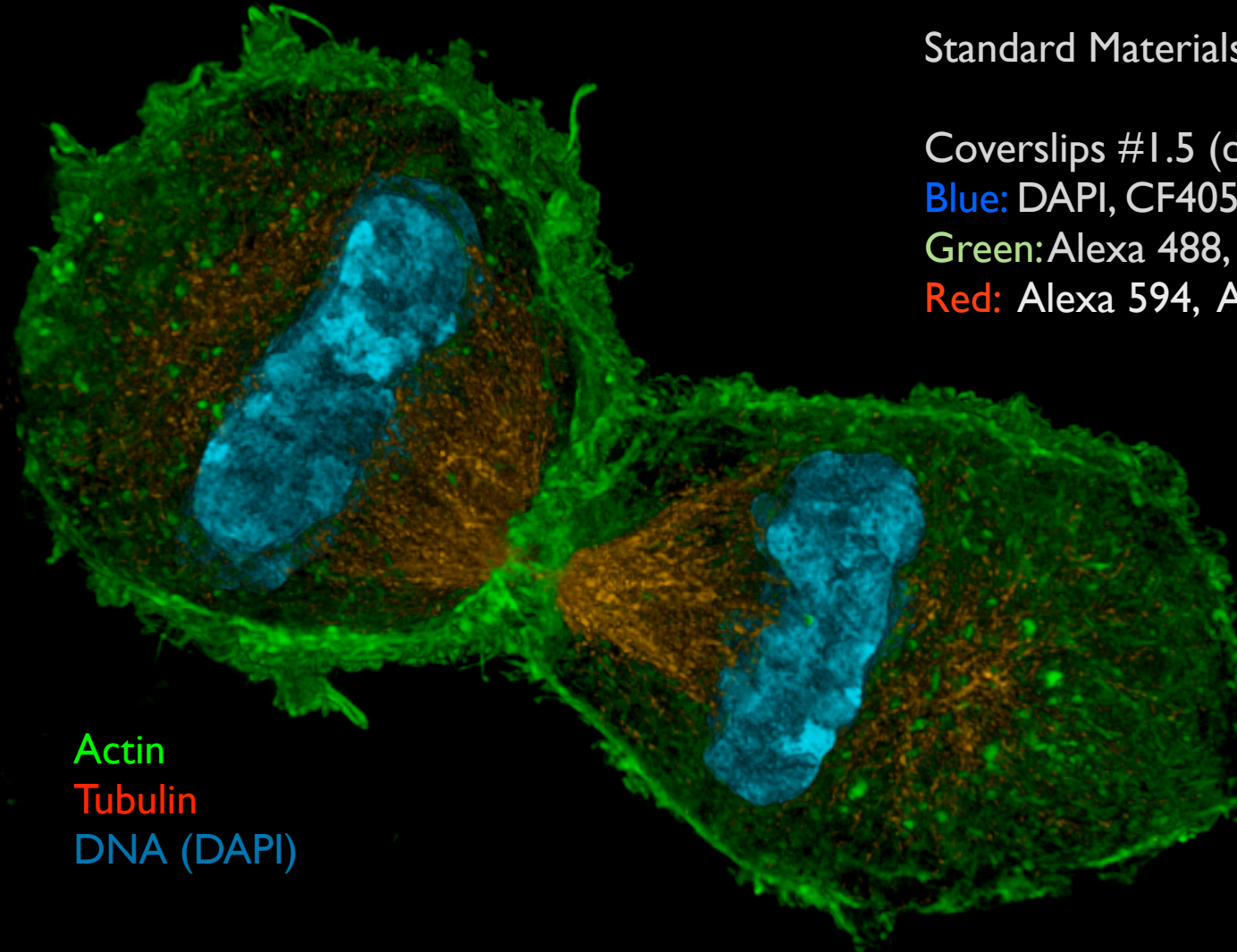
3D SIM example: Prophase

Lamin B
DAPI

3D volume
rendering



3D SIM example: Telophase



Actin
Tubulin
DNA (DAPI)

Standard Materials:

Coverslips #1.5 ($d=0.170\pm 0.005$ mm)

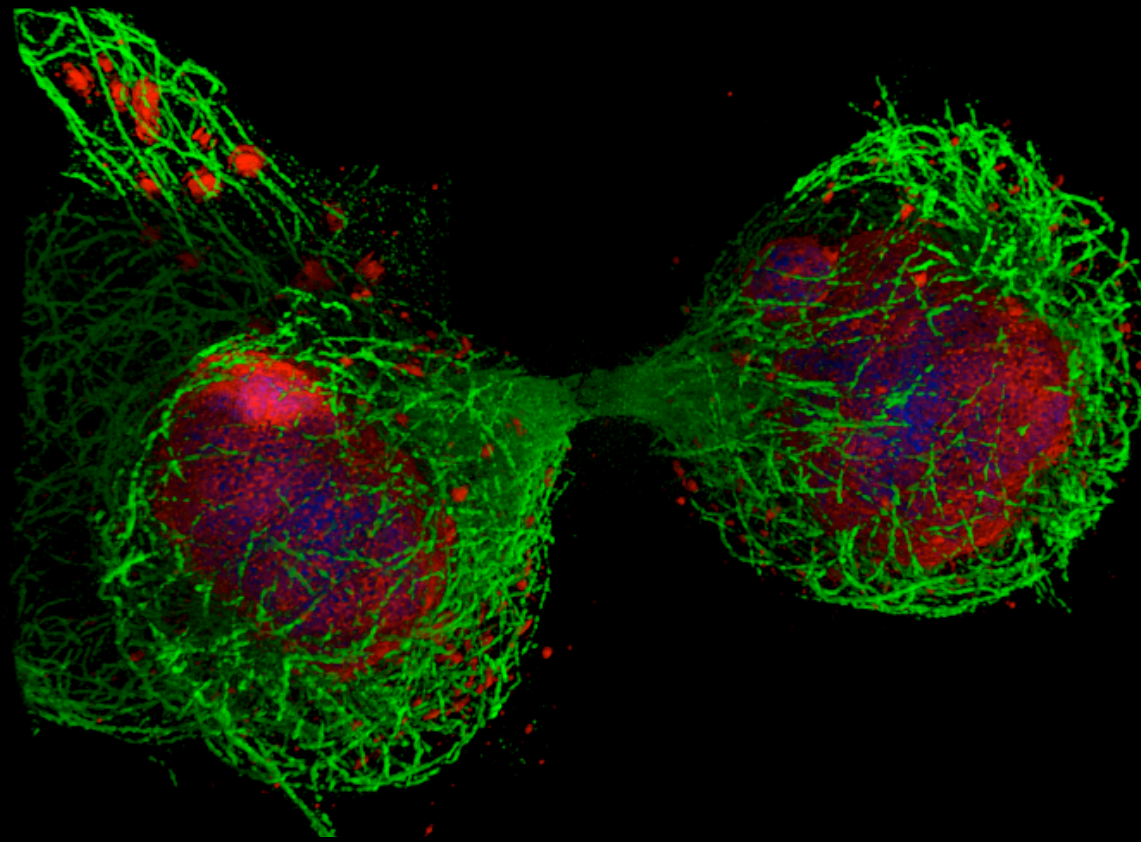
Blue: DAPI, CF405M, ATTO425

Green: Alexa 488, ATTO 488, GFP (?)

Red: Alexa 594, ATTO 590, ATTO 594

Tubulin
Lamin B
DAPI

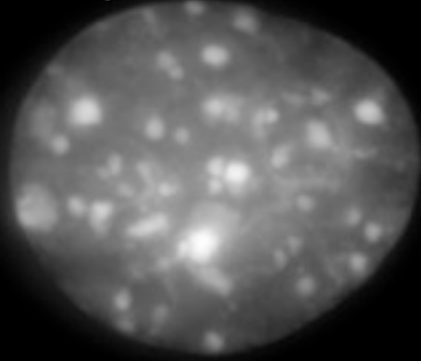
Ray tracing
rendering



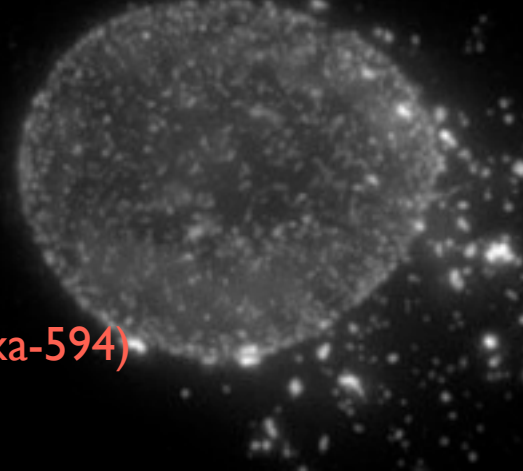
3D SIM example: Nuclear pores

WF projections

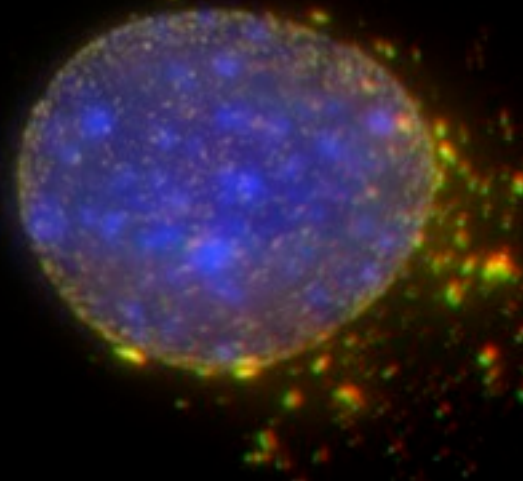
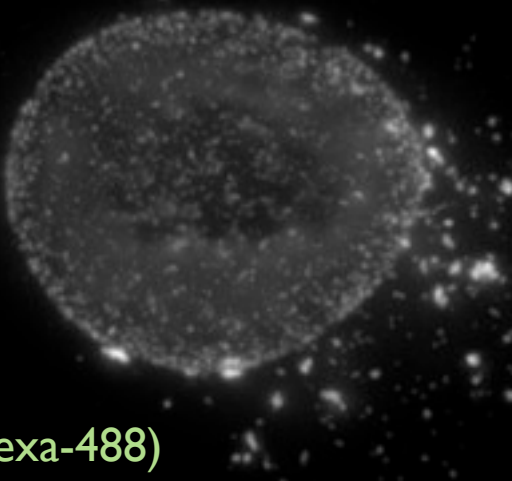
DAPI



nup153 (Alexa-594)

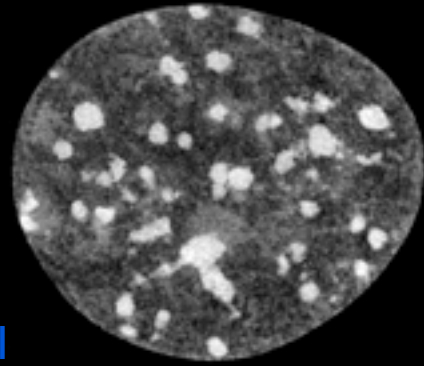


nup153 (Alexa-488)

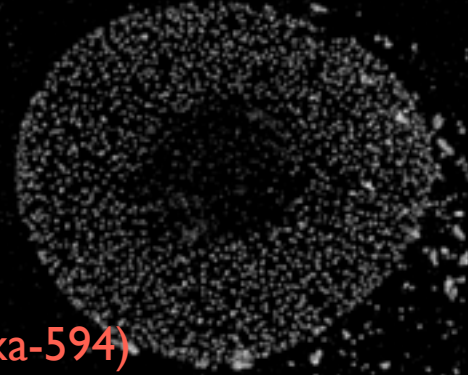


3D SIM example: Nuclear pores

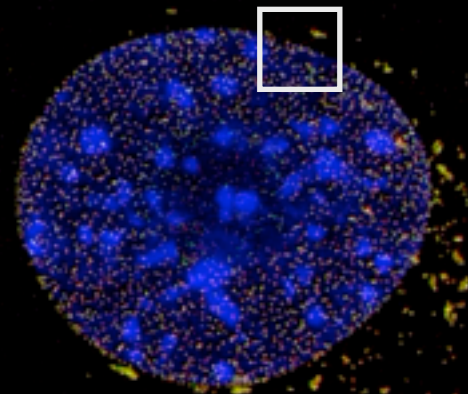
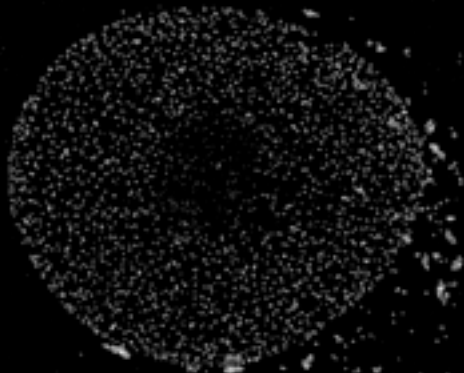
DAPI



nup153 (Alexa-594)

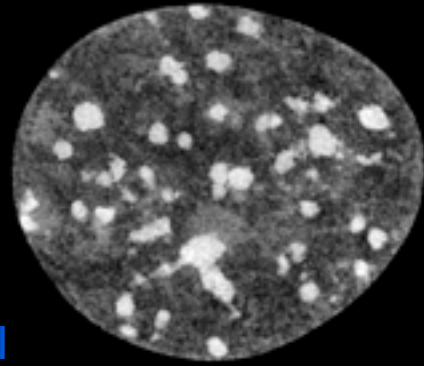


nup153 (Alexa-488)

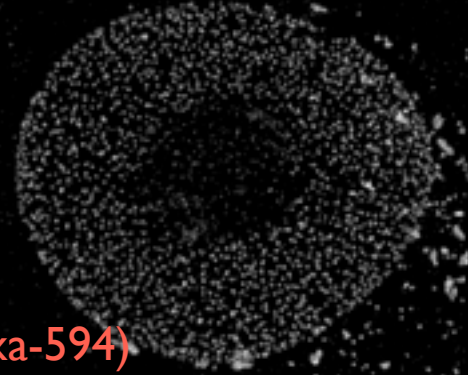


3D SIM example: Nuclear pores

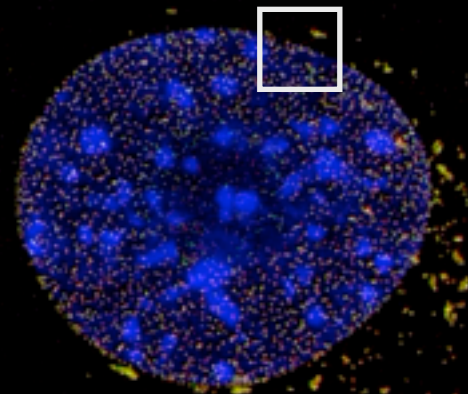
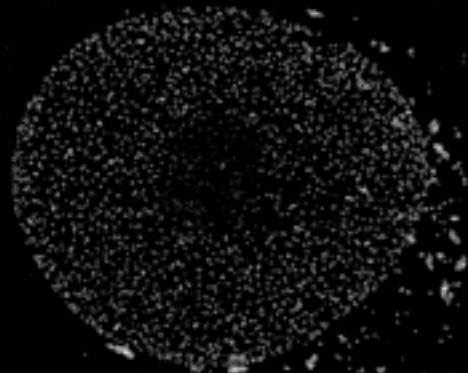
DAPI



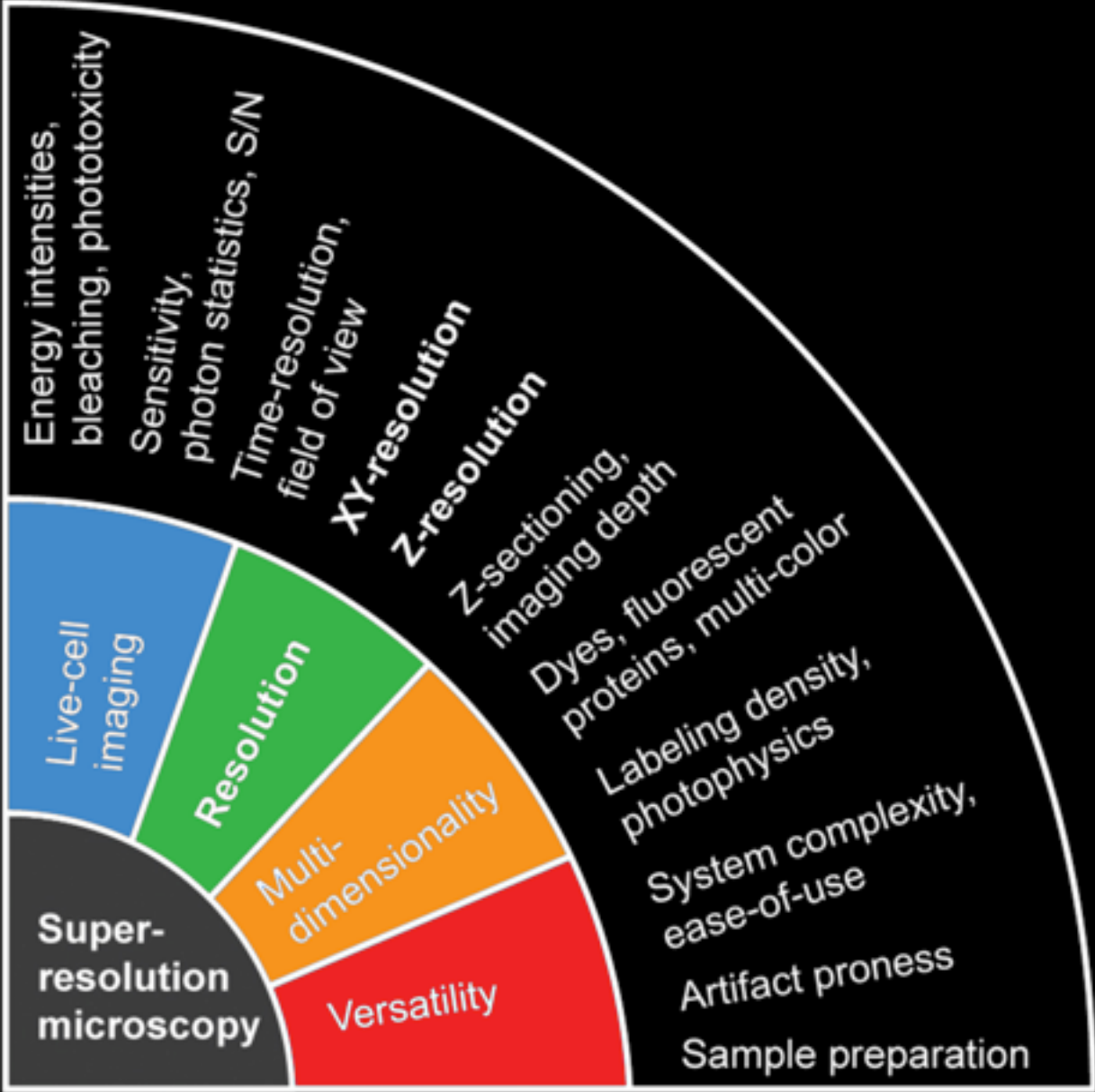
nup153 (Alexa-594)



nup153 (Alexa-488)



Super-resolution microscopy: a multi-dimensional challenge



Which super-resolution method to use ?

3D-SIM	general method - 3 colors, 3D sectioning, only modest (x2) resolution gain in xy and z (x8 volumetric) postprocessing, prone to artifacts
Live 3D-SIM	<i>OMX Blaze. Fast, large field-of-view (40 x40 μm), high sensitivity</i>
Non-linear SIM	<i>experimental setup, dx,y 40-50 nm, currently restricted to TIRF and one color only (Dronpa)</i>
TIRF	<i>only near-field, improved z-resolution only, high sensitivity and temporal resolution, „surface biology“</i>
SPIM	<i>isotropic resolution (\sim400 nm in xy, z) , deep imaging of large fields, large data, tissues and whole mounts</i>
STED	high resolution, theoretically unlimited, WYSWG, speed scales with field of view special dye requirements, bleaching issues, complex instrumentation, works best in Hell's lab.
4Pi	absolutely need a physicist. Little reported biology so far.
I5M	same specimen mounting difficulties as 4Pi, no commercial implementation.
PALM/STORM	simple hardware. software more complex, various flavours, high localization precision (\sim 20 nm in x,y), structural resolution depends on labeling density, rather slow.

„All superresolution techniques excel in certain aspects and fail in others—the best technique will be determined by the demands of the application.“ Rego et al. 2012, PNAS



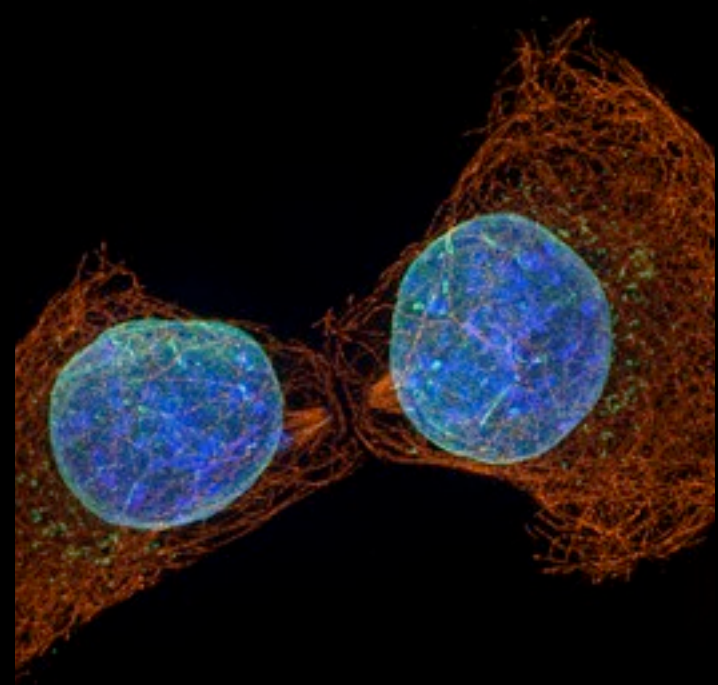
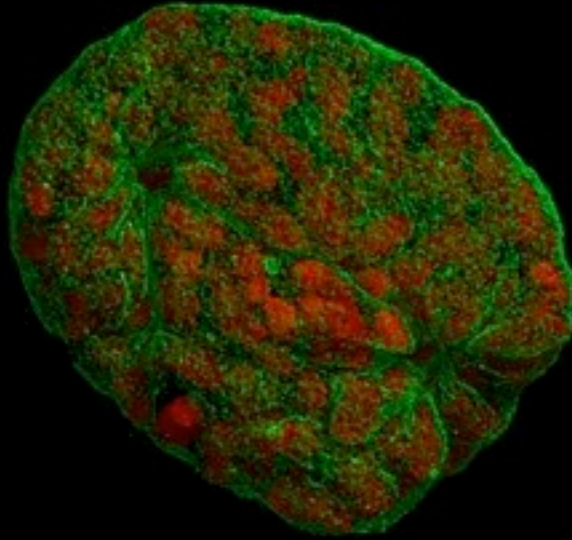
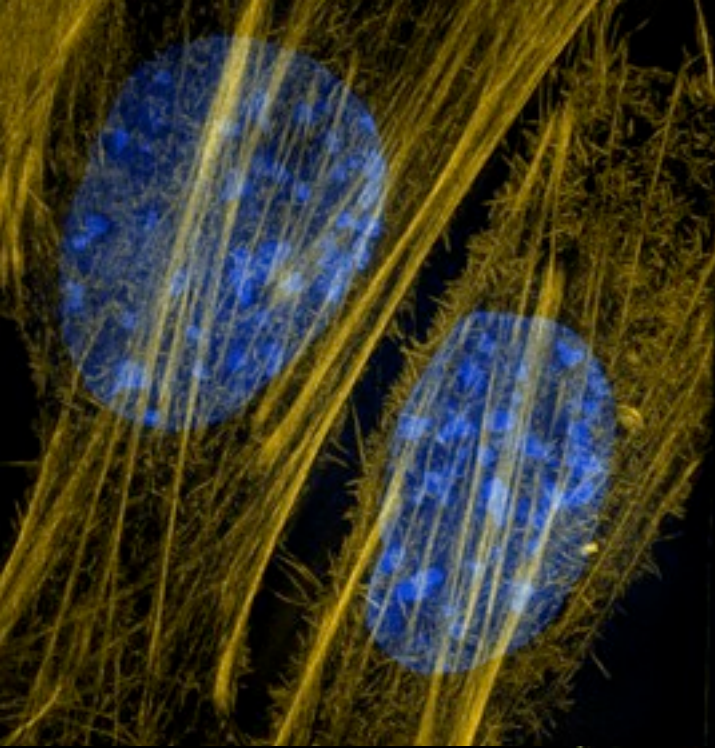
What, all?!

How many are there?

...let's go through the image, point-by-point...

79.345!

Pontillism sucks!



The End

